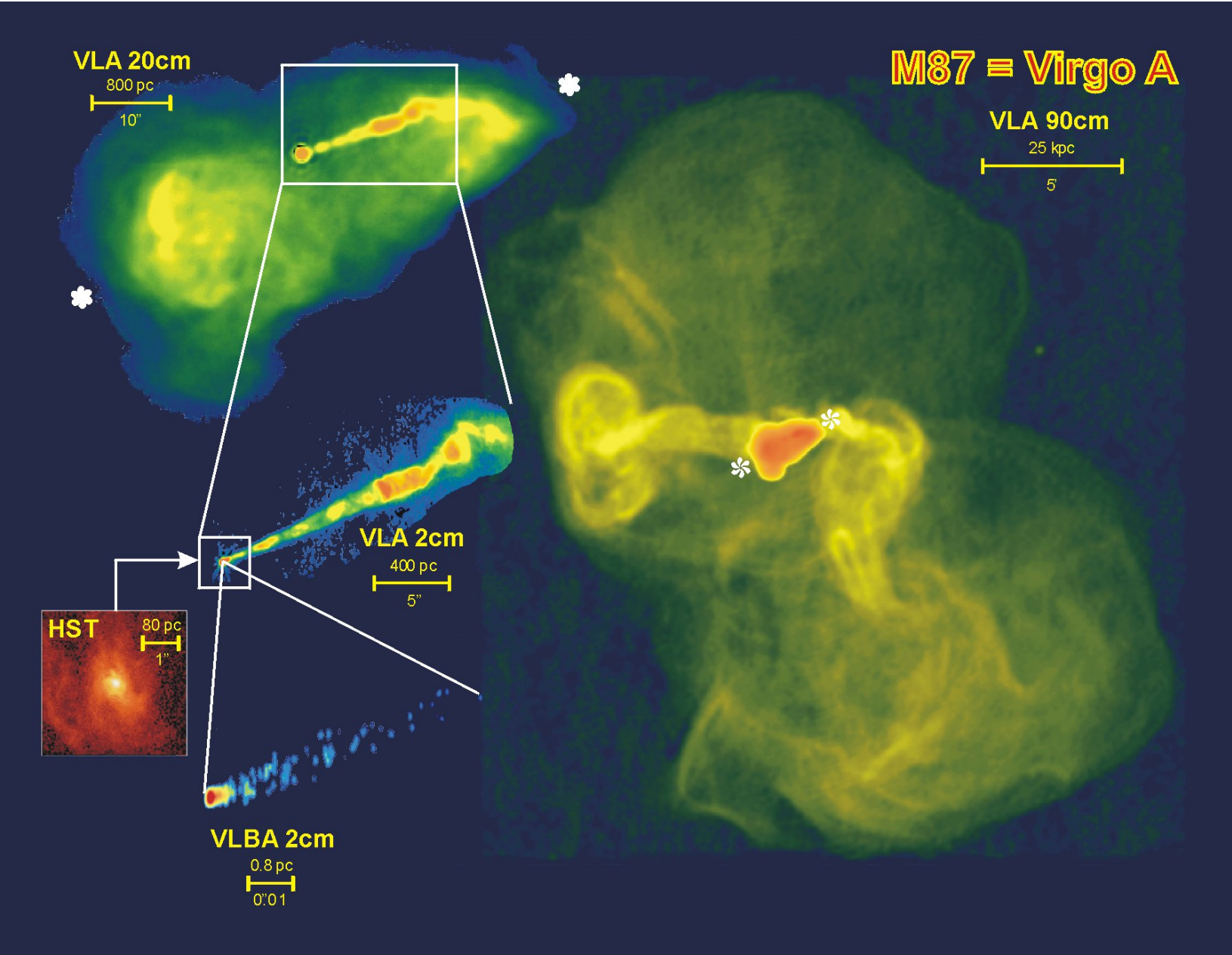


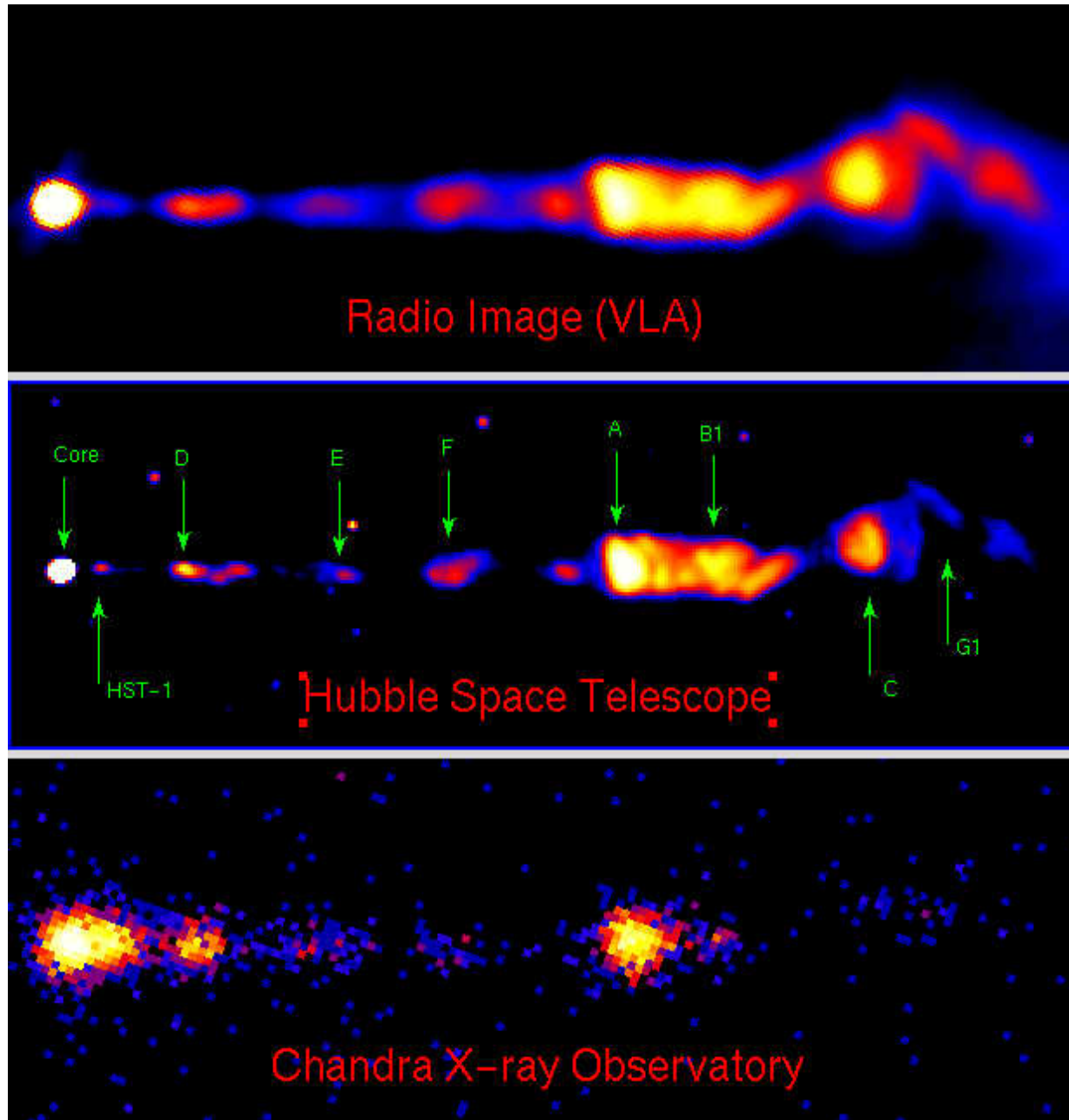
Relativistic jet dynamics and the role of the magnetic field

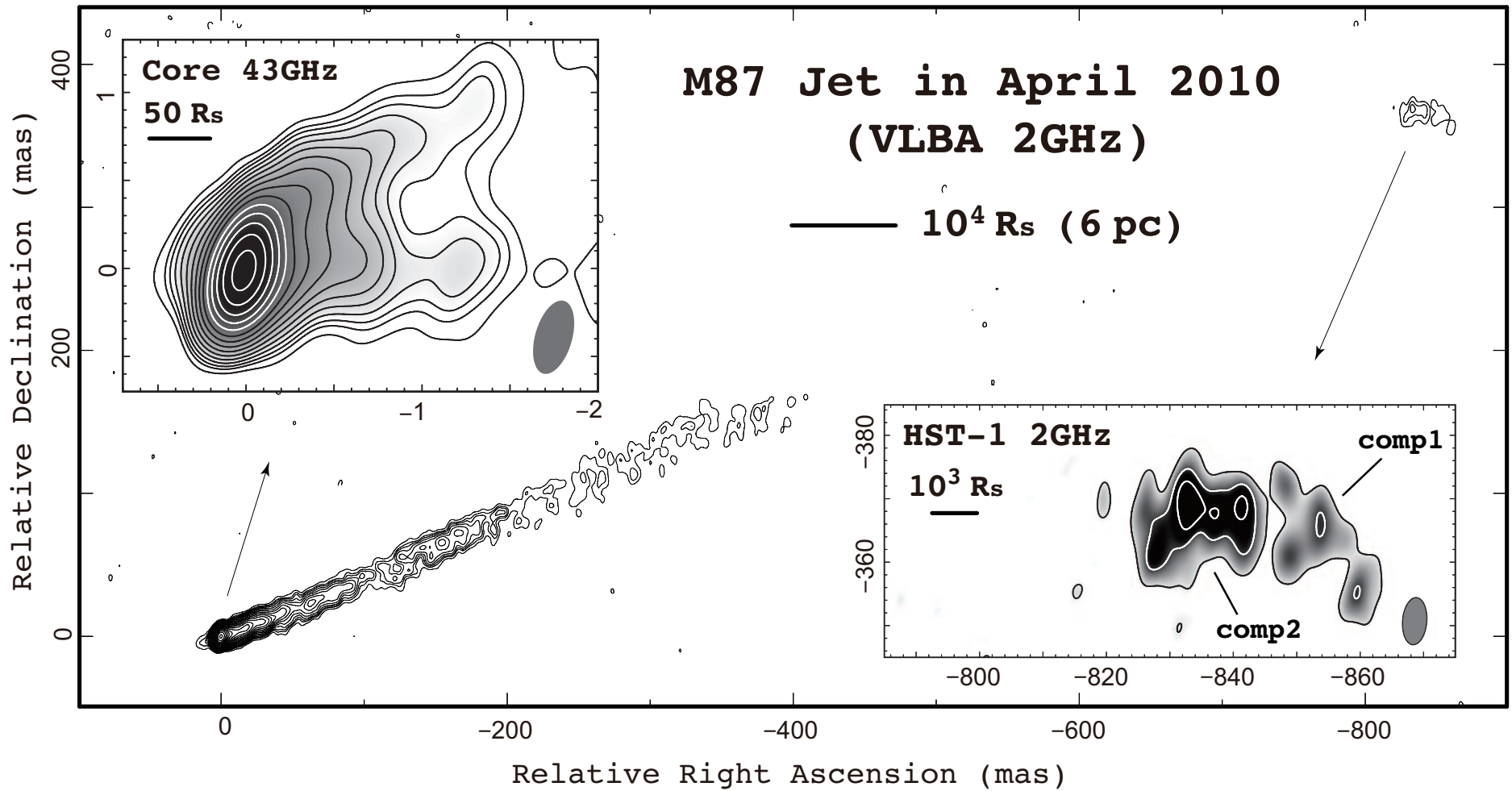
Nektarios Vlahakis
University of Athens

Outline

- introduction
- collimation-acceleration paradigm
- rarefaction acceleration in GRB outflows



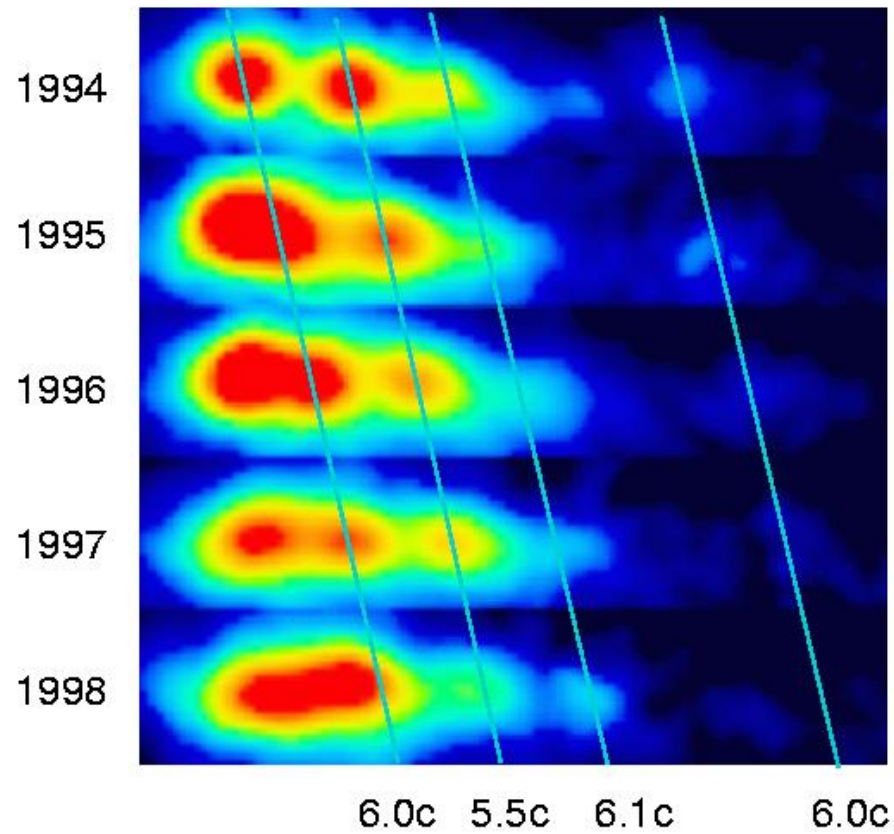
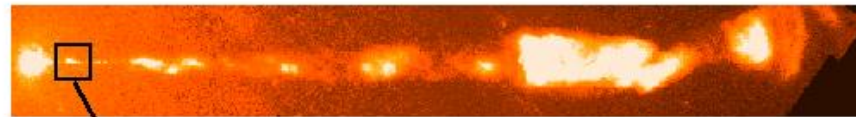




