

## Production of vacancy-oxygen defect in electron irradiated silicon in the presence of self-interstitial-trapping impurities

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The enhancement by carbon of vacancy-oxygen (VO) defect formation in electron irradiated silicon was investigated using many samples of various carbon contents. The effect of carbon is well described by a simple analytical model of competing trapping of self-interstitials by VO and by carbon (and by emerging carbon-related defects like  $C_iO_i$  and  $IC_iO_i$ ). The trapping ratio by  $C_s$  and by VO was determined to be about 0.9, and the optical calibration coefficients for  $C_iO_i$  and  $IC_iO_i$  were deduced. In crystals containing a high concentration of Ge, germanium also acts as a self-interstitial trapping impurity and, thus, enhances VO production. The trapping efficiency of Ge is 1000 times less than that of carbon. © 2011 American Institute of Physics. [doi:10.1063/1.3657946]

### I. INTRODUCTION

Irradiation-produced vacancies (V) in Czochralski-grown (CZ) silicon are known<sup>1–3</sup> to be quickly trapped by oxygen that is initially present as an electrically inactive interstitial species ( $O_i$ ). The electrical, optical, and electronic properties of the resulting vacancy-oxygen (VO) defect (also called the A-centre) have been studied<sup>2–10</sup> intensively over the years. The defect has an acceptor level at  $E_c - 0.17$  eV. It is optically active, with a local vibration mode (LVM) band at  $830\text{ cm}^{-1}$  for the neutral charge state at room temperature (RT).

Since self-interstitials (I) are simultaneously created in the same amount as V, a production of VO in an appreciable concentration is possible only in the presence of some traps for I—otherwise VO would be almost completely annihilated by the  $I + VO$  reaction. The carbon impurity (initially in an electrically inactive substitutional state  $C_s$ ) is well known<sup>11–16</sup> as an efficient trap for I. The emerging interstitial carbon atoms ( $C_i$ ) are trapped by oxygen and carbon producing  $C_iO_i$  and  $C_iC_s$  defects that further trap self-interstitials. In lightly doped material, carbon is most likely the major trap for I, and hence, the concentration of VO is expected to be controlled by the carbon concentration  $[C_s]$  (square brackets are used to denote the concentration of a species). Indeed, it was noted<sup>17</sup> that, at sufficiently high irradiation dose,  $[VO]$  is higher in a sample of a higher  $[C_s]$ . The goal of the present work is to analyze the carbon effect quantitatively, using a database of many samples of different  $[C_s]$ .

Another impurity that apparently enhances VO production is germanium.<sup>18</sup> An additional goal of the present work is to separate the contributions of Ge and C into self-interstitial trapping.

### II. EXPERIMENTAL DETAILS

The Cz-Si samples used in this study were about 2 mm thick. The oxygen concentration was deduced from the intensity of the  $1107\text{ cm}^{-1}$  band (with a calibration coefficient of  $2.45 \times 10^{17}\text{ cm}^{-2}$ ) and the carbon concentration from the  $605\text{ cm}^{-1}$  band (with a calibration coefficient of  $1 \times 10^{17}\text{ cm}^{-2}$ ). These concentrations—before irradiation—are listed in the third and fourth columns of Table I; the measured substitutional carbon concentration is identical to the total carbon content and denoted  $[C]$ . Due to irradiation, the concentration of substitutional carbon is significantly reduced; this value—denoted  $[C_s]$ —is shown in the fifth column. For oxygen, a reduction is relatively weak and not indicated. The samples Ge1 and Ge4 are doped with Ge ( $1 \times 10^{17}$  and  $4 \times 10^{18}\text{ cm}^{-3}$ , respectively). The effect of the Ge impurity as a trap for self-interstitials is discussed below; it is significant only at  $[Ge] > 3 \times 10^{19}\text{ cm}^{-3}$ . The sample Sn3.1 contains  $3 \times 10^{17}\text{ cm}^{-3}$  of tin—an impurity that is known<sup>19</sup> to compete with  $O_i$  in trapping V. Since  $[Sn] < [O_i]$  in this sample, vacancy trapping is still mostly by oxygen although some reduction in  $[VO]$  may occur. This sample was included into the database, because it is the only available sample with a carbon content intermediate between high and medium. All samples were boron-doped ( $[B] \leq 2.5 \times 10^{15}\text{ cm}^{-3}$ ) with the exception of the Sn-containing sample which was lightly doped with phosphorus ( $[P] = 6 \times 10^{13}\text{ cm}^{-3}$ ).

The samples were irradiated with 2 MeV electrons, using the Dynamitron accelerator at Takasaki-JAERI (Japan). The temperature of irradiation was about  $70^\circ\text{C}$ . The samples are divided into three groups of irradiation dose. The first group, of four samples, was irradiated at a dose  $\phi = 5 \times 10^{17}\text{ cm}^{-2}$ , the second group, of three samples—at  $\phi = 10^{18}\text{ cm}^{-2}$ , and the third group, of two samples—at  $2 \times 10^{18}\text{ cm}^{-2}$ . The IR spectra were recorded at RT, with an

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TABLE I. Characteristics of electron-irradiated samples. The concentrations  $[O_i]$  of oxygen and  $[C]$  of carbon are measured before irradiation. The other columns refer to the post-irradiation state.

