

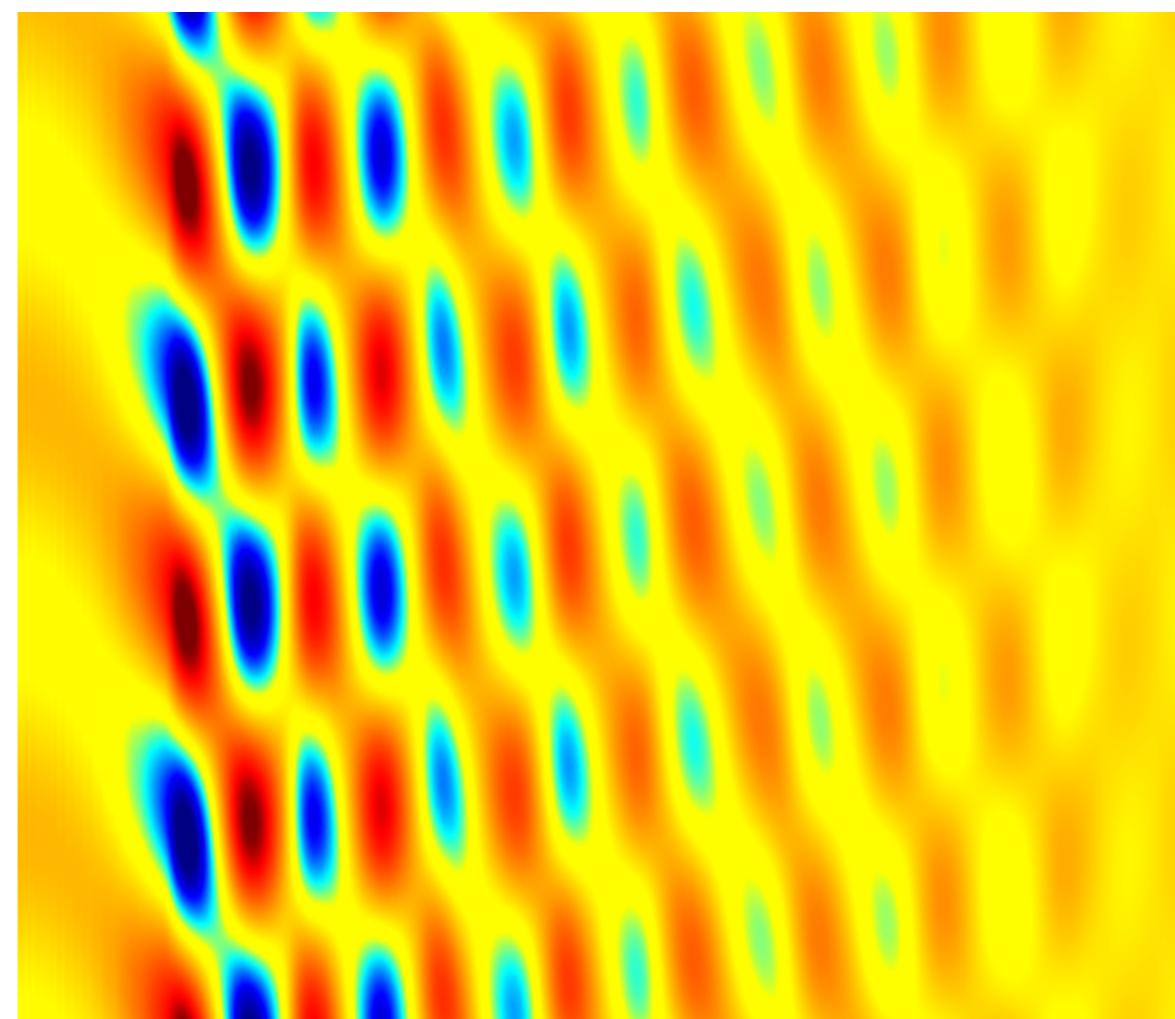


Phys. Rev. Lett. 106, 021302 (2011)

Black hole physics in the laboratory



- **Greg Lawrence**
- **Matt Penrice**
- **Ted Tedford**
- **Bill Unruh**
- Silke Weinfurtner**



General idea behind my line of research

General idea is...

to test various aspects of quantum gravity in table-top experiments

some aspects/ideas of/for quantum gravity that are otherwise hard to impossible to access observationally/experimentally

...using
 * fluids and superfluids
 * condensed matter systems
 * quantum information
 in
theoretical, numerical & experimental studies.



semi-classical

&

quantum gravity

classical and quantum field theory in curved spacetimes

discrete gravity & effective field theories

- super-radiant scattering from rotating black holes
ongoing experiment at SISSA
- **black-hole radiation**
experiment carried out at UBC
- cosmological particle production
ongoing theoretical studies
future experiments...