(Hada et al)

Jet speed

Superluminal Motion in the M87 Jet



On the bulk acceleration

- More distant components have higher apparent speeds
- Brightness temperature increases with distance (Lee, Lobanov, et al)
- A more general argument on the acceleration (Sikora et al):
 - ★ lack of bulk-Compton features \rightarrow small ($\gamma < 5$) bulk Lorentz factor at $\lesssim 10^3 r_g$
 - ★ the γ saturates at values \sim a few 10 around the blazar zone ($10^3 - 10^4 r_g$)

So, relativistic AGN jets undergo the bulk of their acceleration on parsec scales (\gg size of the central black hole)

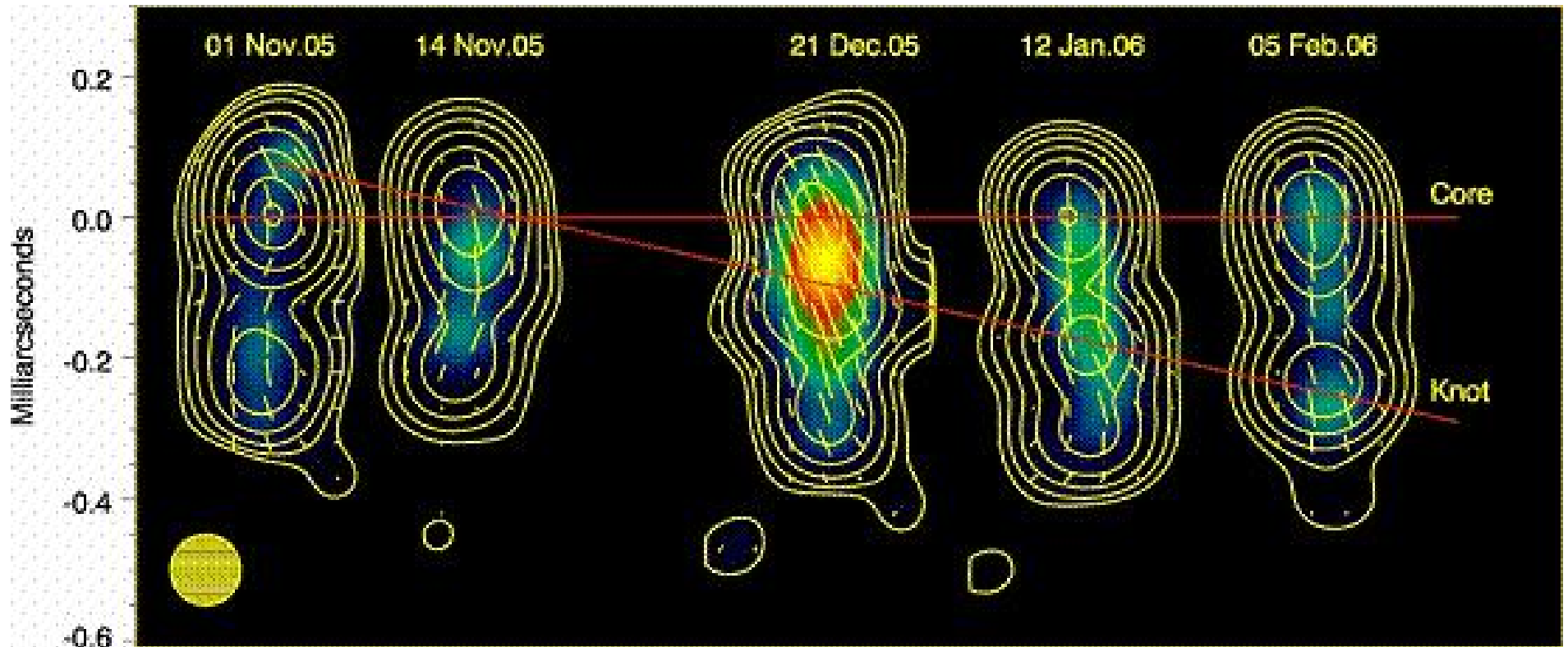
- Sikora et al also argue that the protons are the dynamically important component in the outflow.

Hydro-Dynamics

- In case $n_e \sim n_p$, $\gamma_{\max} \sim kT_i/m_p c^2 \sim 1$ even with $T_i \sim 10^{12} K$
- If $n_e \neq n_p$, $\gamma_{\max} \sim (n_e/n_p) \times (kT_i/m_p c^2)$ could be $\gg 1$
- With some heating source, $\gamma_{\max} \gg 1$ is in principle possible

However, even in the last two cases, **HD is unlikely to work** because the HD acceleration saturates at distances comparable to the sonic surface where gravity is still important, i.e., very close to the disk surface (certainly at $\ll 10^3 r_g$)

Polarization

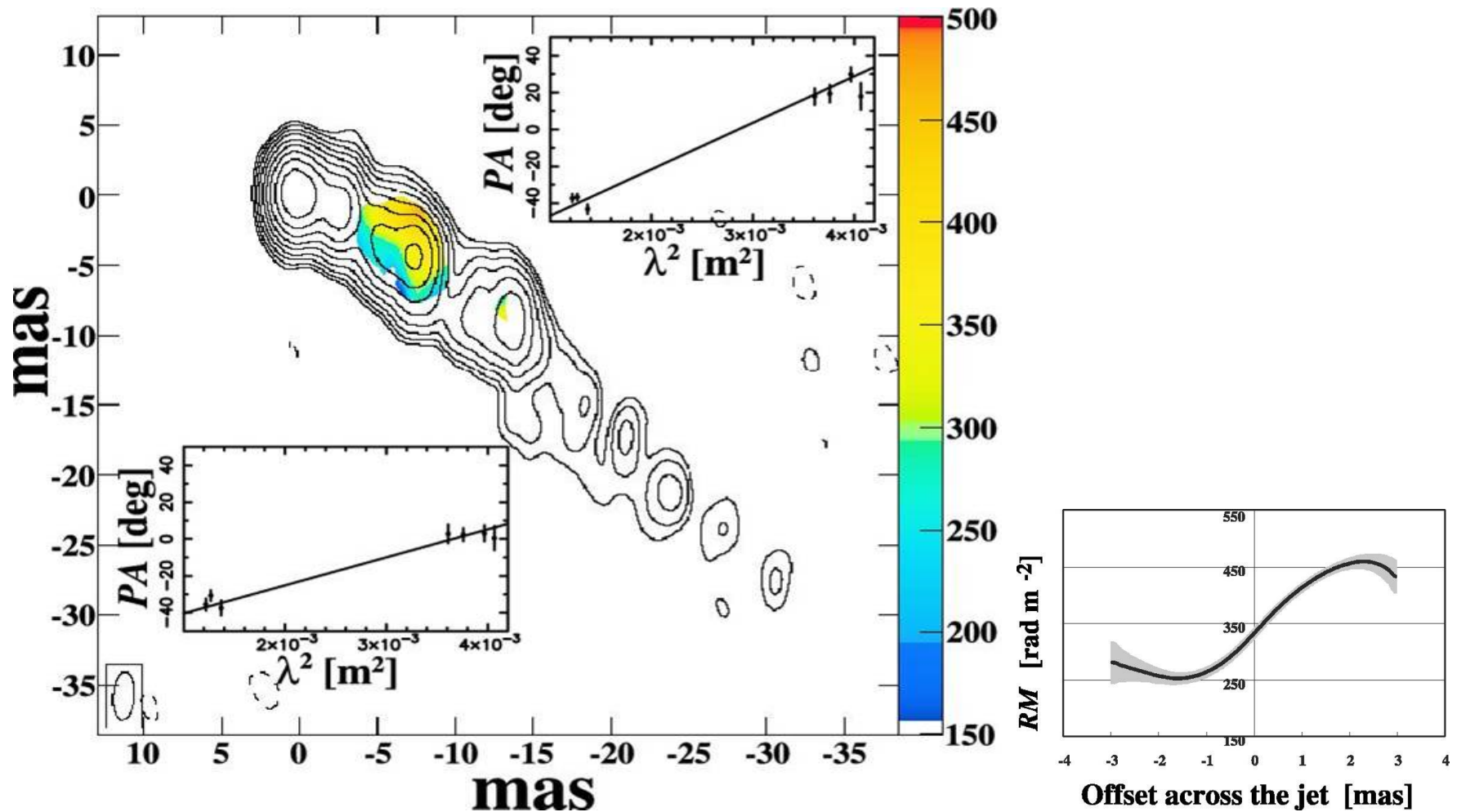


(Marscher et al 2008, Nature)

observed $E_{\text{rad}} \perp B_{\perp \text{los}}$

(modified by Faraday rotation and relativistic effects)

Faraday RM gradients across the jet

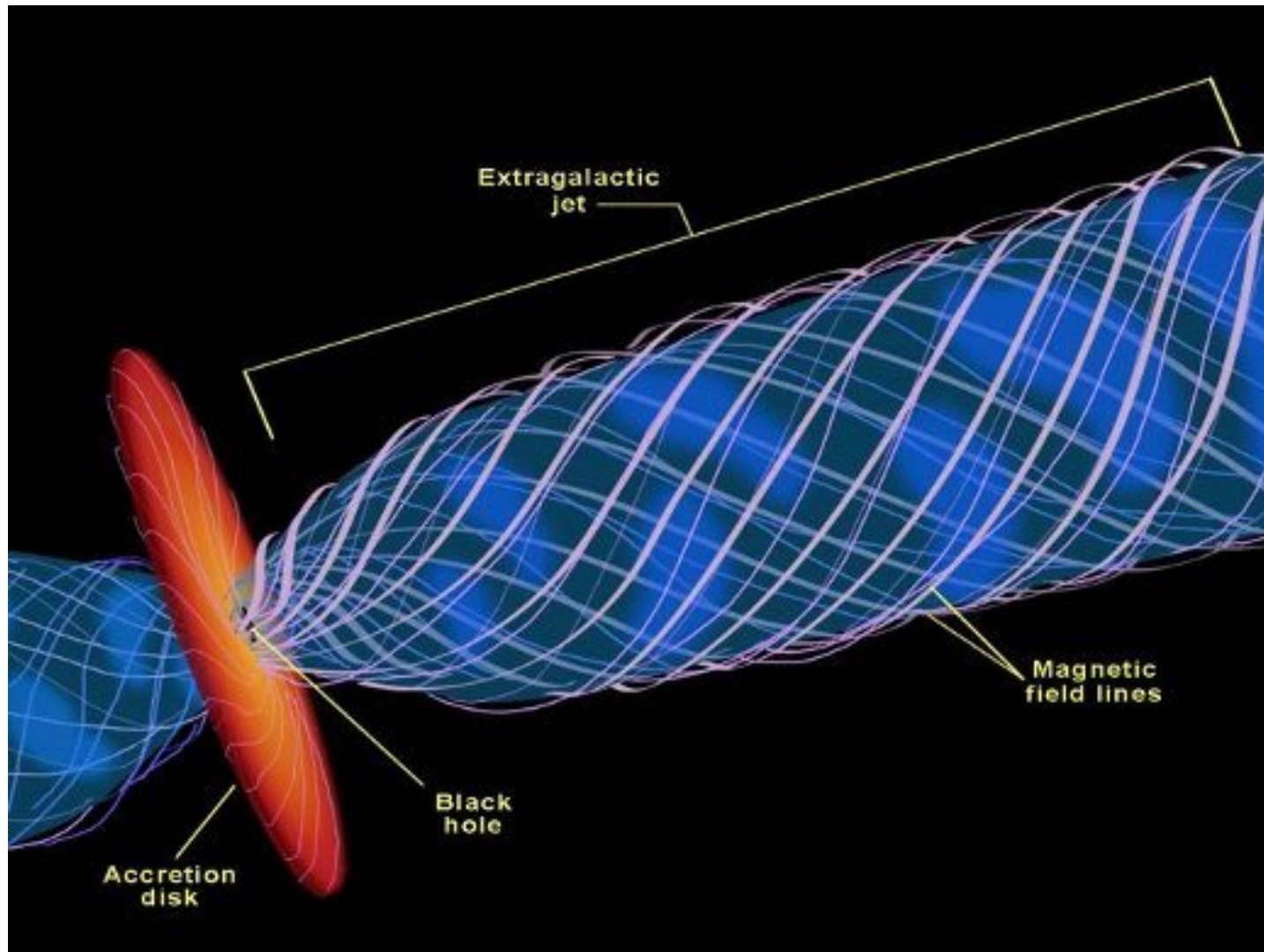


(Asada et al)