Sample	Dose ( $10^{18} \text{ cm}^{-2}$ )	$[O_i]$ ( $10^{17} \text{ cm}^{-3}$ )	$[C]$ ( $10^{16} \text{ cm}^{-3}$ )	$[C_s]$ ( $10^{16} \text{ cm}^{-3}$ )	$[VO]$ ( $10^{16} \text{ cm}^{-3}$ )	$A_{862}$ ( $\text{cm}^{-1}$ )	$A_{1020}$ ( $\text{cm}^{-1}$ )
Ge1	0.5	7.5	2	1.5	3.4	0.14	0.07
Ge4	0.5	4.3	10	4.9	3.6	0.26	0.08
E3	0.5	8	16	9.6	3.9	0.34	0.06
E1	0.5	5.3	75	60	4.8	0.38	0.03
M4	1	7.4	5	1	5.9	0.28	0.07
H3	1	7.3	22	13.2	6.2	0.53	0.12
Sn3.1	1	7.5	47	18	7.3	0.63	0.13
M7	2	8.2	4	2.3	7.2	0.09	0.09
M5	2	7.4	8.8	3.9	9.8	0.46	0.24

FTIR spectrometer of  $1 \text{ cm}^{-1}$  resolution. The two phonon intrinsic absorption was always subtracted by using a float-zone sample of the same thickness.

### III. EXPERIMENTAL RESULTS AND DISCUSSION

Fig. 1 shows RT absorption spectra of irradiated samples, in the wavenumber range of  $530\text{--}1060 \text{ cm}^{-1}$ , for three representative carbon concentrations: high, medium, and low (samples E1, E3, and M7 of Table I). The most pronounced irradiation-induced bands are those of VO and  $C_iO_i$ . There are also weaker bands due to  $IC_iO_i$ —a defect formed by  $I + C_iO_i$  reaction. A band due to the di-carbon defect  $C_iC_s$  is very weak and near the detection limit. The bands due to  $C_i$  are not seen at all—since at the irradiation temperature of  $70^\circ\text{C}$  the produced  $C_i$  are immediately trapped, mostly by  $O_i$ . By comparing the samples E1 and E3 (of the same dose), it appears that the VO band is stronger at higher  $[C_s]$ . The sample M7 in Fig. 1 has received the highest dose, and the VO band is strong, in spite of a low  $[C_s]$ .

The VO concentration listed in Table I was calculated using a calibration coefficient<sup>20</sup> of  $6.25 \times 10^{16} \text{ cm}^{-2}$  for the  $830 \text{ cm}^{-1}$  band at RT. This calibration was coupled<sup>20</sup> to the oxygen calibration assumed in that work which was the same as that adopted above. Were the oxygen calibration to be changed (for instance, to a frequently used value of  $3.14 \times 10^{17} \text{ cm}^{-2}$ ), then the VO calibration coefficient would be increased proportionally to  $8 \times 10^{16} \text{ cm}^{-2}$ . The two last columns of Table I show the intensity of larger bands due to the  $C_i$ -related defects:  $C_iO_i$  (at  $862 \text{ cm}^{-1}$ ) and  $IC_iO_i$  (at  $1020 \text{ cm}^{-1}$ ).

#### A. Analytical model of VO production in the presence of carbon traps for self-interstitials

The accumulation of VO and of accompanying carbon defects  $C_iO_i$ ,  $C_iC_s$  and subsequently formed clusters (such as  $IC_iO_i$  and larger ones) in dependence of the irradiation dose was numerically simulated<sup>11,17,21–23</sup> assuming many trapping reactions for V and I and thus using a large number of fitting parameters. This problem can be, however, solved analytically, with several reasonable simplifications:

- neglecting the di-carbon defect  $C_iC_s$  (as mentioned above, the band due to  $C_iC_s$  is always weaker than those of carbon and of carbon-oxygen species).
- assuming the same kinetic coefficient for trapping of I by all the carbon-related traps  $C_s$ ,  $C_iO_i$ ,  $IC_iO_i$ , etc.
- neglecting production of divacancies  $V_2$ —justified by a relatively low ratio<sup>24</sup> of the production rates of  $V_2$  and V by 2 MeV electron irradiation.