- emergence of a smooth geometry as an ensemble average over discrete geometries (analogue CDT)
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...and to apply quantum gravity studies to other branches of physics

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Semi-classical gravity ➤ (Q)FT in curved spaces

Gravitational field is classical and **back-reaction** of the quantum processes onto the classical gravitational field are **negligible**.

Simple example:

(i) waves propagating on **flat** spacetime (massless minimally coupled Klein-Gordon scalar field):

$$\frac{1}{c^2} \frac{\partial^2}{\partial t^2} \psi = \nabla^2 \psi \quad \text{equivalently to} \quad \partial_a (\sqrt{-\eta} \eta^{ab} \partial_b \psi) = 0 \quad \text{where} \quad \eta_{ab} = \begin{bmatrix} -c^2 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

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(ii) “minimal substitution” **curved** spacetime :

$$\partial_a (\sqrt{-g} g^{ab} \partial_b \psi) = 0$$

where

$$g_{ab} = \begin{bmatrix} g_{00}(\mathbf{x}, t) & g_{01}(\mathbf{x}, t) & g_{02}(\mathbf{x}, t) & g_{03}(\mathbf{x}, t) \\ g_{01}(\mathbf{x}, t) & g_{11}(\mathbf{x}, t) & g_{12}(\mathbf{x}, t) & g_{13}(\mathbf{x}, t) \\ g_{02}(\mathbf{x}, t) & g_{12}(\mathbf{x}, t) & g_{22}(\mathbf{x}, t) & g_{23}(\mathbf{x}, t) \\ g_{03}(\mathbf{x}, t) & g_{13}(\mathbf{x}, t) & g_{23}(\mathbf{x}, t) & g_{33}(\mathbf{x}, t) \end{bmatrix}$$



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(iii) quantized Klein-Gordon scalar on generally curved-spacetime:

$$\partial_a (\sqrt{-g} g^{ab} \partial_b \hat{\psi}) = 0 \quad \text{where} \quad G_{ab}(g_{ab}, \Lambda) \neq 8\pi G_N \langle \hat{T}_{ab} \rangle$$

QFT in CS ➤ Analogue/Effective Gravity

Analogue gravity systems:

The equations of motion for linear perturbations in an analogue/effective/emergent gravity system can be simplified to

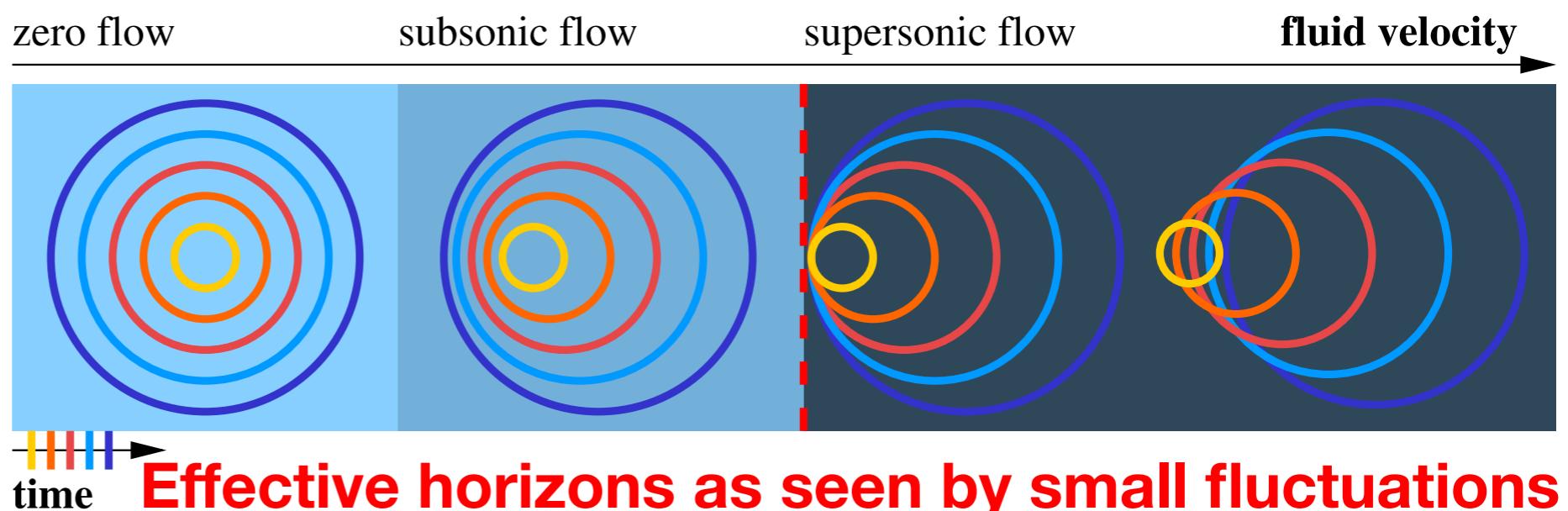
$$\frac{1}{\sqrt{-g}} \partial_a (\sqrt{-g} g^{ab} \partial_b \psi) = 0$$