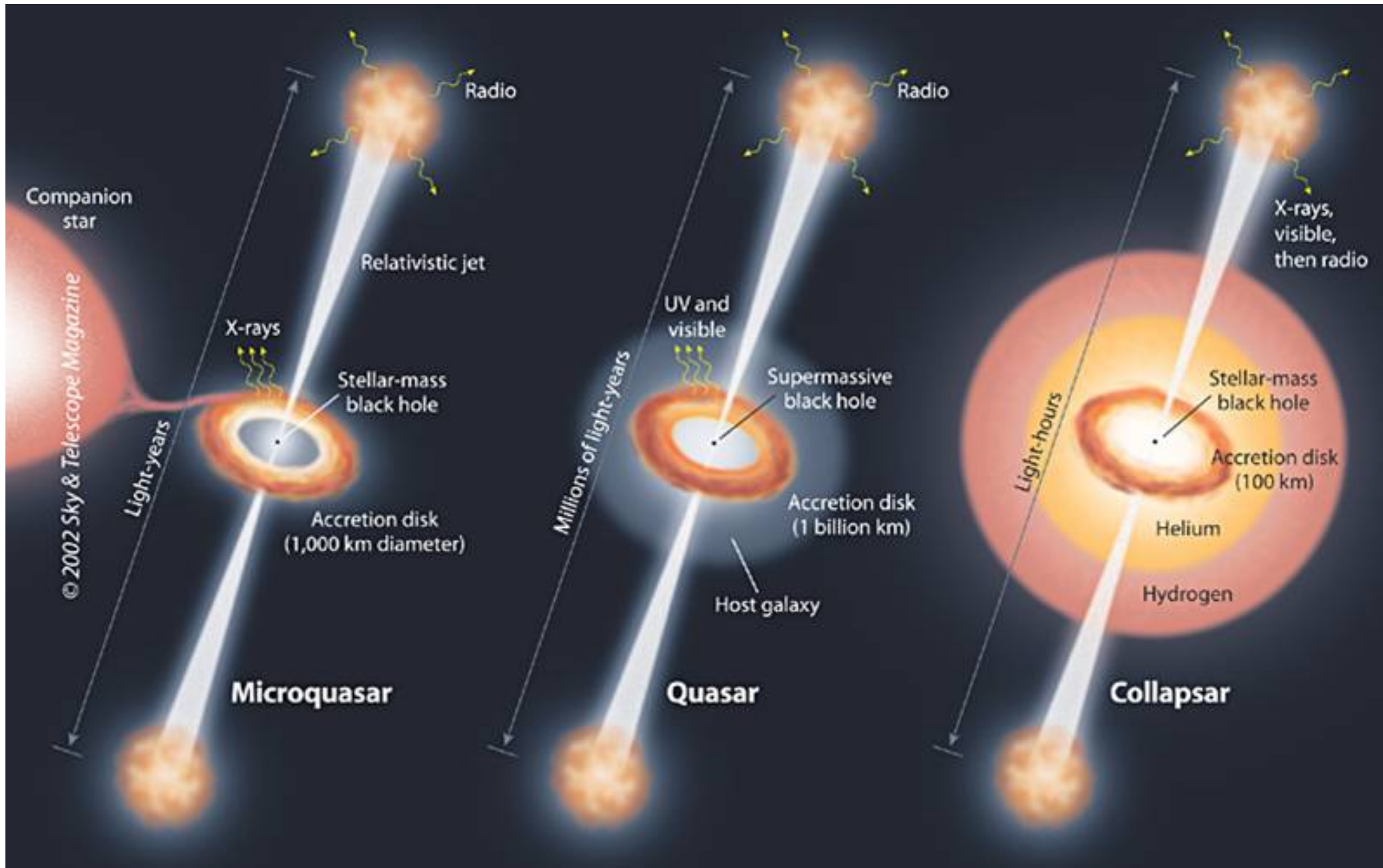
helical field surrounding the emitting region (Gabuzda)

What magnetic fields can do

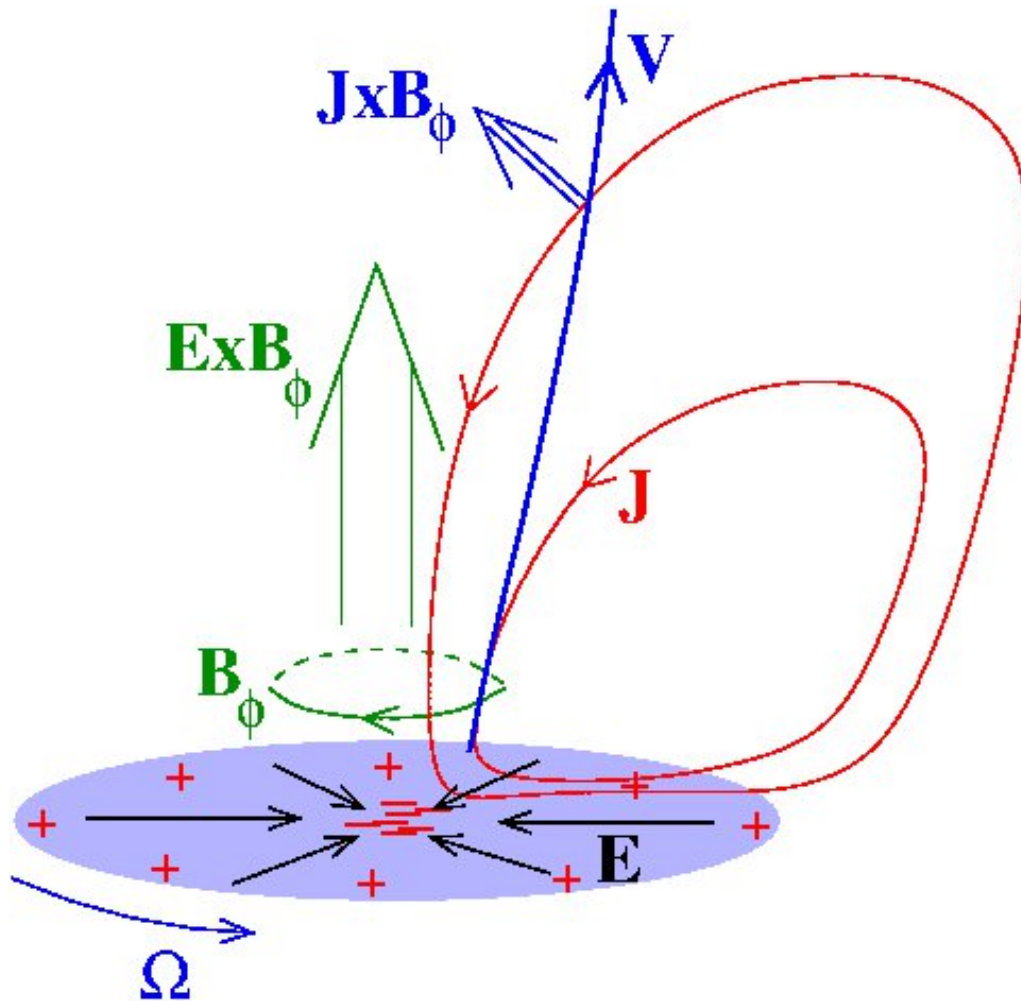
- ★ extract energy (Poynting flux)
- ★ extract angular momentum
- ★ transfer energy and angular momentum to matter
- ★ explain relatively large-scale acceleration
- ★ self-collimation
- ★ synchrotron emission
- ★ polarization and RM maps



B field from advection, or dynamo, or cosmic battery (Poynting-Robertson drag).



A unipolar inductor



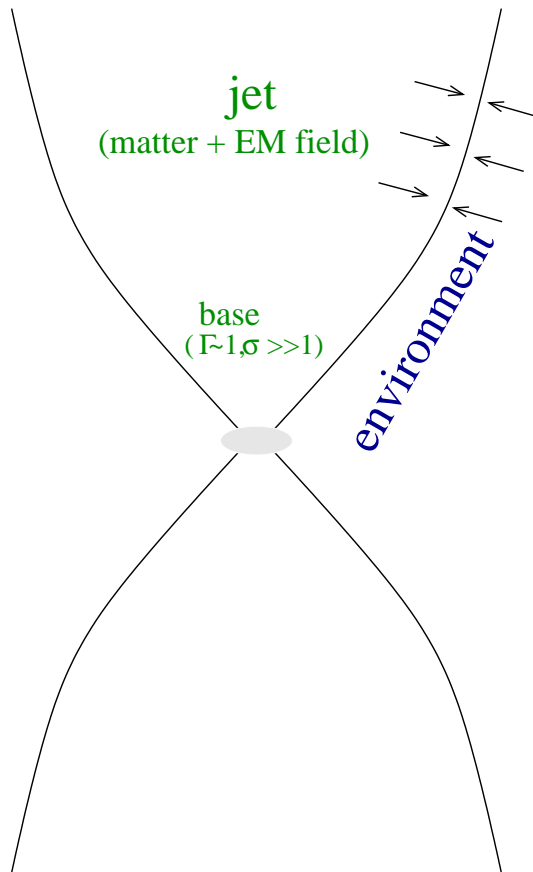
current $\leftrightarrow B_\phi$
 Poynting flux $\frac{c}{4\pi} E B_\phi$ is
 extracted (angular momentum
 as well)

The Faraday disk could be the rotating accretion disk, or the frame dragging if energy is extracted from the ergosphere of a rotating black hole (Blandford & Znajek mechanism)

How to model magnetized outflows?

- ★ as pure electromagnetic energy (force-free, magnetodynamics, electromagnetic outflows):
 - ignore matter inertia (reasonable near the origin)
 - this by assumption does not allow to study the transfer of energy from Poynting to kinetic
 - wave speed = c → no shocks
 - there may be some dissipation (e.g. reconnection) → radiation
- ★ as magneto-hydro-dynamic flow
 - the force-free case is included as the low inertia limit
 - the back reaction from the matter to the field is included

Magnetized outflows



- Extracted energy per time $\dot{\mathcal{E}}$ mainly in the form of Poynting flux (magnetic fields tap the rotational energy of the compact object or disk)

$$\dot{\mathcal{E}} = \frac{c}{4\pi} \underbrace{\frac{r}{r_{lc}} B_p}_{E} B_\phi \times (\text{area}) \approx \frac{c}{2} B^2 r^2$$

- Ejected mass per time \dot{M}
- The $\mu \equiv \dot{\mathcal{E}} / \dot{M} c^2$ gives the maximum possible bulk Lorentz factor of the flow
- **Magnetohydrodynamics:**
matter (velocity, density, pressure)
+ large scale electromagnetic field

Basic questions

☞ bulk acceleration

- **thermal** (due to ∇P) \rightarrow velocities up to C_s
- **magnetocentrifugal** \rightarrow velocities up to $V_{\phi i}$
- **relativistic thermal** (thermal fireball) gives $\gamma \sim \left(\frac{\text{enthalpy}}{\text{mass} \times c^2} \right)_i$.
- **magnetic** ($\mathbf{J} \times \mathbf{B}$ force)
acceleration efficiency $\gamma_{\infty}/\mu = ?$
terminal $\gamma_{\infty} ?$

☞ collimation

hoop-stress + electric force

degree of collimation ?

jet opening angle ?

some key steps on MHD modeling

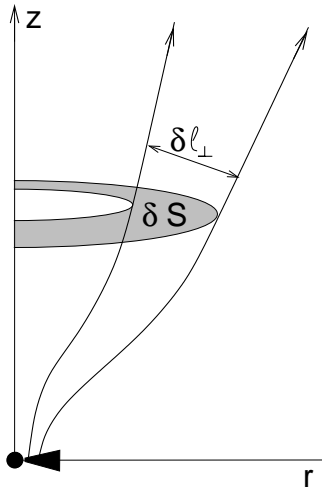
- Michel 1969: assuming monopole flow (crucial) → inefficient acceleration with $\gamma_\infty \approx \mu^{1/3} \ll \mu$
- Li, Chiueh & Begelman 1992; Contopoulos 1994: cold self-similar model → $\gamma_\infty \approx \mu/2$ (50% efficiency)
- Vlahakis & Königl 2003: generalization of the self-similar model (including thermal and radiation effects) → $\gamma_\infty \approx \mu/2$ (50% efficiency)
- Vlahakis 2004: complete asymptotic transfield force-balance connect the flow-shape (collimation) with acceleration explain why Michel's model is inefficient
- Beskin & Nokhrina 2006: parabolic jet with $\gamma_\infty \approx \mu/2$

some key steps (cont'd)

- Komissarov, Barkov, Vlahakis & Königl 2007 and Komissarov, Vlahakis, Königl & Barkov 2009:
possible for the first time to simulate high γ MHD flows and follow the acceleration up to the end
+ analytical scalings
+ role of causality, **role of external pressure**
- Tchekhovskoy, McKinney & Narayan, 2009: simulations of nearly monopolar flow (more detailed than in Komissarov et al 2009)
Even for nearly monopolar flow the acceleration is efficient near the rotation axis
- Lyubarsky 2009:
generalization of the analytical results of Vlahakis 2004 and Komissarov et al 2009

“Standard” model for magnetic acceleration

☞ component of the momentum equation



$$\gamma n (\mathbf{V} \cdot \nabla) (\gamma w \mathbf{V}) = -\nabla p + J^0 \mathbf{E} + \mathbf{J} \times \mathbf{B}$$

along the flow (wind equation): $\gamma \approx \mu - \mathcal{F}$
where $\mathcal{F} \propto r^2 n \gamma V_p = r^2 \times$ mass flux

since mass flux $\times \delta S = \text{const}$,

$$\mathcal{F} \propto r^2 / \delta S \propto r / \delta \ell_{\perp}$$

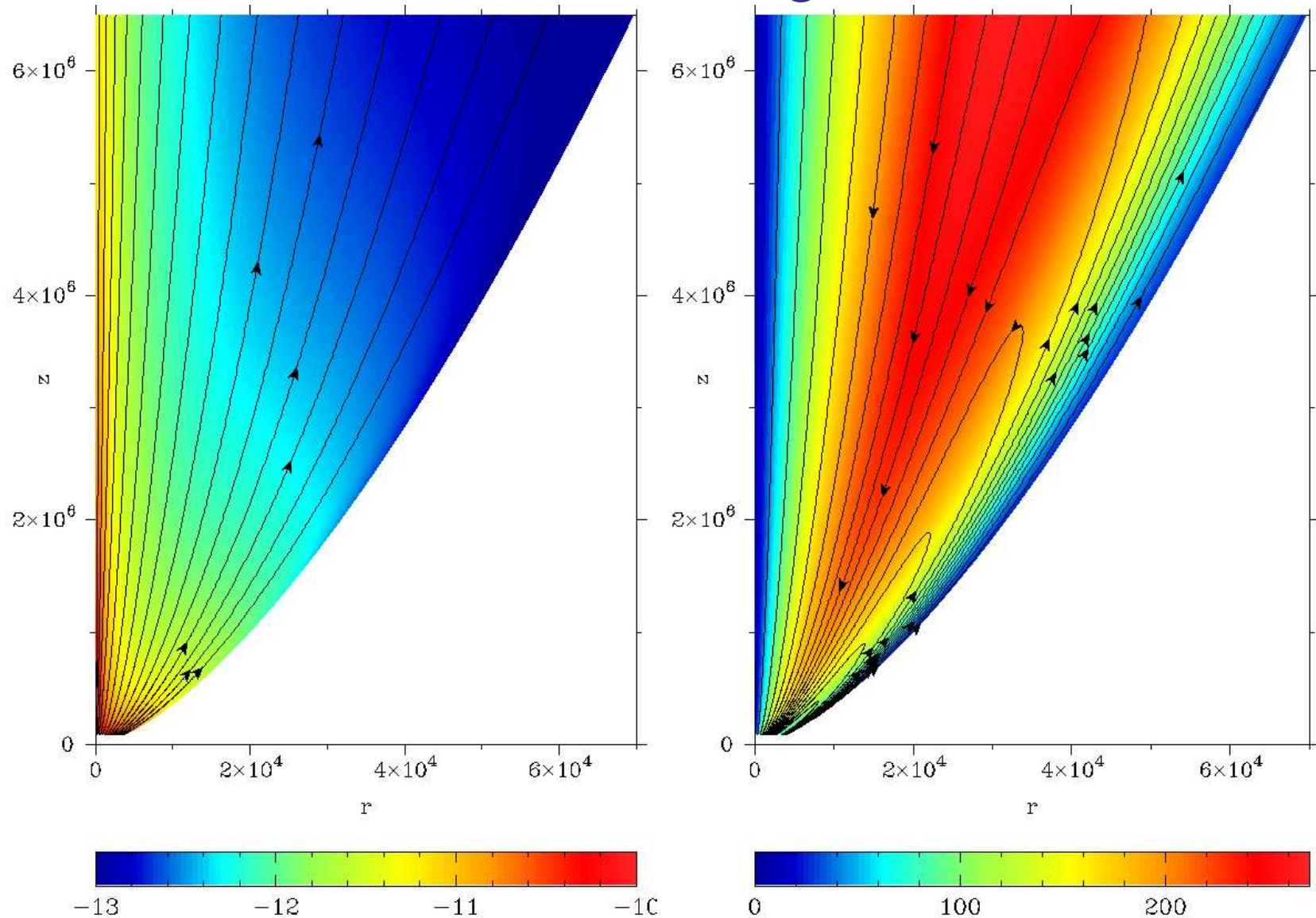
acceleration requires the separation between streamlines to increase faster than the cylindrical radius

the collimation-acceleration paradigm:

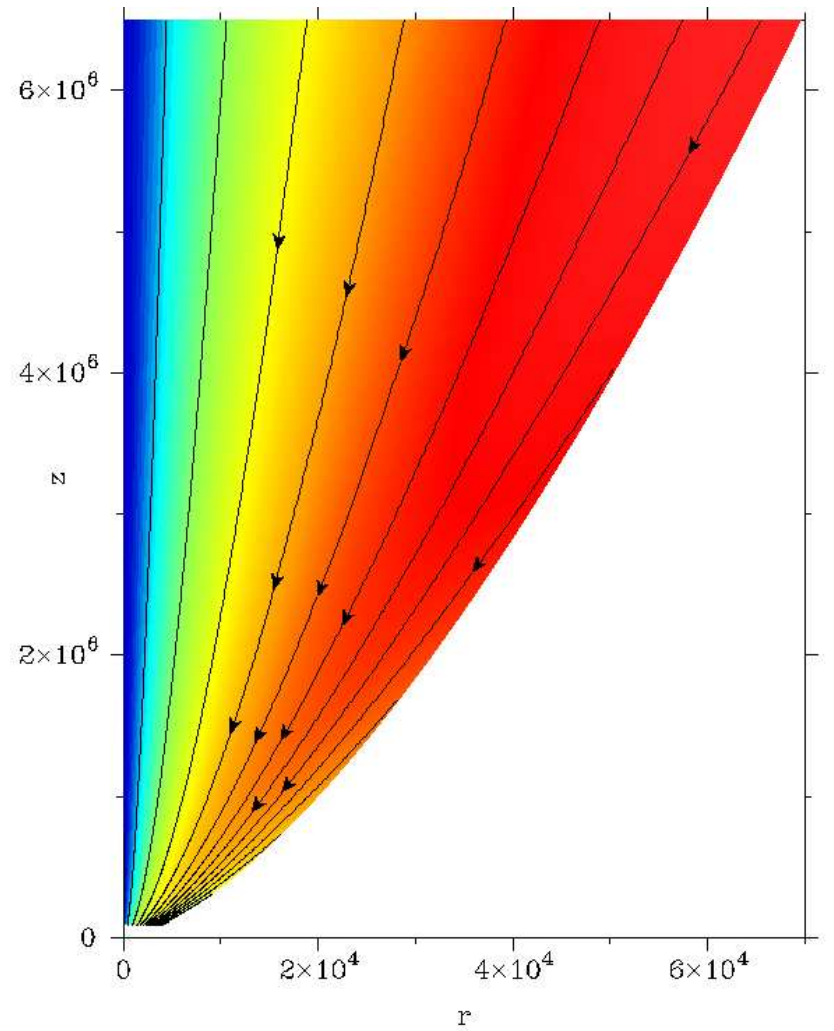
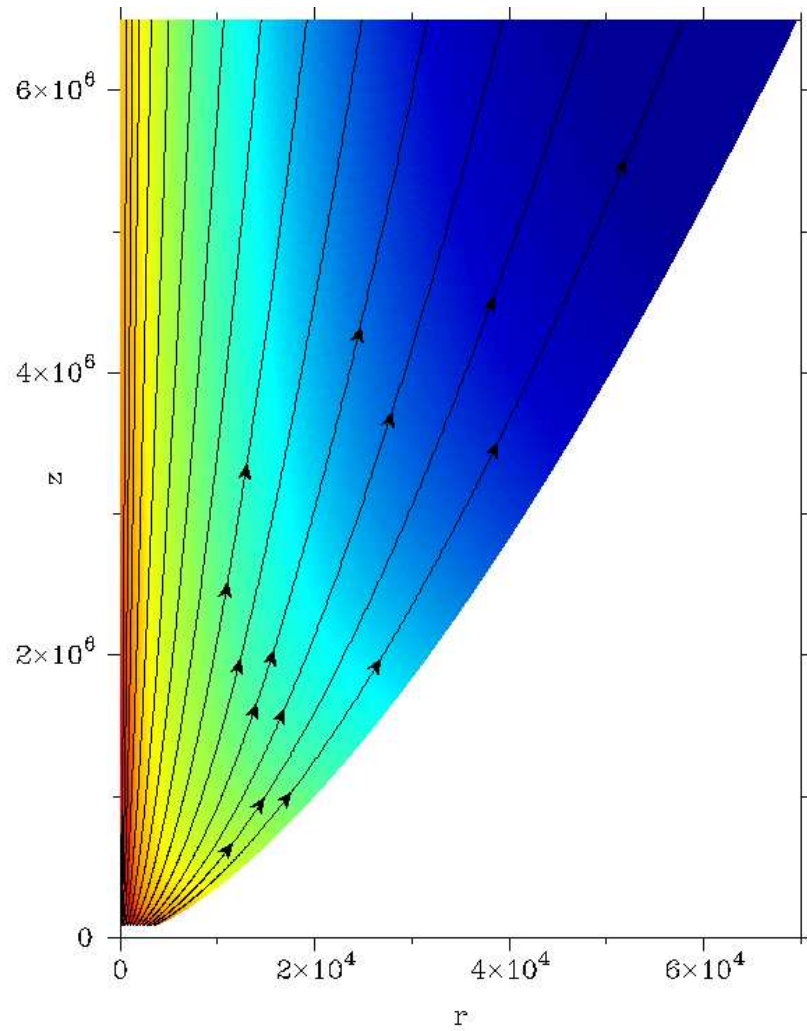
$\mathcal{F} \downarrow$ through stronger collimation of the inner streamlines relative to the outer ones (differential collimation)

☞ external pressure plays important role

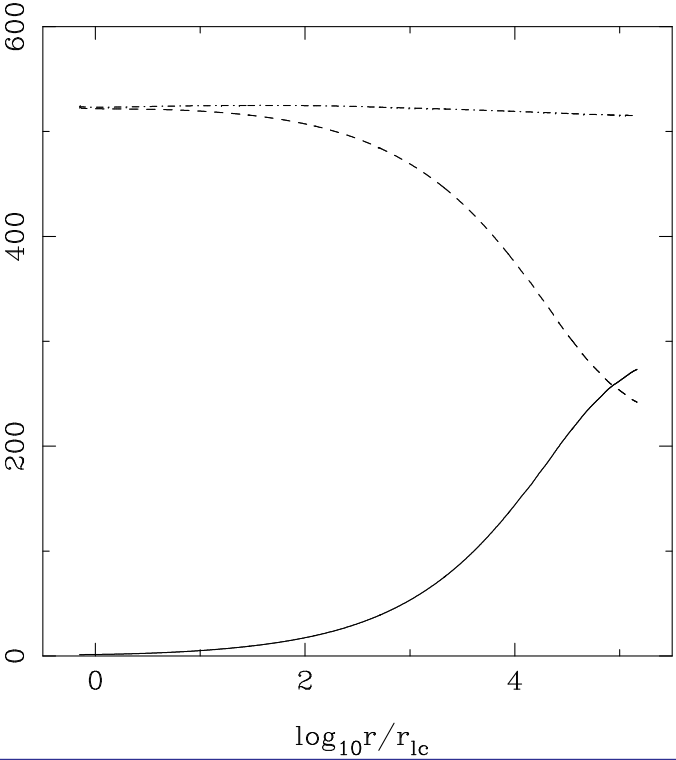
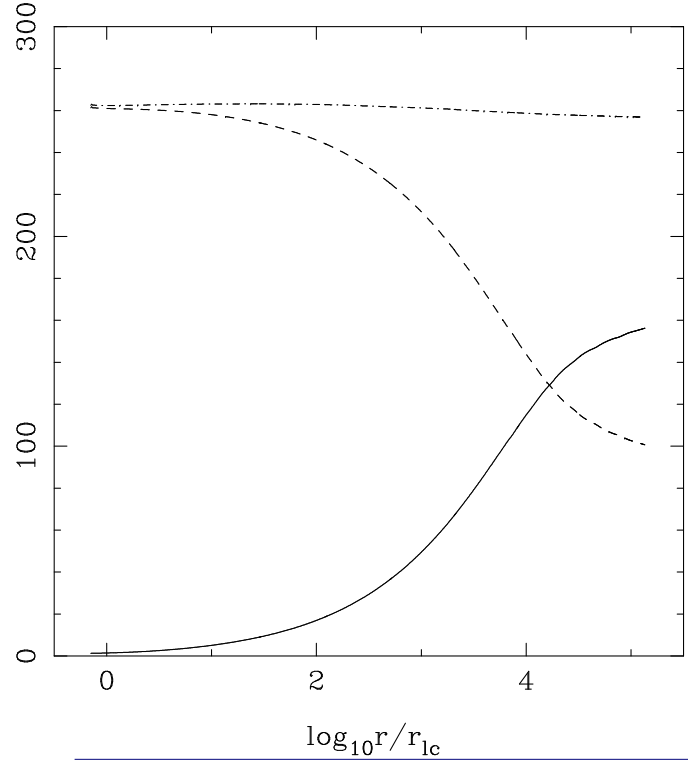
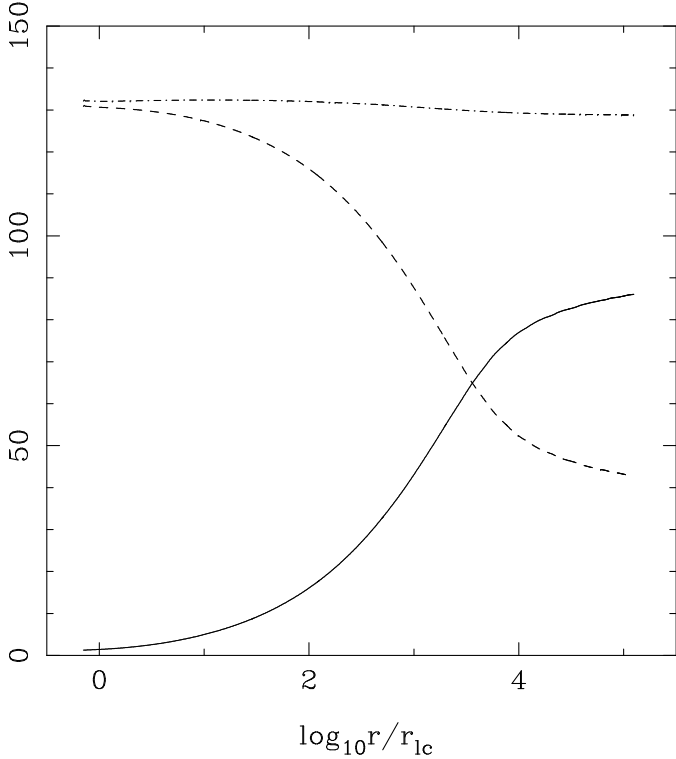
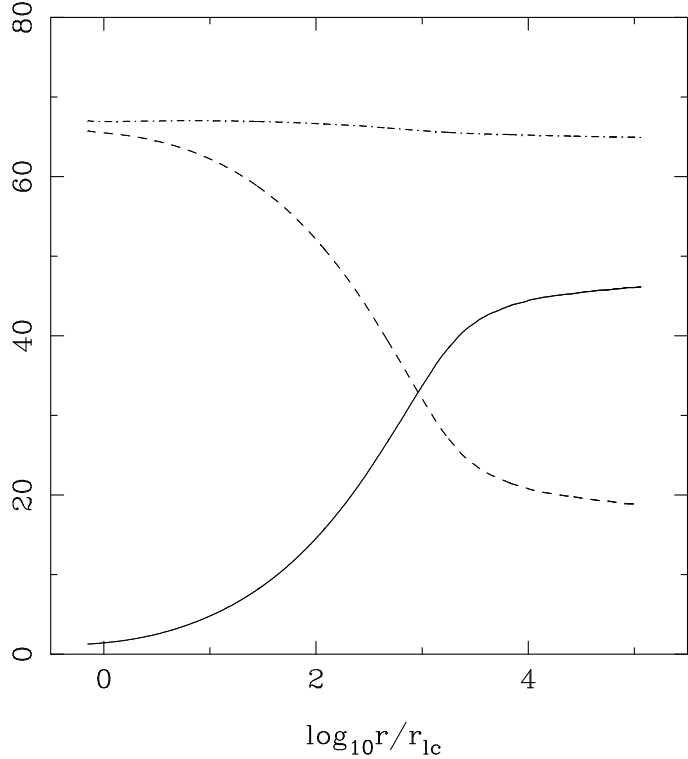
Komissarov, Vlahakis, Königl, & Barkov 2009



left: density/field lines, right: Lorentz factor/current lines (wall shape $z \propto r^{1.5}$)
Differential rotation \rightarrow slow envelope



Uniform rotation $\rightarrow \gamma$ increases with r



energy flux ratios:

$$\gamma = \frac{\text{kinetic}}{\text{rest mass}}$$

$$\gamma\sigma = \frac{\text{Poynting}}{\text{rest mass}}$$

$$(\sigma = \frac{\text{Poynting}}{\text{kinetic}})$$

$$\mu = \gamma + \gamma\sigma$$

γ (increasing),

$\gamma\sigma$ (decreasing),

and μ (constant)

efficiency > 50%

Caveat: $\gamma\vartheta \sim 1$ (for high γ)