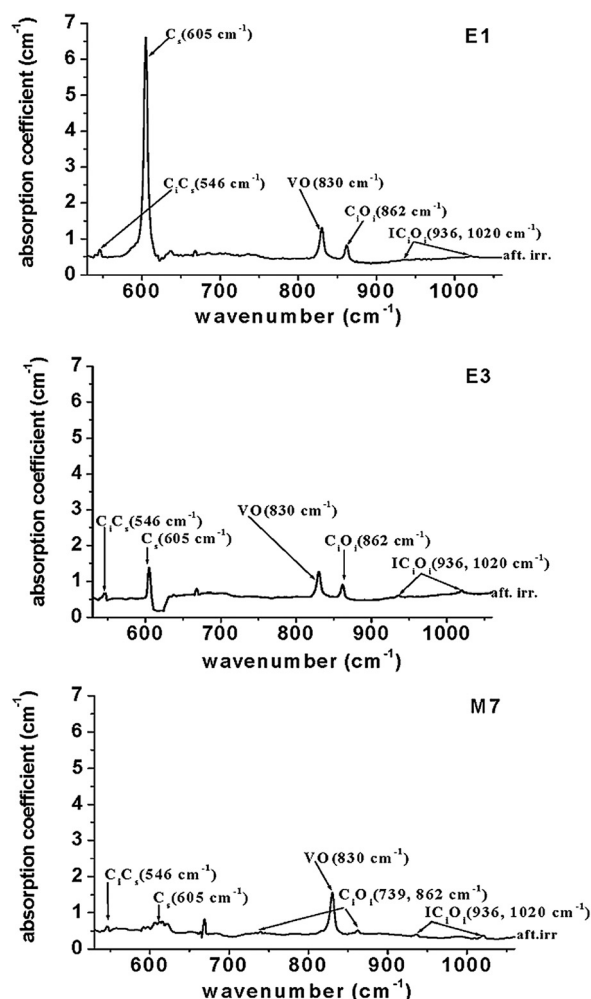


FIG. 1. Fragments of absorption spectra after electron irradiation for samples of three representative carbon concentrations: high, medium, and low (samples E1, E3, and M7 of Table I, respectively).

The production rate  $G$  of vacancies (the number of isolated vacancies produced per unit time and volume) is proportional to the dose rate  $d\phi/dt$

$$G = \eta d\phi/dt. \quad (1)$$

The generation coefficient  $\eta$  is a fundamental parameter of irradiation, and yet, there is a large scatter of reported values. We accept  $\eta = 0.09 \text{ cm}^{-1}$ . This value gives the best fit to the data processed below. Were the calibration for VO changed as mentioned above, the best-fit value of  $\eta$  would change proportionally, to  $0.12 \text{ cm}^{-1}$ . Both values of  $\eta$  are consistent with the results of early work<sup>24</sup> based on an electron paramagnetic resonance study of VO at low dose.

The vacancies are immediately trapped by oxygen, and accordingly, the production rate of VO is identical to  $G$ . The VO defects, when produced, trap self-interstitials leading to a reduction in [VO]. The overall time derivative is

$$d[\text{VO}]/dt = G - \beta_{\text{vo}}[\text{I}][\text{VO}], \quad (2)$$

where  $\beta_{\text{vo}}$  is the kinetic coefficient for the I + VO annihilation reaction. The self-interstitial concentration [I] corresponds to a balance of the production (at a rate identical to  $G$ ) and of the loss controlled by all the relevant traps: by VO—at a rate of  $\beta_{\text{vo}}$  [I] [VO]—and by the carbon-containing species  $\text{C}_s$ ,  $\text{C}_i\text{O}_i$ ,  $\text{IC}_i\text{O}_i$  etc—at a rate of  $\beta_c$  [I] [C]. Here, [C] is the total concentration of these species—identical to the initial concentration of  $\text{C}_s$ —and  $\beta_c$  is the kinetic coefficient for the trapping reaction. The concentration [I] is then expressed as

$$[\text{I}] = G/(\beta_c[\text{C}] + \beta_{\text{vo}}[\text{VO}]). \quad (3)$$

With this expression, the kinetic Equation (2) for the accumulation of VO defects takes the form

$$d[\text{VO}]/dt = G\beta_c[\text{C}]/(\beta_c[\text{C}] + \beta_{\text{vo}}[\text{VO}]). \quad (4)$$

The time derivative is expressed as  $(G/\eta) d[\text{VO}]/d\phi$ , taking into account Eq. (1). Then, Eq. (4) is integrated and gives [VO] in dependence of the dose  $\phi$  and the carbon concentration [C]

$$[\text{VO}]^2 + 2q_c[\text{VO}][\text{C}] = 2\eta q_c\phi[\text{C}], \quad (5)$$

where  $q_c$  is the ratio of the two trapping coefficients:  $q_c = \beta_c/\beta_{\text{vo}}$ . By Eq. (5), the normalized concentration  $[\text{VO}]/[\text{C}]$  is a function of  $\phi/[\text{C}]$ , and this rule is well obeyed by the samples of Table I (Fig. 2). The two last points, showing some deviation, are less reliable since they refer to the lowest [C]. The solid line in Fig. 2 is the solution of the quadratic Equation (5)

$$[\text{VO}]/[\text{C}] = -q_c + (q_c^2 + 2q_c\eta\phi/[\text{C}])^{1/2}, \quad (6)$$

with the best-fit parameters:  $\eta = 0.09 \text{ cm}^{-1}$  and  $q_c = 0.9$ . If  $\phi/[\text{C}] \ll q_c/(2\eta)$ , then  $[\text{VO}] = \eta\phi$ ; in this case, V and I are trapped independent of each other: vacancies—by oxygen, self-interstitials—by carbon. At  $\phi/[\text{C}] \gg q_c/(2\eta)$ , [VO] is