defining an effective/acoustic/emergent metric tensor:

$$g_{ab} \propto \begin{bmatrix} - (c^2(\mathbf{x}, t) - v^2(\mathbf{x}, t)) & -\vec{v}^T(\mathbf{x}, t) \\ -\vec{v}(\mathbf{x}, t) & \mathbf{I}_{d \times d} \end{bmatrix}$$

Simple example:

Small fluctuations in
inviscid,
irrotational,
incompressible
fluid flow



Where do we expect such a behavior?

Broad class of systems with various dynamical equations, e.g. electromagnetic waveguide, fluids, ultracold gas of Bosons and Fermions.

In example below: Fluid dynamics derived from conservation laws:

$$\frac{\partial \rho}{\partial t} + \nabla \cdot (\rho \mathbf{v}) = 0 \quad \textit{Continuity equation}$$

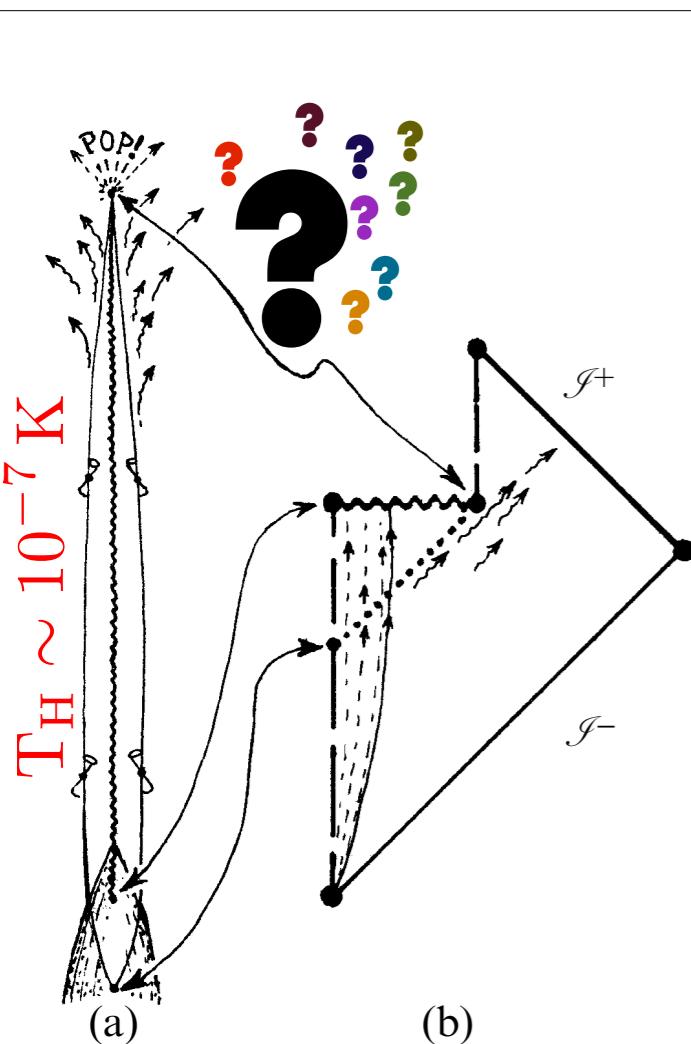
$$\rho \frac{D \mathbf{v}}{D t} = -\nabla p \quad \textit{Euler equation}$$

Analogue Gravity ➤ Applications

Let us first put aside the issue of classical versus quantum field theory in curved spacetimes...