- very narrow jets ($\vartheta < 1^\circ$ for $\gamma > 100$) \longrightarrow early breaks or no breaks at all
- this is a result of causality (across jet): outer lines need to know that there is space to expand

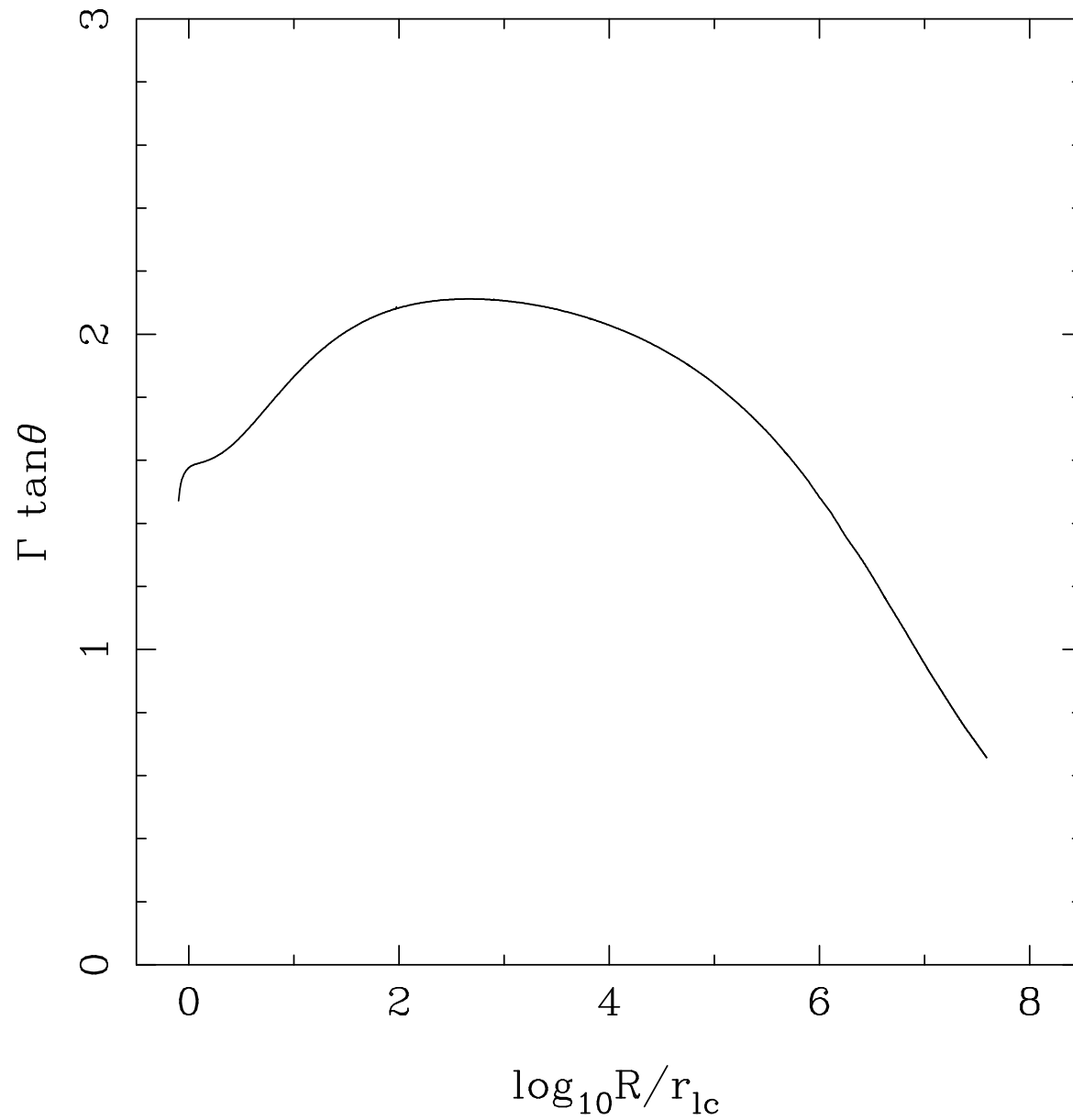
- Mach cone half-opening θ_m should be $> \vartheta$

With $\sin \theta_m = \frac{\gamma_f c_f}{\gamma V_p} \approx \frac{\sigma^{1/2}}{\gamma}$ the requirement for causality yields