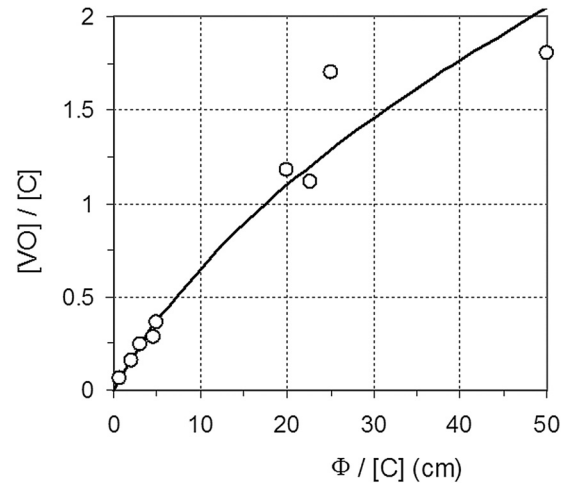


FIG. 2. Concentration ratio [VO]/[C] plotted in dependence of a normalized dose,  $\phi/[\text{C}]$ , for samples of Table I. The solid curve is the analytical solution, Eq. (6), with the best-fit parameters.

proportional to the square root of the dose and to the square root of [C].

Equation (6) allows to plot [VO] in dependence of [C], for a specified dose; in Fig. 3(a), these curves are computed for the actually used 3 doses which allows for comparison with the experimental points shown by symbols and lying reasonably close to the predicted curves. One can plot the same computed values of [VO] in dependence of the dose, for any specified carbon content, but this presentation is less convenient than Fig. 3(a) for comparison with experiment—due to many values of [C] in our sample set. To get a general idea of the dose dependence of [VO] (Fig. 3(b)), some arbitrary representative values of [C] were used.

## B. Carbon loss during generation of VO

The present model also predicts a variation in the concentration of the substitutional carbon component,  $[\text{C}_s]$ —at least for samples of not too high [C], when the irradiation-produced  $\text{C}_i$  species are trapped mostly by  $\text{O}_i$  and not by  $\text{C}_s$ . The loss rate of  $\text{C}_s$  is then identical to the trapping rate of self-interstitials by substitutional carbon and equals  $\beta_c$  [I]  $[\text{C}_s]$  where [I] is specified by Eq. (3). Making use of Eq. (4) for [VO], one obtains  $d[\text{C}_s]/d[\text{VO}] = -[\text{C}_s]/[\text{C}]$ . Then,  $[\text{C}_s]$  is expressed through [VO], without using any fitting parameters,

$$[\text{C}_s] = [\text{C}]\exp(-[\text{VO}]/[\text{C}]). \quad (7)$$

The remaining fraction of substitutional carbon,  $[\text{C}_s]/[\text{C}]$ , is equal to  $\exp(-X)$ , with  $X = [\text{VO}]/[\text{C}]$ . This rule is, however, not well obeyed by the samples of Table I (Fig. 4), even if only the samples of moderate carbon concentration—E3, H3, Ge4, and M5 shown by circles—are taken into account (for low-carbon samples, the remaining concentration  $[\text{C}_s]$  is too low to be determined reliably).

The two carbon-rich samples (the rhombs in Fig. 4) show still larger deviation. In this case, the expected carbon loss,  $[\text{C}] - [\text{C}_s]$ , is close to [VO] by Eq. (7), but the actual