1981: Experimental black hole evaporation?
W.G. Unruh

Possibility for experimental verification of the generality (UV-independence) of effects predicted within quantum field theory in curved spacetimes!

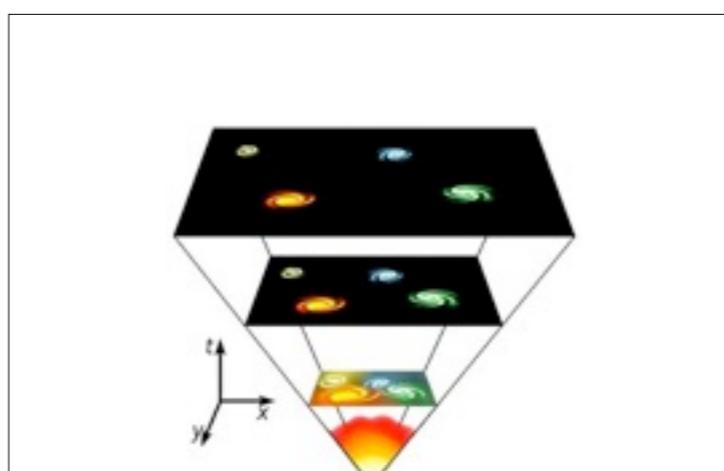
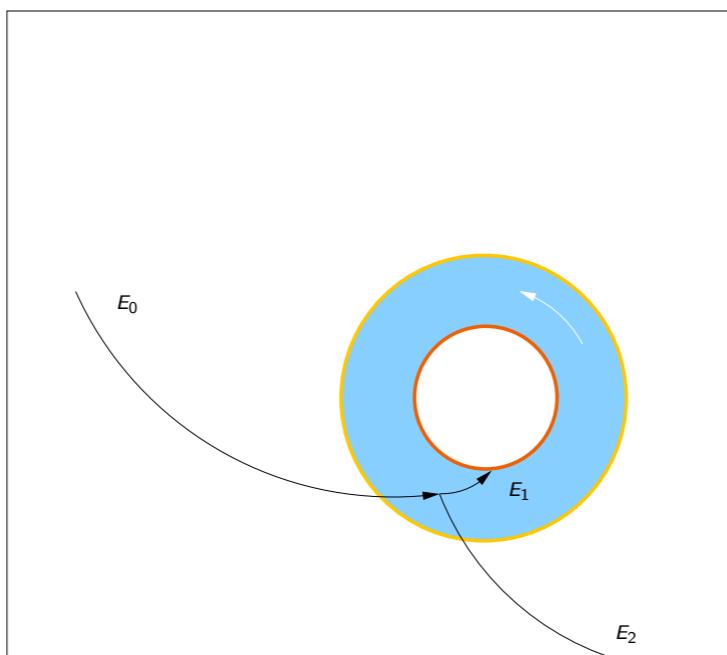


Example 1:

Experimental Black Hole Evaporation

Example 2:

Superradiant scattering from rotating black holes



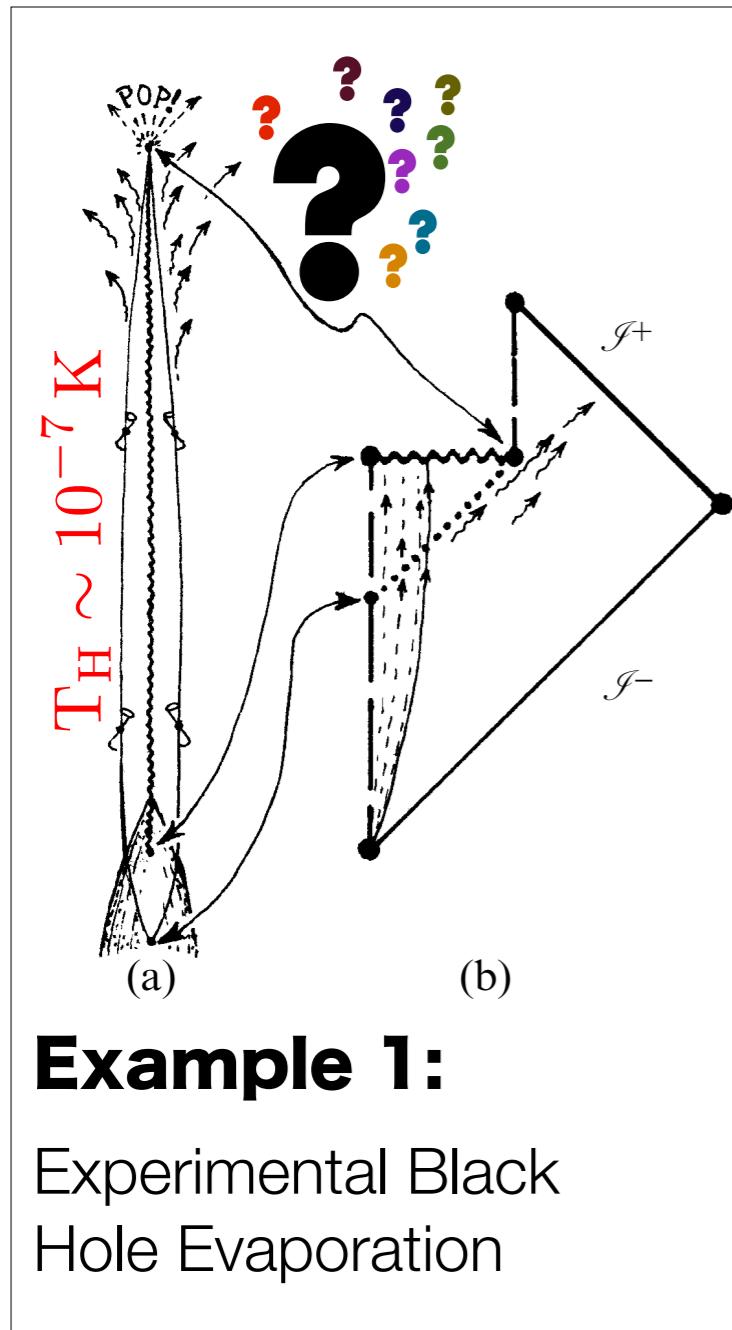
Example 3:

Cosmological particle production

Analogy Gravity: Strong model dependent deviations and eventual break-down at ‘small’ scales expected!

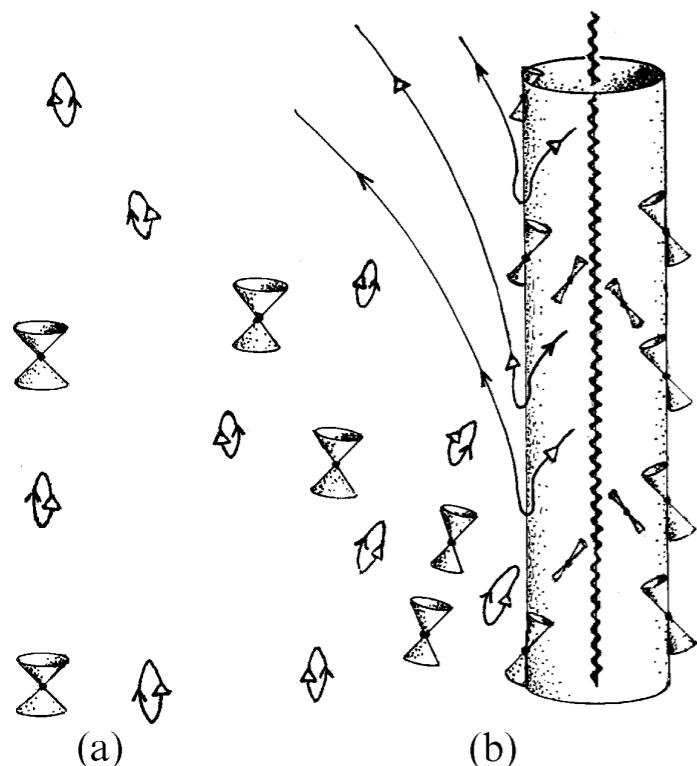
Experimental Black Hole Evaporation [Example 1]

How do black holes lose their mass..?