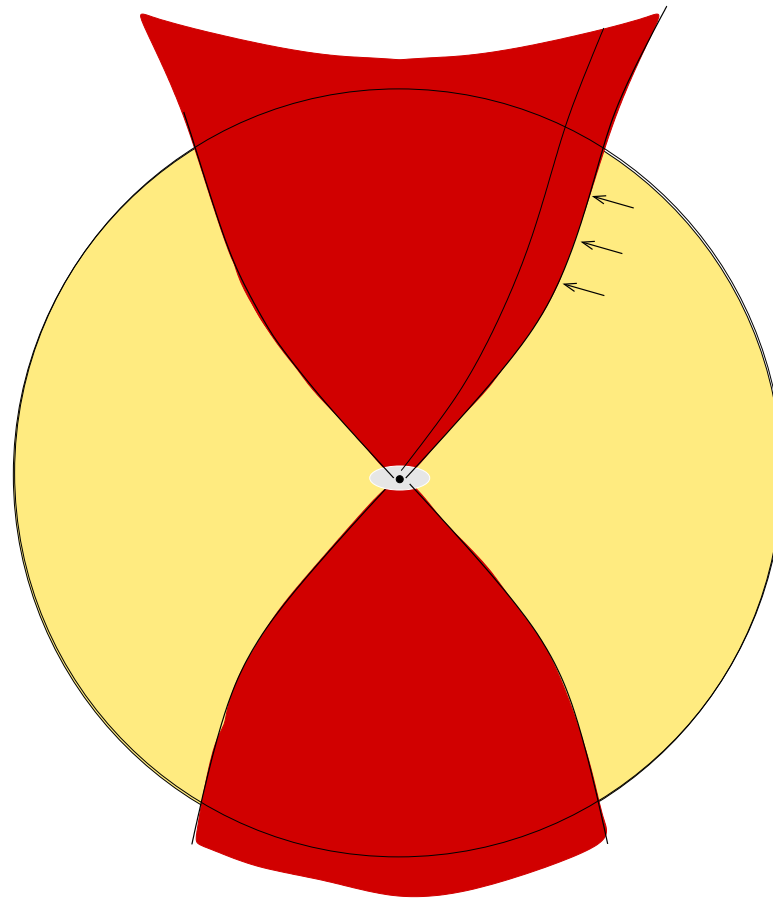
$$\gamma\vartheta < \sigma^{1/2}.$$

For efficient acceleration ($\sigma \sim 1$ or smaller) we always get

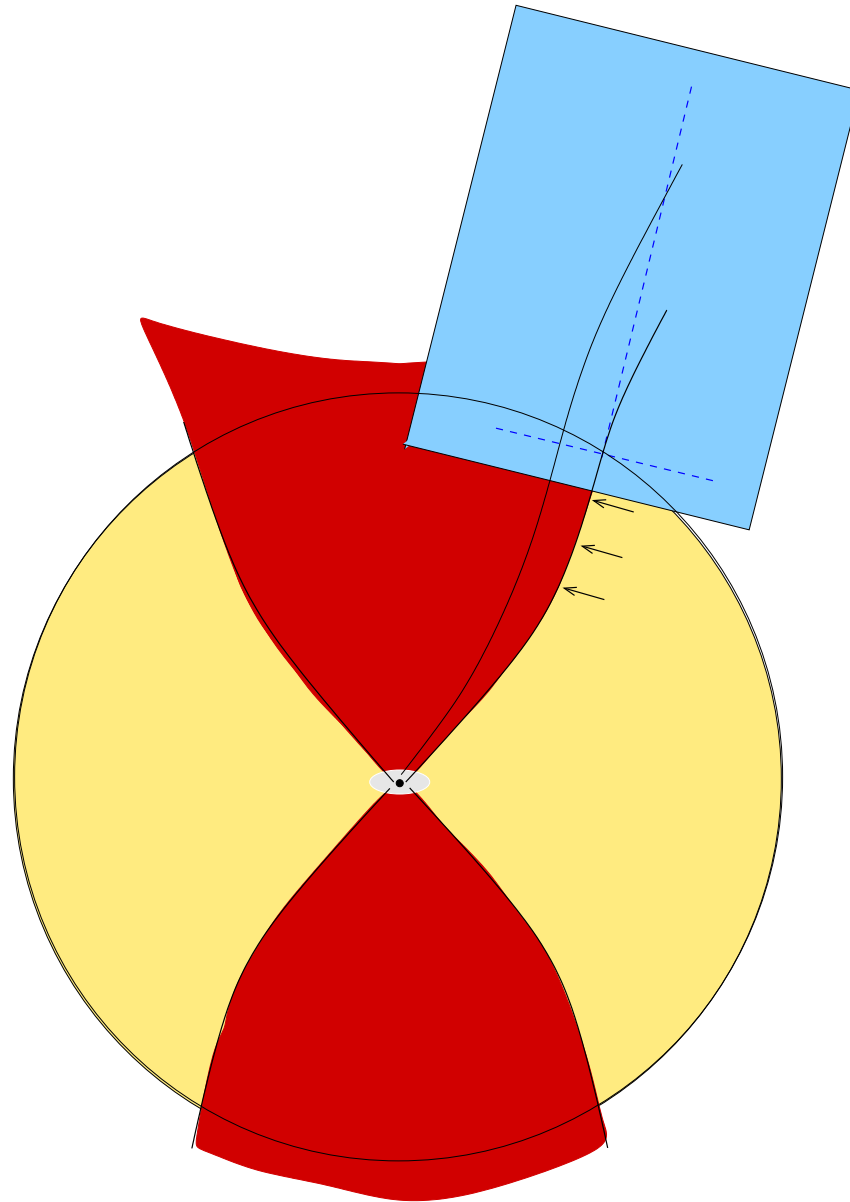
$$\gamma\vartheta \sim 1$$



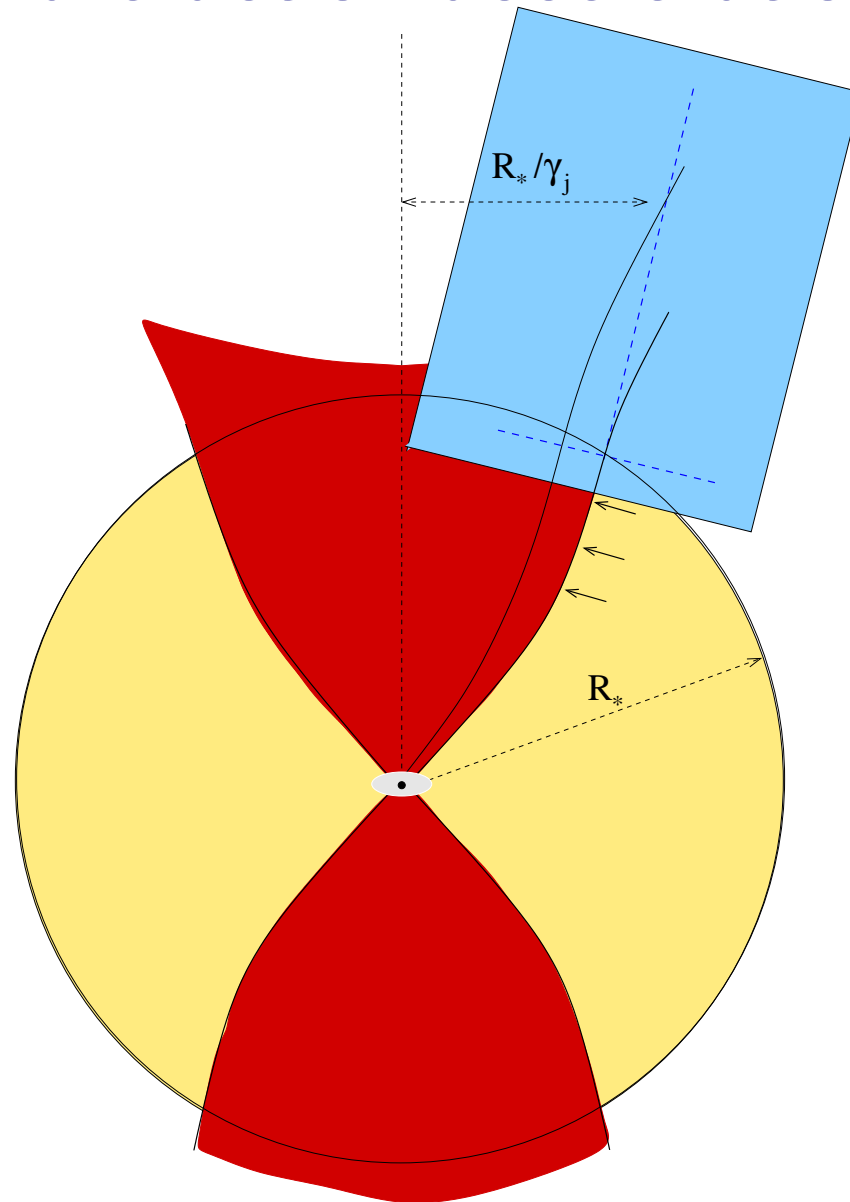
Rarefaction acceleration



Rarefaction acceleration

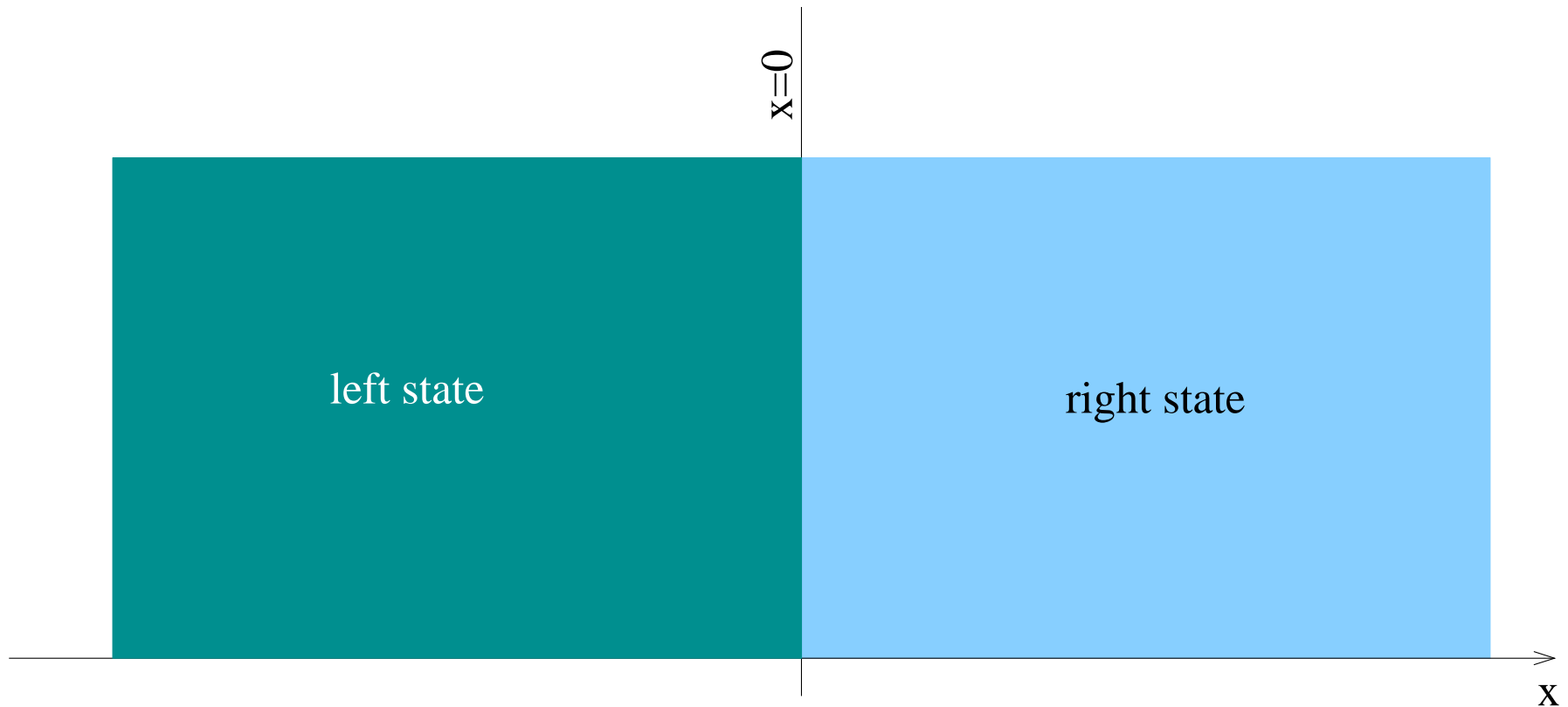


Rarefaction acceleration



Rarefaction simple waves

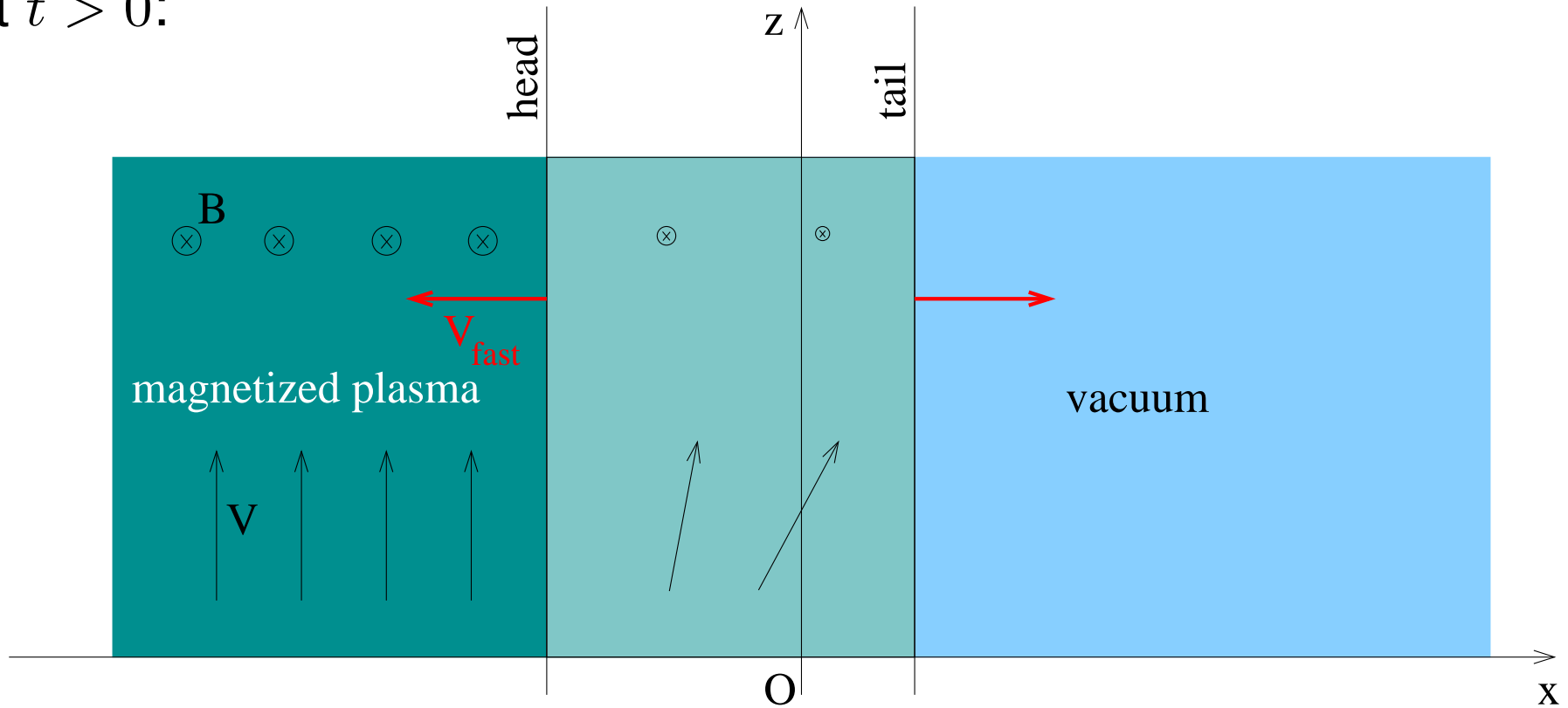
At $t = 0$ two uniform states are in contact:



This Riemann problem allows self-similar solutions that depend only on $\xi = x/t$.

- when right=vacuum, simple rarefaction wave

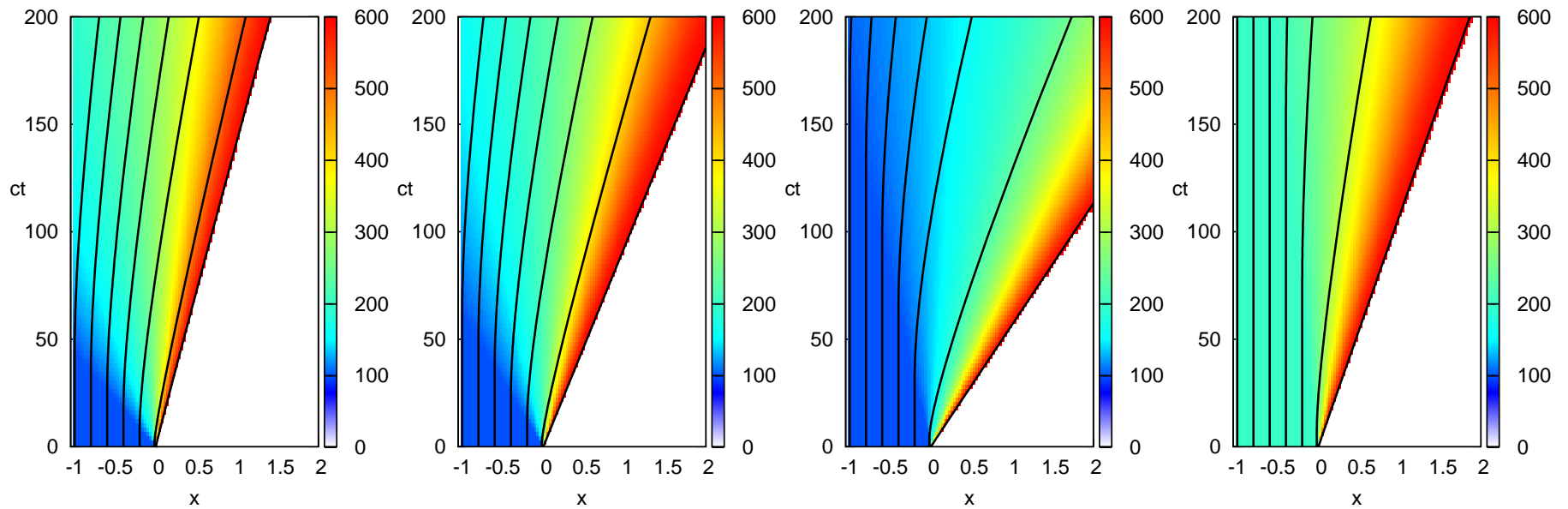
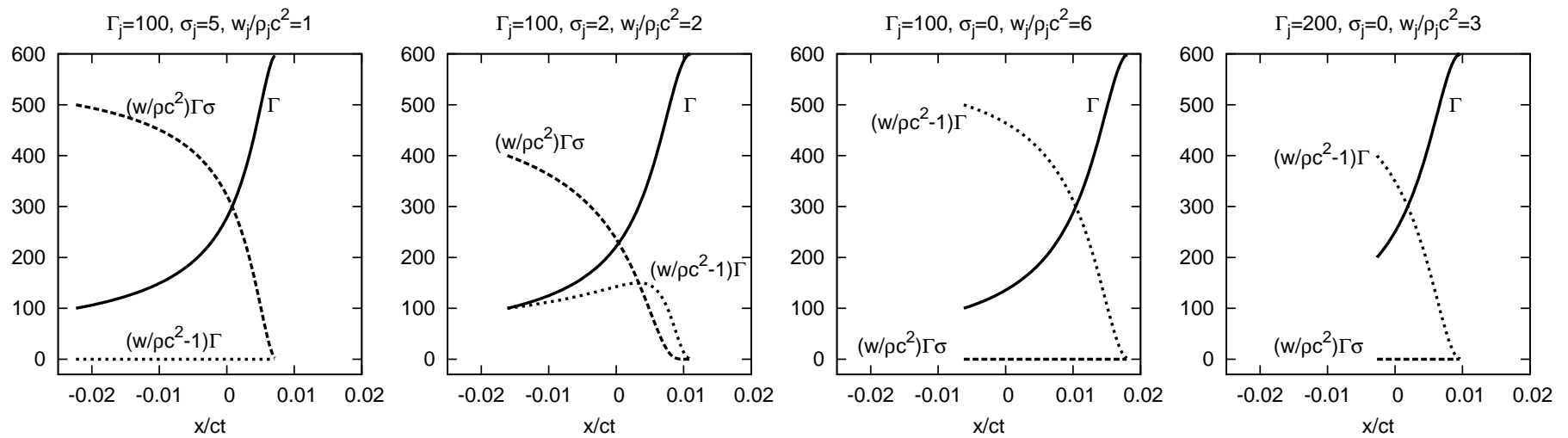
At $t > 0$:



for the cold case the Riemann invariants imply

$$v_x = \frac{1}{\gamma_j} \frac{2\sigma_j^{1/2}}{1 + \sigma_j} \left[1 - \left(\frac{\rho}{\rho_j} \right)^{1/2} \right], \quad \gamma = \frac{\gamma_j (1 + \sigma_j)}{1 + \sigma_j \rho / \rho_j}, \quad \rho = \frac{4\rho_j}{\sigma_j} \sinh^2 \left[\frac{1}{3} \operatorname{arcsinh} \left(\sigma_j^{1/2} - \frac{\mu_j x}{2t} \right) \right]$$