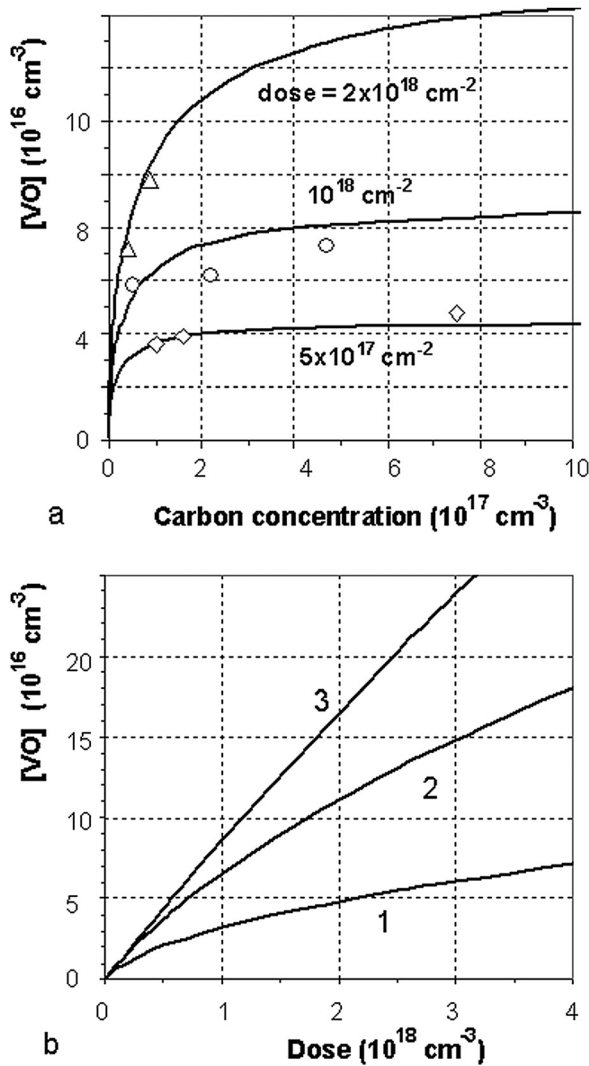


FIG. 3. The calculated concentration of the VO defect. a: in dependence of the carbon content, for three values of the dose  $\phi$ ; the symbols represent samples of Table I (rhombs:  $\phi = 5 \times 10^{17}$ , circles:  $\phi = 10^{18}$ , triangles:  $2 \times 10^{18} \text{ cm}^{-2}$ ). b: in dependence of the dose, for three representative carbon concentrations:  $10^{16}$ ,  $10^{17}$ ,  $10^{18}$  (curves 1 to 3, respectively).

loss is significantly larger, probably due to a contribution of  $C_i C_s$ .

### C. Concentrations of $C_i O_i$ , $IC_i O_i$ , and larger interstitial clusters $I_n C_i O_i$

It is also possible to calculate the concentration of  $C_i O_i$  (and of subsequently formed  $I_n C_i O_i$  clusters)—if  $C_i$  is trapped mostly by  $O_i$  and not by  $C_s$ . The production rate of  $C_i O_i$  is equal to the loss rate of substitutional carbon,  $\beta_c [I] [C_s]$ . On the other hand, the  $C_i O_i$  species are lost by trapping self-interstitials at a rate  $\beta_c [I] [C_i O_i]$ . The overall kinetic equation,  $d[C_i O_i]/dt = \beta_c [I] ([C_s] - [C_i O_i])$ , together with Eq. (4), specifies  $[C_i O_i]$  as a function of  $[VO]$

$$d[C_i O_i]/d[VO] = ([C_s] - [C_i O_i])/[C]. \quad (8)$$

With new variables  $X = [VO]/[C]$  and  $Y_0 = [C_i O_i]/[C]$  and with the carbon concentration  $[C_s]$  substituted from Eq. (7), the kinetic equation for  $[C_i O_i]$  becomes

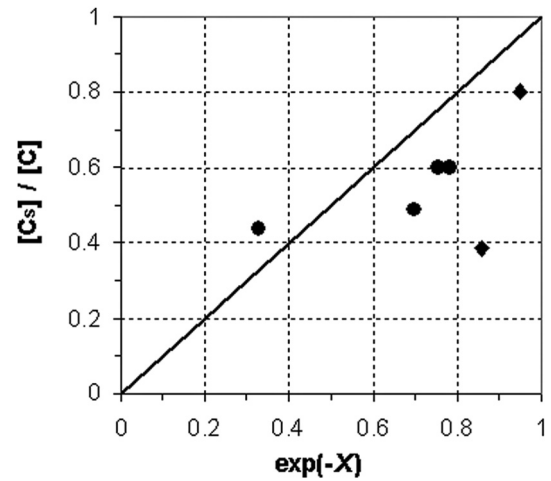


FIG. 4. The remaining fraction of substitutional carbon,  $[C_s]/[C]$ , expected to be equal to  $\exp(-X)$ , where  $X = [VO]/[C]$ . The samples of medium carbon content (E3, H3, Ge4, and M5) are shown by circles and the carbon-rich ones (E1 and Sn3.1) by rhombs.

$$dY_0/dX = \exp(-X) - Y_0. \quad (9)$$

The solution is  $Y_0 = X \exp(-X)$ .

For the next cluster,  $IC_i O_i$ , the source species is  $C_i O_i$  instead of  $C_s$ , and the variable  $Y_1 = [IC_i O_i]/[C]$  obeys the equation similar to Eq. (9) for  $Y_0$ —only  $\exp(-X)$  should be replaced with  $[C_i O_i]/[C] = X \exp(-X)$ . The solution is  $Y_1 = (X^2/2) \exp(-X)$ . In a similar way, the concentrations of all the larger clusters are found one by one

$$Y_n = [I_n C_i O_i]/[C] = (X^{n+1}/(n+1)!) \exp(-X). \quad (10)$$

The normalized concentrations  $Y_n$  are plotted in dependence of  $X = [VO]/[C]$  in Fig. 5, for  $n=0$  to 6. This plot shows that the population of carbon-based interstitial defects  $I_n C_i O_i$  is qualitatively different at small and large  $X$  (high and low carbon concentration):

At  $X < 1$  ( $[C] > [VO]$ ), the first species  $C_i O_i$  ( $n=0$ ) dominates, the second species  $IC_i O_i$  ( $n=1$ ) is a minor one, and larger species ( $n > 1$ ) are negligible.