- (1) What is Hawking radiation?
- (2) Is there a reason why we should at all doubt that black holes evaporate..?
- (3) How can we set up a table-top experiment that “conclusively” tests Hawking/Unruh’s prediction?

BHE process ➤ What is Hawking radiation?



Pair-creation:

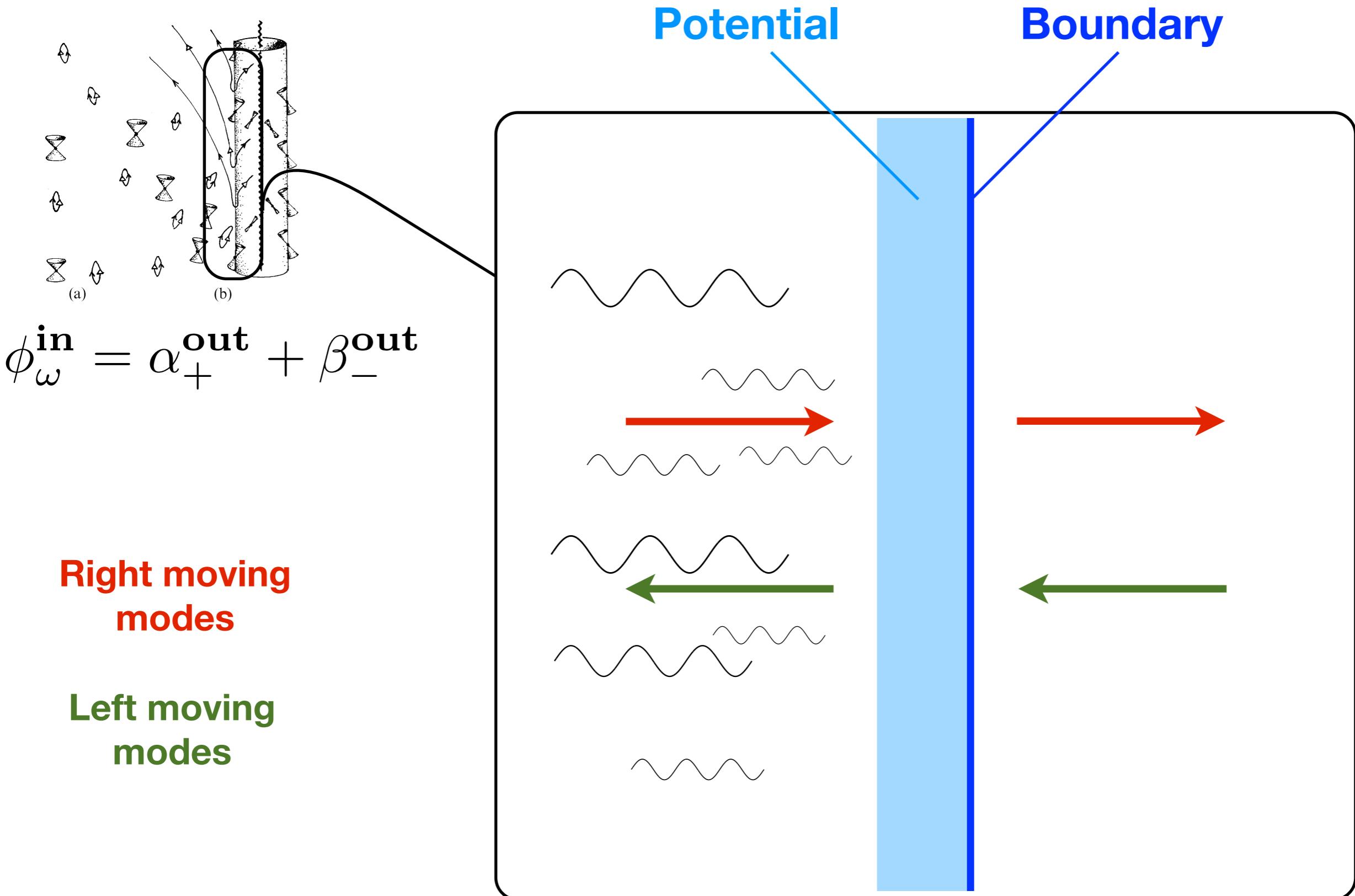
Separation of particle-anti-particle pairs from the quantum vacuum;
Negative norm modes absorbed by black hole;