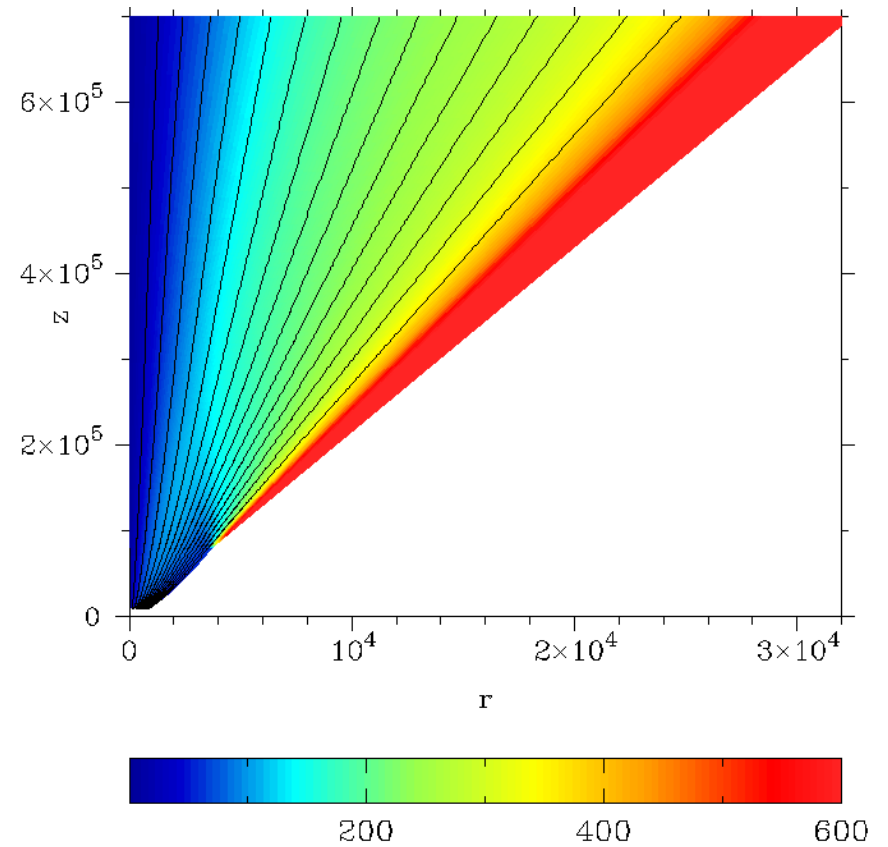
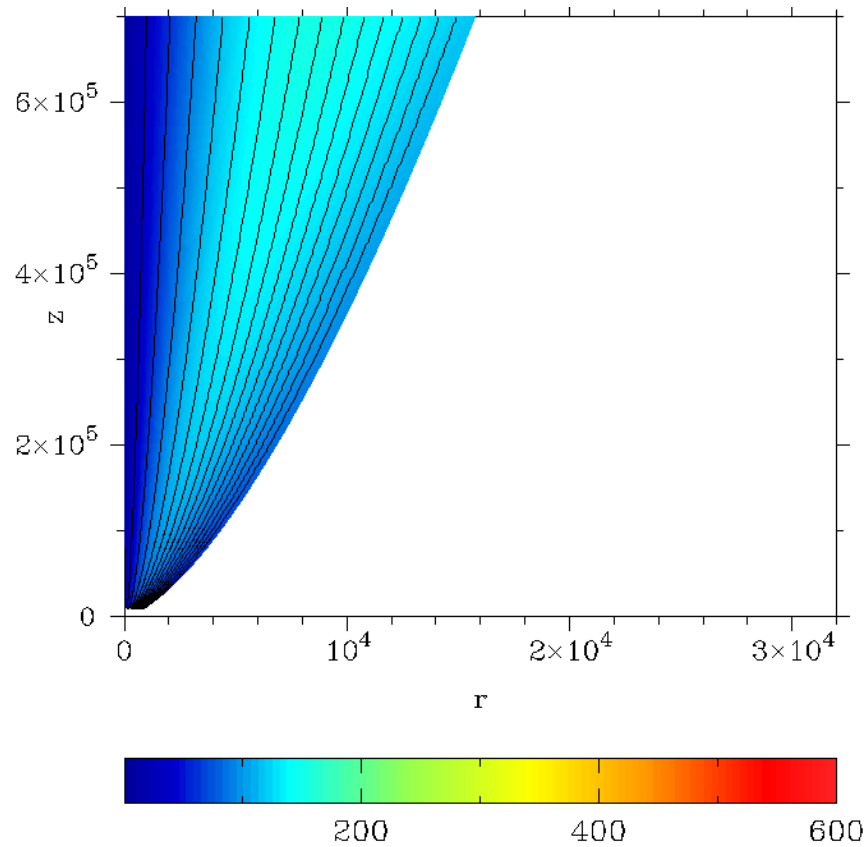
$$V_{head} = -\frac{\sigma_j^{1/2}}{\gamma_j}, \quad V_{tail} = \frac{1}{\gamma_j} \frac{2\sigma_j^{1/2}}{1 + \sigma_j}, \quad \Delta\vartheta = V_{tail} < 1/\gamma_i$$

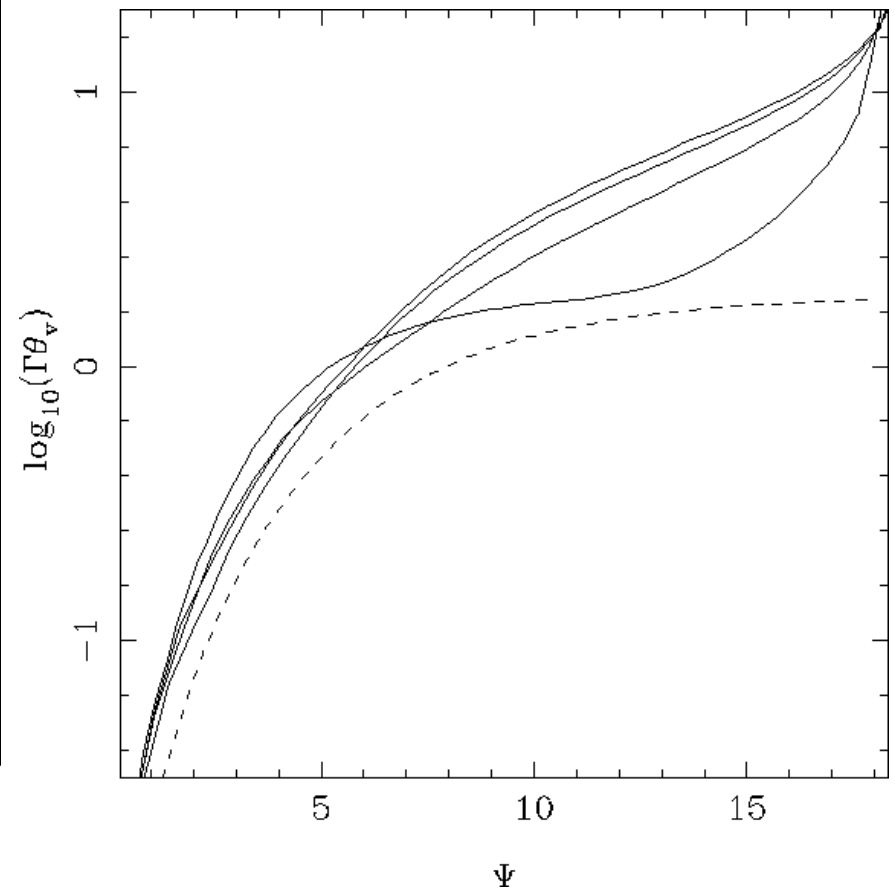
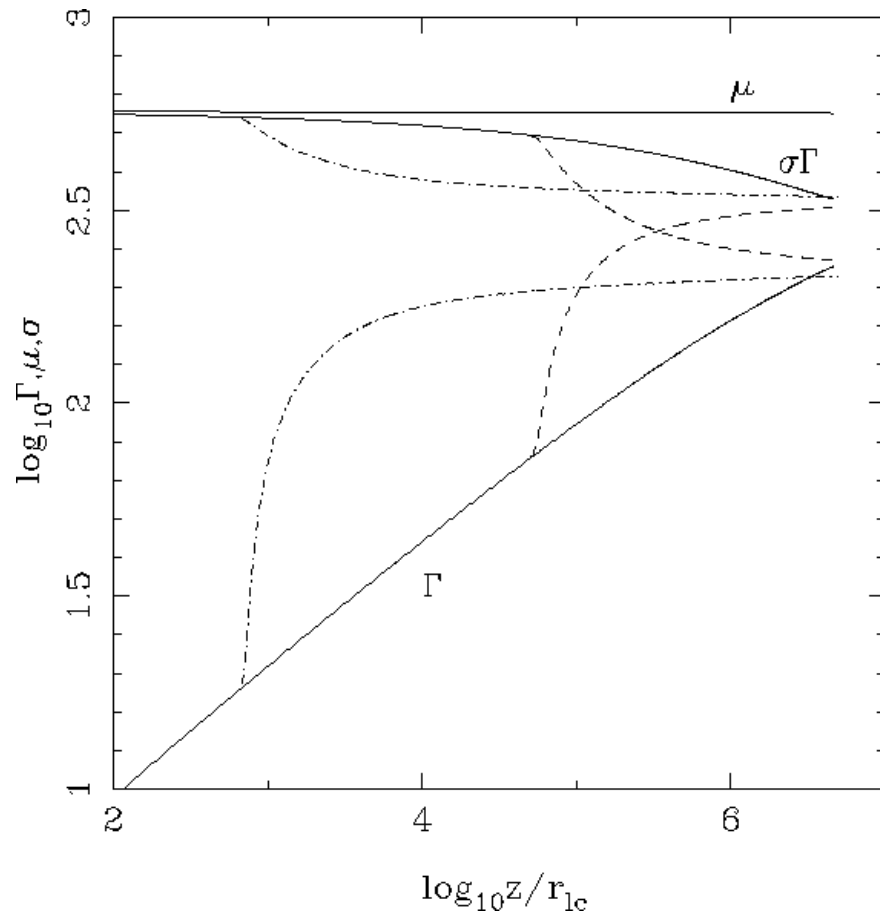


The colour image in the Minkowski diagrams represents the distribution of the Lorentz factor and the contours show the worldlines of fluid parcels initially located at $x_i = -1, -0.8, -0.6, -0.4, -0.2, -0.02, 0$.

Simulation results

Komissarov, Vlahakis & Königl 2010

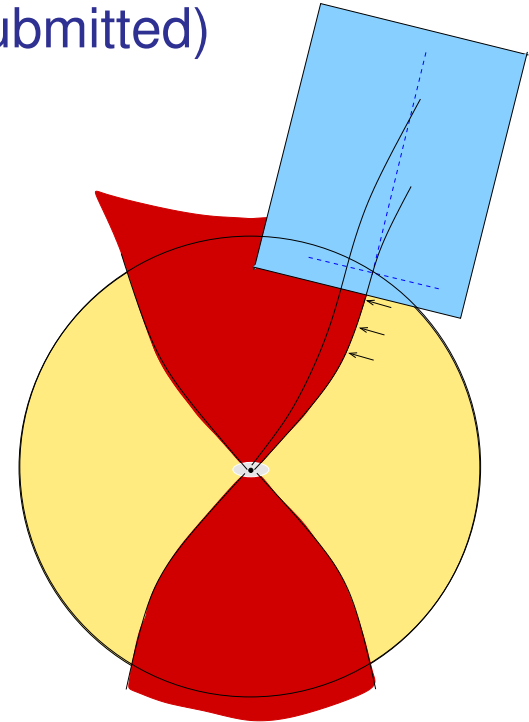


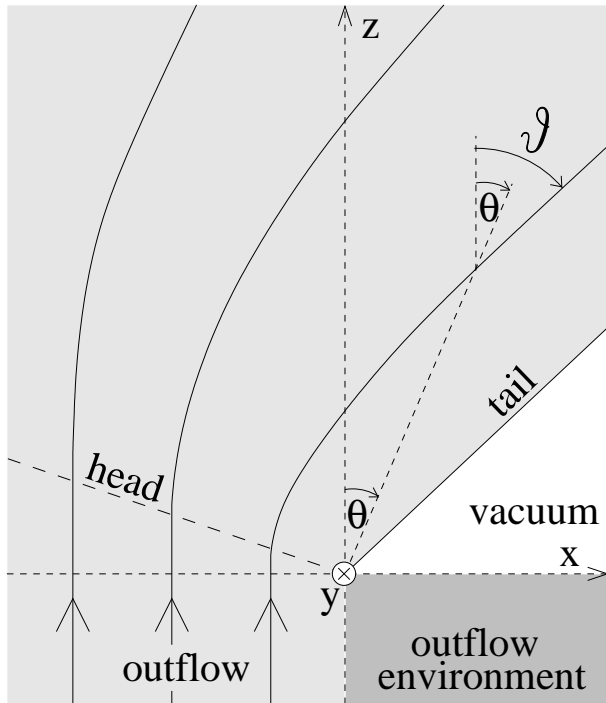


Steady-state rarefaction wave

Sapountzis & Vlahakis (MNRAS submitted)

- “flow around a corner”
- planar geometry
- ignoring B_p (nonzero B_y)
- similarity variable x/z (angle θ)
- generalization of the nonrelativistic, hydrodynamic rarefaction (e.g. Landau & Lifshitz)
- in addition, allow for inhomogeneity in the “left” state



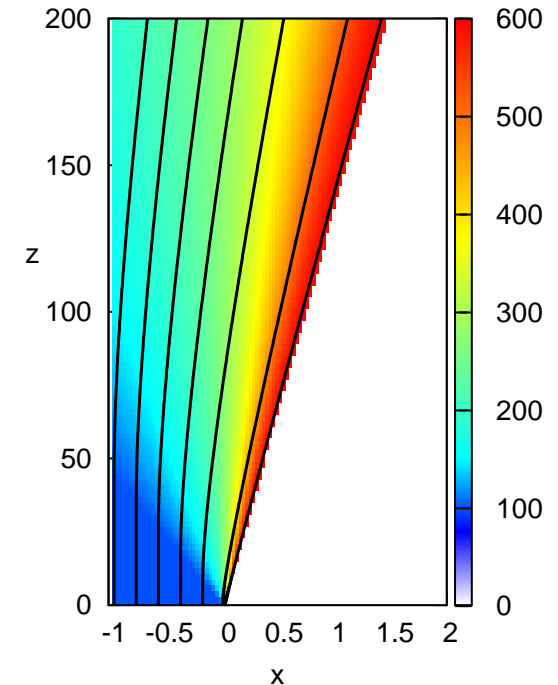
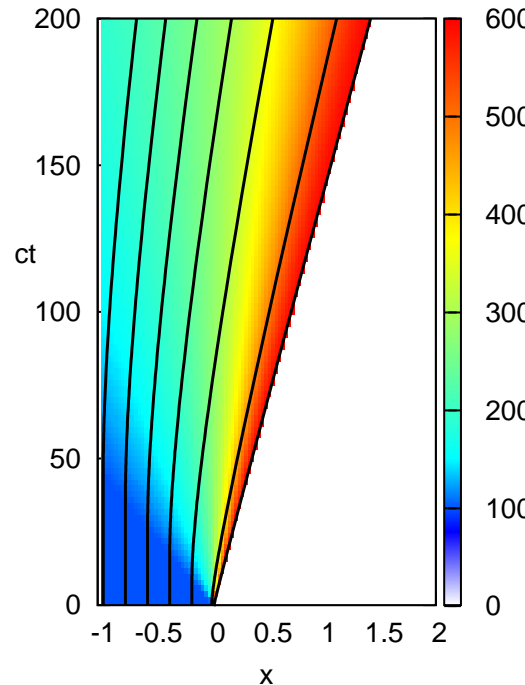
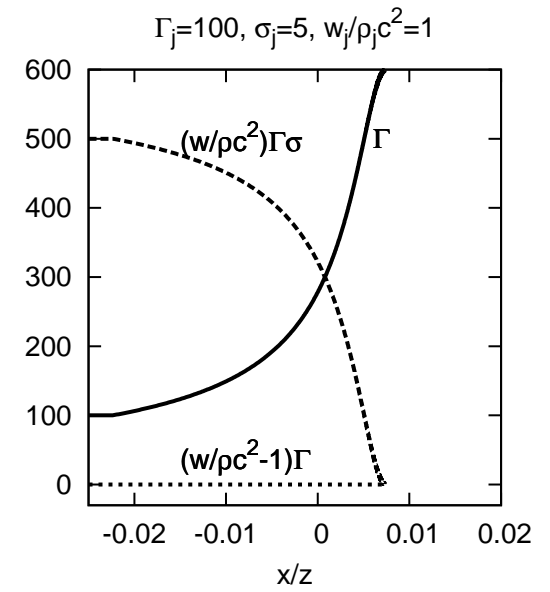
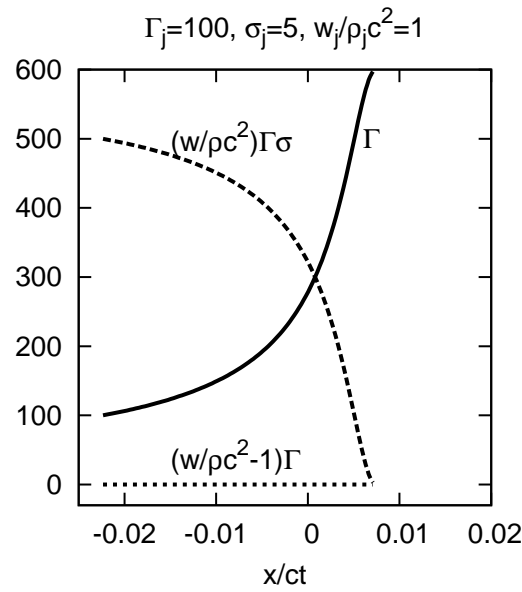