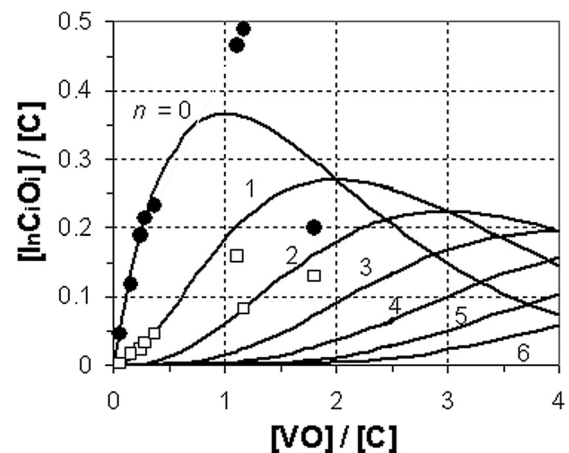


FIG. 5. Concentration of  $I_n C_i O_i$  species (normalized by the carbon concentration  $[C]$ ) calculated in dependence of  $X = [VO]/[C]$ . The experimental points—filled circles for  $C_i O_i$  ( $n=0$ ) and open squares for  $IC_i O_i$  ( $n=1$ )—correspond to the IR band calibration discussed below.

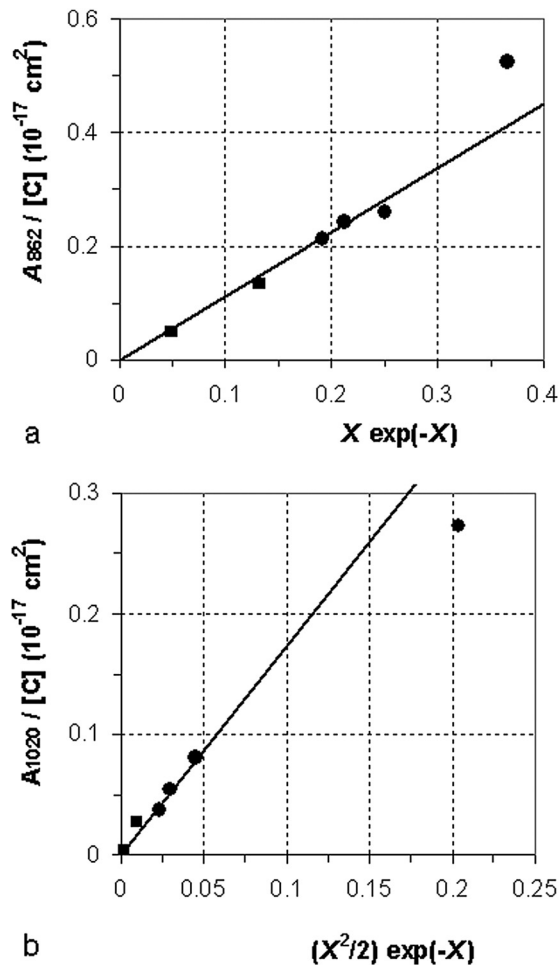


FIG. 6. Absorption intensity of: (a)  $C_iO_i$  ( $862\text{ cm}^{-1}$  band); (b)  $IC_iO_i$  ( $1020\text{ cm}^{-1}$  band) normalized by the carbon concentration  $[C]$ . The former is expected to be proportional to  $X \exp(-X)$  and the latter to  $(X^2/2) \exp(-X)$  where  $X = [VO]/[C]$ . The medium-carbon samples are shown by circles and the high-carbon ones by squares.

At  $X \gg 1$  ( $[C] \ll [VO]$ ), there are several species— $C_iO_i$ ,  $IC_iO_i$ ,  $I_2C_iO_i$ , etc—co-existing in comparable concentrations. An  $I_nC_iO_i$  cluster contains  $n + 1$  stored self-interstitials (one of them is represented by  $C_i$ ). The total amount of stored self-interstitials—a sum of  $(n + 1)$   $[I_nC_iO_i]$  over  $n$ —is equal to  $[VO]$ . The total cluster concentration—a sum of  $[I_nC_iO_i]$ —is identical to the carbon loss,  $[C] (1 - \exp(-X))$ , and therefore, the average size of the clusters,  $\langle n + 1 \rangle$ , is equal to  $X/(1 - \exp(-X))$ . At  $X \gg 1$ , all the initial carbon atoms are converted into the clusters and the average size is then simply  $[VO]/[C]$ .

The experimental points in Fig. 5 correspond to the calibration coefficients for the  $C_iO_i$  and  $IC_iO_i$  related bands deduced in Sec. III D. They follow, approximately, the computed curves for both  $[C_iO_i]/[C]$  ( $n = 0$ ) and  $[IC_iO_i]/[C]$  ( $n = 1$ ).