[Particle Creation by Black Holes, by Stephen Hawking, in 1974]

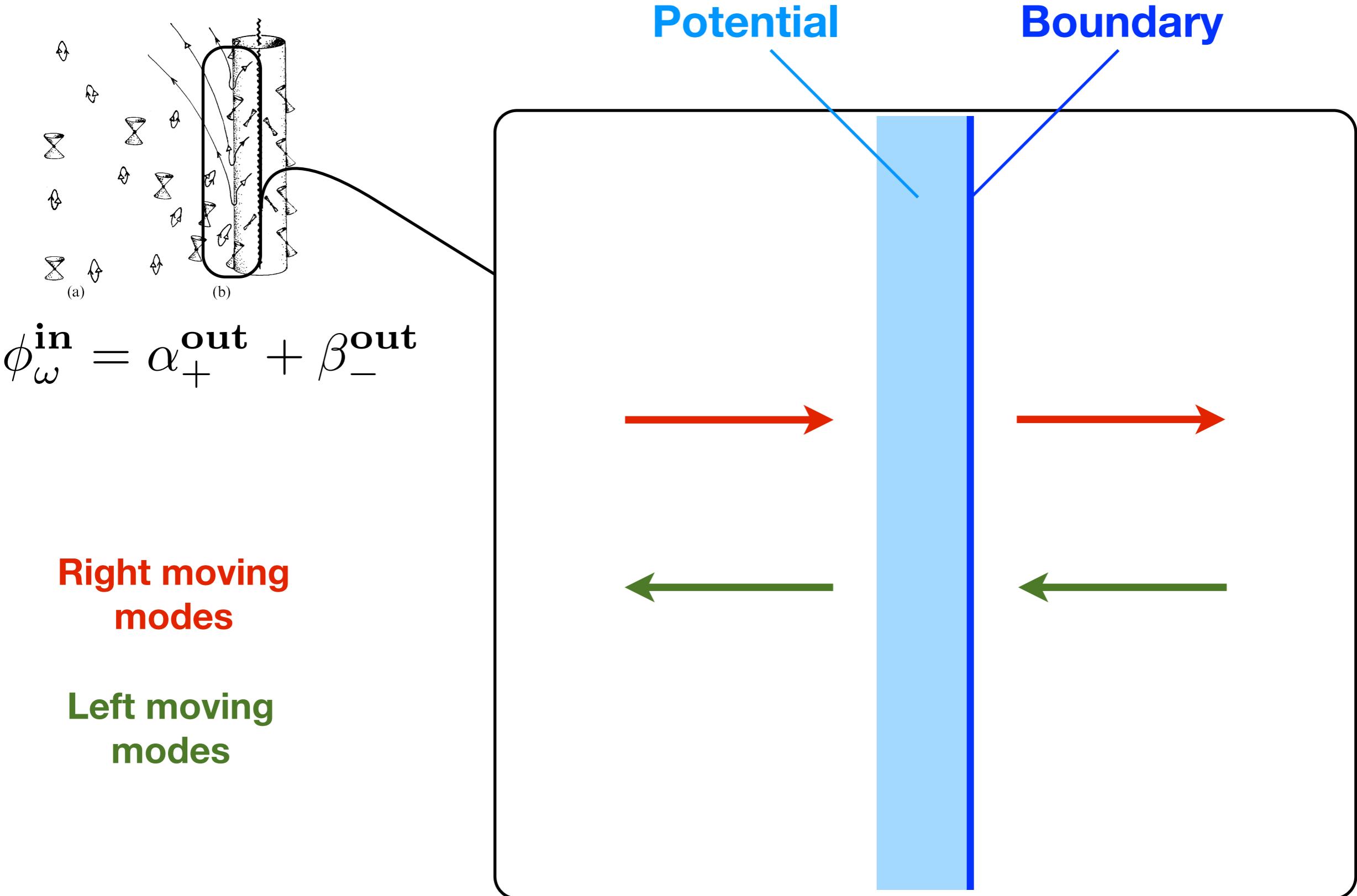
$$\phi_{\omega}^{\text{in}} = \alpha_+^{\text{out}} + \beta_-^{\text{out}}$$

Let's try to understand Hawking radiation as a simple scattering process...