$$\theta_{\text{head}} = -\frac{\sigma_j^{1/2}}{\gamma_j}$$

$$\theta_{\text{tail}} = \frac{2\sigma_j^{1/2}}{\gamma_j(1+\sigma_j)}$$

$$\sigma = (\sigma_j \gamma_j x_i / z)^{2/3}$$

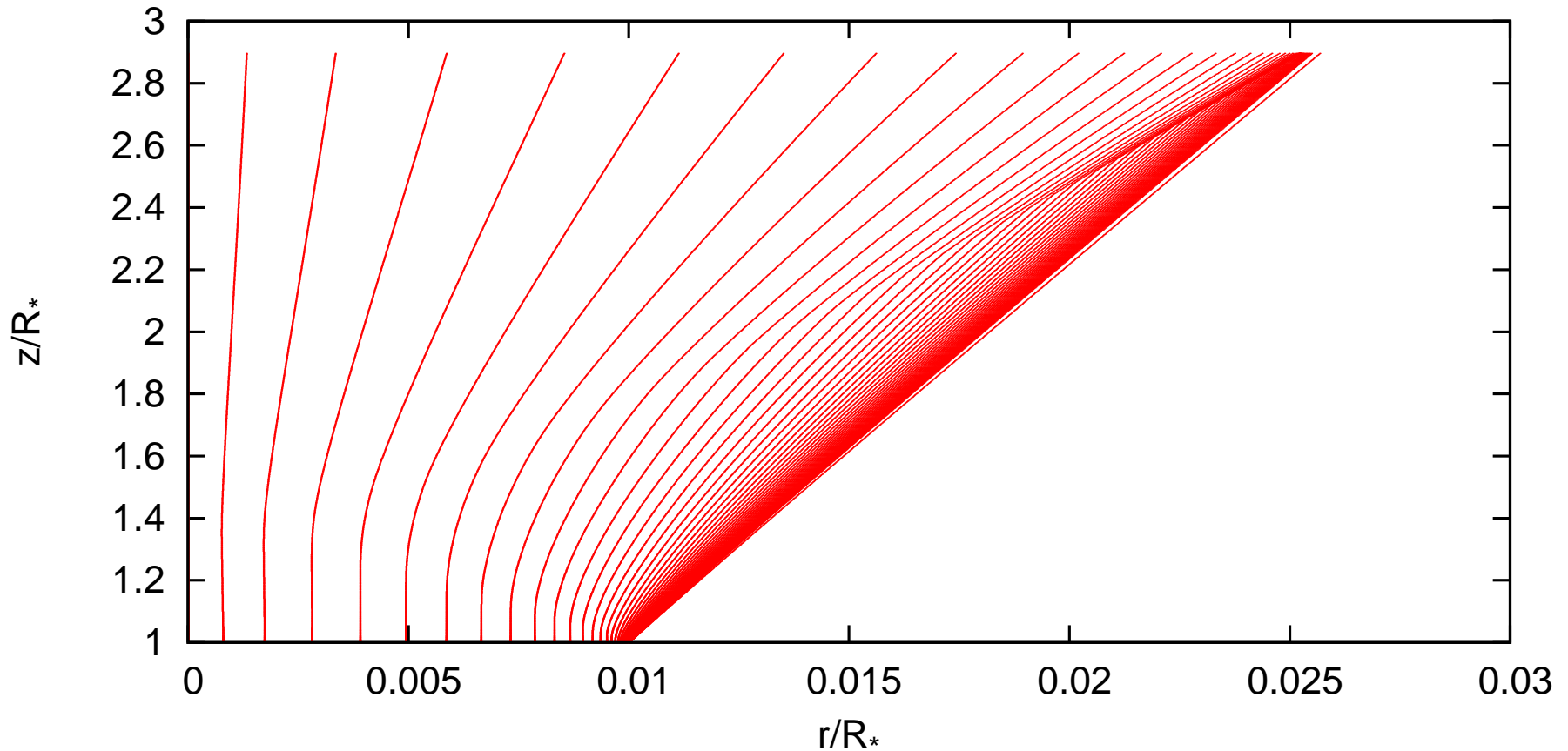
$$\sigma = 1 \text{ at } r = \sigma_j \gamma_j |x_i| = 7 \times 10^{11} \sigma_j \left(\frac{|x_i|}{R_* / \gamma_j} \right) \left(\frac{R_*}{10 R_\odot} \right) \text{ cm}$$



time-dependent (left) and steady-state (right)
rarefaction (similar; $ct \rightarrow z$)
(distance unit = $R_* / \gamma_j \sim 10^{10}$ cm)

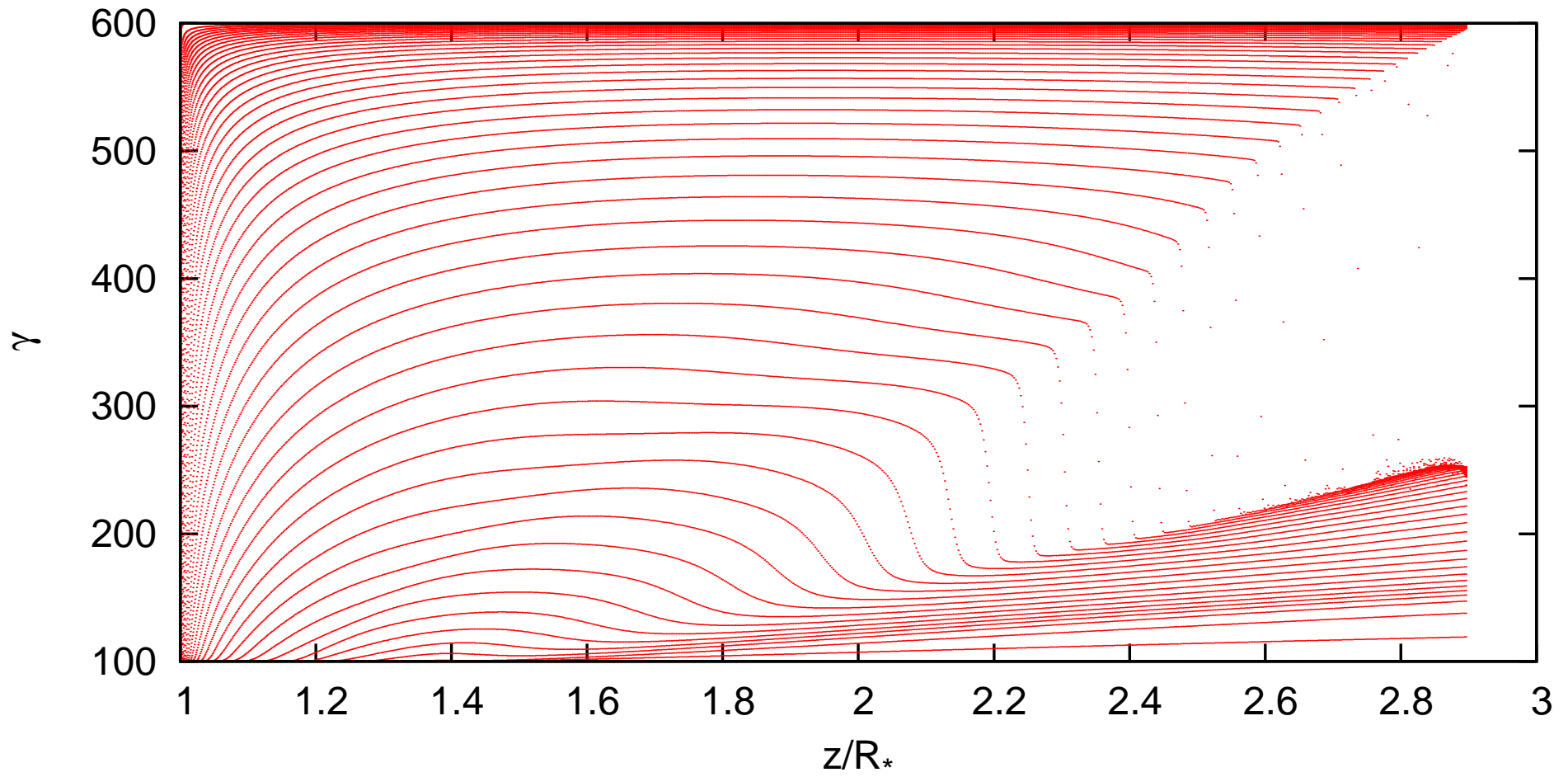
Axisymmetric model

Solve steady-state axisymmetric MHD eqs using the method of characteristics (Sapountzis & Vlahakis in preparation)

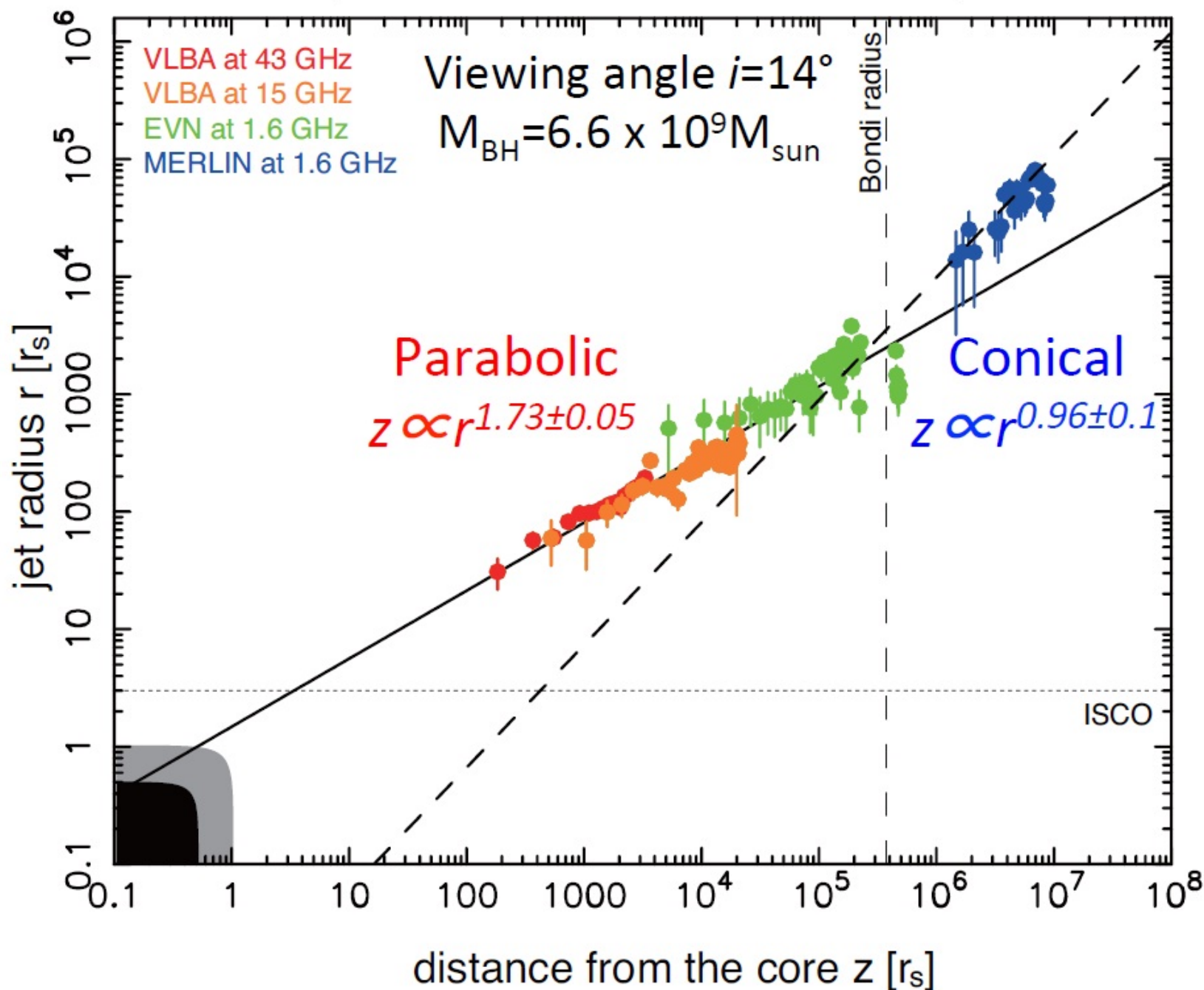


(not in scale!)

typical value of $R_* = 10^{12}$ cm



(Asada & Nakamura 2011)



Summary

- ★ The collimation-acceleration paradigm provides a viable explanation of the dynamics of relativistic jets
- ★ bulk acceleration up to Lorentz factors $\gamma_\infty \gtrsim 0.5 \frac{\mathcal{E}}{Mc^2}$
caveat: in ultrarelativistic GRB jets $\vartheta \sim 1/\gamma$
- ★ Rarefaction acceleration
 - further increases γ
 - makes GRB jets with $\gamma\vartheta \gg 1$
- ★ Future work
 - apply other stratified jet models
 - attention to the shock from reflection on the rotation axis
 - use realistic pressure distributions
 - inside the star (from stellar-evolution models),
 - and outside – shock formation