#### D. Calibration of the bands due to $C_iO_i$ and $IC_iO_i$

The concentration  $[C_iO_i]$  is proportional to the observed intensity  $A_{862}$  of the  $C_iO_i$ -related band (at  $862\text{ cm}^{-1}$ )

$$[C_iO_i] = \gamma_{862} A_{862}, \quad (11)$$

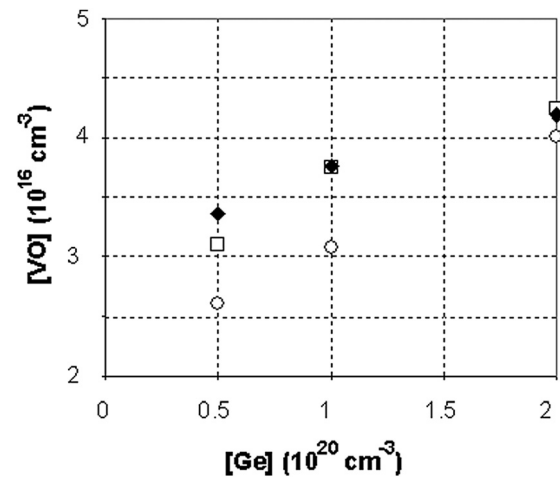


FIG. 7. The VO concentration in Ge-doped samples of Ref. 18, in dependence of  $[Ge]$  (open squares). The calculated carbon-controlled values of  $[VO]$  are shown by circles. The computed values shown by filled rhombs correspond to self-interstitial trapping by both germanium and carbon, with a proper trapping ratio  $\beta_{ge}/\beta_c = 7 \times 10^{-4}$ .

where  $\gamma_{862}$  is the optical calibration coefficient. Equation (10), at  $n = 0$ , means that the ratio  $A_{862}/[C]$  is expected to be proportional to  $X \exp(-X)$ , with a slope equal to  $1/\gamma_{862}$ . This plot is presented in Fig. 6(a) for the samples of moderate and high  $[C]$ . The expected proportionality is well fulfilled excepting a less reliable point of the highest  $X$  (the lowest carbon content), and the deduced calibration coefficient is  $\gamma_{862} = 8.9 \times 10^{16}\text{ cm}^{-2}$ . This is not far from a previously reported<sup>21</sup> value of  $1.1 \times 10^{17}\text{ cm}^{-2}$ .

Similarly, the intensity  $A_{1020}$  of the band due to  $IC_iO_i$ , if normalized by  $[C]$ , is predicted to be proportional to  $(X^2/2) \exp(-X)$ —by Eq. (10) at  $n = 1$ . This rule is consistent with the data (Fig. 6(b), for the same samples), and the deduced calibration for this band is  $\gamma_{1020} = 5.8 \times 10^{16}\text{ cm}^{-3}$ —some-what larger than the previously reported<sup>21</sup> value of  $3.8 \times 10^{16}\text{ cm}^{-2}$ .

#### E. Germanium as a self-interstitial trap in Si

The Ge impurity is known<sup>25</sup> to trap vacancies but only at low irradiation temperature ( $< 220\text{ K}$ ), implying a very small binding energy of V and  $Ge_s$ . For our irradiation temperature ( $70^\circ\text{C}$ ), no V trapping by  $Ge_s$  occurs. The reported concentration  $[VO]$  in Ge-doped samples<sup>18</sup> irradiated by 2 MeV electrons at a dose of  $5 \times 10^{17}\text{ cm}^{-2}$  is shown in Fig. 7 by open squares. These samples additionally contained<sup>18</sup> carbon. A separation of the two contributions—by C and by Ge—is now possible since the trapping parameter  $q_c$  for carbon was specified above. The carbon-controlled values of  $[VO]$ —computed by Eq. (6)—are shown by circles. These are systematically lower than the actual values of  $[VO]$ —indicating some Ge contribution into self-interstitial trapping. With two self-interstitial-trapping impurities, C and Ge, in all the above equations, the trapping rate by carbon—proportional to  $\beta_c [C]$ —should be modified by adding a term due to germanium,  $\beta_{ge} [Ge]$ . Equivalently,  $[C]$  should be replaced with  $[C] + [Ge] \beta_{ge}/\beta_c$ . The VO concentrations

calculated by Eq. (6) with this replacement (filled rhombs in Fig. 7) are close to the actual values with a proper choice of the trapping ratio:  $\beta_{\text{ge}}/\beta_{\text{c}} = 7 \times 10^{-4}$ . Germanium can compete with carbon for trapping self-interstitials only if the concentration ratio  $[\text{Ge}]/[\text{C}]$  is about 1000 or larger. The concentrations of produced interstitial species,  $\text{Ge}_i$  and  $\text{C}_i$ , are then comparable. Similar to  $\text{C}_i$ , the  $\text{Ge}_i$  species are likely to be highly mobile and to be immediately trapped by  $\text{O}_i$  into  $\text{Ge}_i\text{O}_i$ . The presence of  $\text{Ge}_i\text{O}_i$  in irradiated Ge-doped samples may account for the peculiarities<sup>26</sup> of isochronal annealing: a significant rise in  $[\text{O}_i]$  was found, started at 220 °C and accompanied by a reduction in  $[\text{VO}]$ . In the absence of Ge, no oxygen rise occurs, and VO starts to decay only at  $T \geq 300$  °C. These effects are straightforwardly explained by dissociation of  $\text{Ge}_i\text{O}_i$ . The liberated  $\text{Ge}_i$  atoms then release self-interstitials ( $\text{Ge}_i \rightarrow \text{Ge}_s + \text{I}$ ) which annihilate VO defects, thus leading to an additional rise in  $[\text{O}_i]$ .

#### IV. CONCLUSIONS

An impact of the carbon impurity on the production of the VO defect is clearly demonstrated by comparing samples of a wide range of the carbon content,  $[\text{C}]$ . An analytical model for VO production controlled by self-interstitial trapping by carbon (or generally also by other impurities) is developed. The VO concentration,  $[\text{VO}]$ , is obtained as a function of the dose and of  $[\text{C}]$ . It is concluded that carbon is only slightly less efficient a trap than VO. The concentrations of carbon-related interstitial species ( $\text{C}_i\text{O}_i$ ,  $\text{IC}_i\text{O}_i$ , etc) are expressed as functions of  $[\text{VO}]/[\text{C}]$  ratio, and the optical calibration coefficients for the  $\text{C}_i\text{O}_i$  and  $\text{IC}_i\text{O}_i$  defects are determined.

In samples containing both carbon and germanium,  $[\text{VO}]$  is systematically higher than the calculated value controlled

by carbon—showing that also Ge is a trap for self-interstitials, although 1000 times less efficient than carbon.

- <sup>1</sup>G. D. Watkins, *J. Phys. Soc. Jpn.* **18**(Suppl. II), 22 (1963).
- <sup>2</sup>G. D. Watkins and J. W. Corbett, *Phys. Rev.* **121**, 1001 (1961).
- <sup>3</sup>J. W. Corbett, G. D. Watkins, and R. S. Mc Donald, *Phys. Rev.* **135**, A 1381 (1964).
- <sup>4</sup>C. A. Londos, N. V. Sarlis, L. G. Fytros, and K. Papastergiou, *Phys. Rev. B* **53**, 6900 (1996).
- <sup>5</sup>H. J. Stein, *Mater. Sci. Forum* **10–12**, 935 (1986).
- <sup>6</sup>J. L. Lindström and B. G. Svensson, in *MRS Symposia Proceedings No. 59* (Materials Research Society, Pittsburgh, 1986), p. 45.
- <sup>7</sup>L. C. Kimerling, in *Radiation Effects in Semiconductors*, edited by N. B. Urali and J. W. Corbett IOP Conference Ser. No. 31 (IOP, Bristol/London, 1977), p. 221.
- <sup>8</sup>C. A. Londos, *Phys. Status Solidi A* **92**, 609 (1985).
- <sup>9</sup>C. A. Londos, *Phys. Status Solidi A* **113**, 503 (1989).
- <sup>10</sup>J. Coutinho, R. Jones, P. R. Briddon, and S. Öberg, *Phys. Rev. B* **62**, 10824 (2000).
- <sup>11</sup>G. Davies, A. S. Oates, R. C. Newman, R. Wooley, E. C. Lightowlers, M. J. Binns, and J. G. Wilkes, *J. Phys. C* **19**, 841 (1986).
- <sup>12</sup>C. A. Londos, *Jpn. J. Appl. Phys., Part 1* **27**, 2089 (1988).
- <sup>13</sup>C. A. Londos, *Phys. Status Solidi A* **102**, 639 (1987).
- <sup>14</sup>C. A. Londos, *Semicond. Sci. Technol.* **5**, 645 (1990).
- <sup>15</sup>R. C. Newman, in *MRS Symposia Proceedings No. 59* (Materials Research Society, Pittsburgh, 1986), p. 403.
- <sup>16</sup>C. A. Londos, *Phys. Rev. B* **35**, 6295 (1987).
- <sup>17</sup>V. D. Ahmetov and V. V. Bolotov, *Radiat. Eff.* **52**, 149 (1980).
- <sup>18</sup>C. A. Londos, A. Andrianakis, V. V. Emtsev, and H. Ohyama, *J. Appl. Phys.* **105**, 123508 (2009).
- <sup>19</sup>A. BreLOT, *IEEE Trans. Nucl. Sci.* **19**, 220 (1972).
- <sup>20</sup>A. S. Oates and R. C. Newman, *Appl. Phys. Lett.* **49**, 262 (1986).
- <sup>21</sup>G. Davies, E. C. Lightowlers, R. C. Newman, and A. S. Oates, *Semicond. Sci. Technol.* **2**, 524 (1987).
- <sup>22</sup>G. Davies, *Mater. Sci. Forum* **38–41**, 151 (1989).
- <sup>23</sup>G. Davies and R. C. Newman, in *Handbook on Semiconductors*, edited by S. Mahajan (Elsevier, Amsterdam, 1994) Vol. 3, p. 1557.
- <sup>24</sup>J. W. Corbett and G. D. Watkins, *Phys. Rev.* **138**, A555 (1965).
- <sup>25</sup>A. BreLOT, in *Damage and Defects in Semiconductors*, edited by J. E. Whitehouse (Institute of Physics, London, 1973), p. 191.
- <sup>26</sup>C. A. Londos, A. Andrianakis, E. N. Sgourou, V. V. Emtsev, and H. Ohyama, *J. Appl. Phys.* **109**, 033508 (2011).