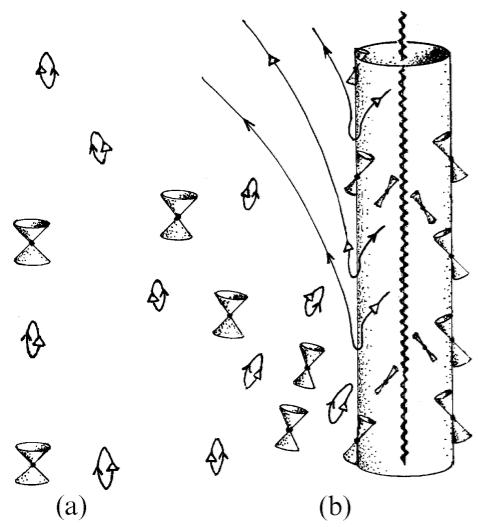
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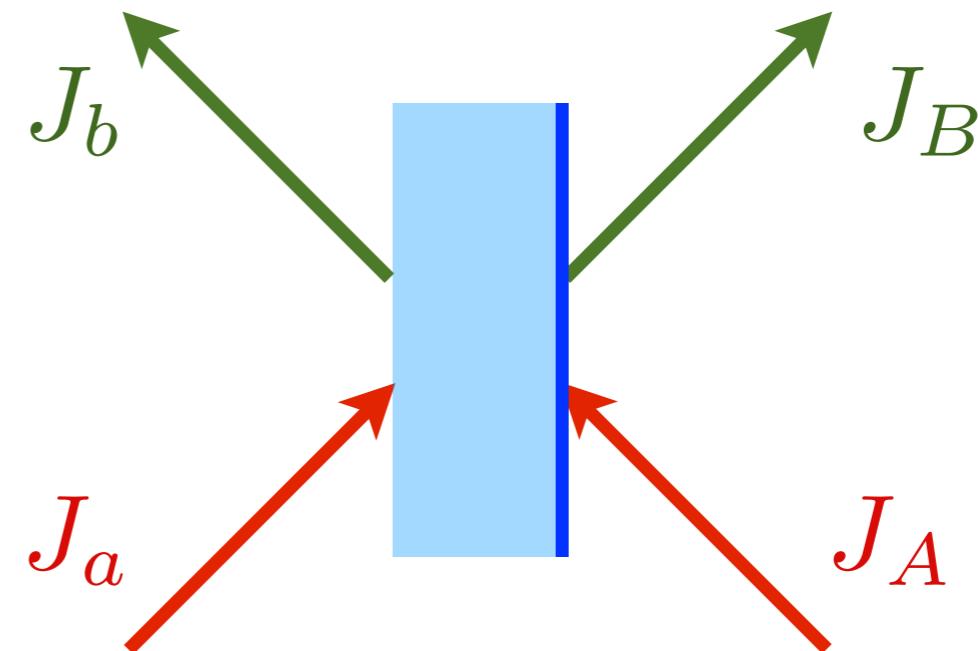
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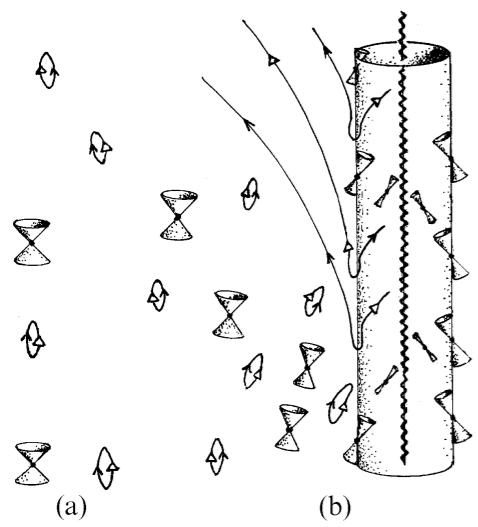
Modes moving
into potential

Modes moving
out of potential



$$J_a + J_A = J_b + J_B$$

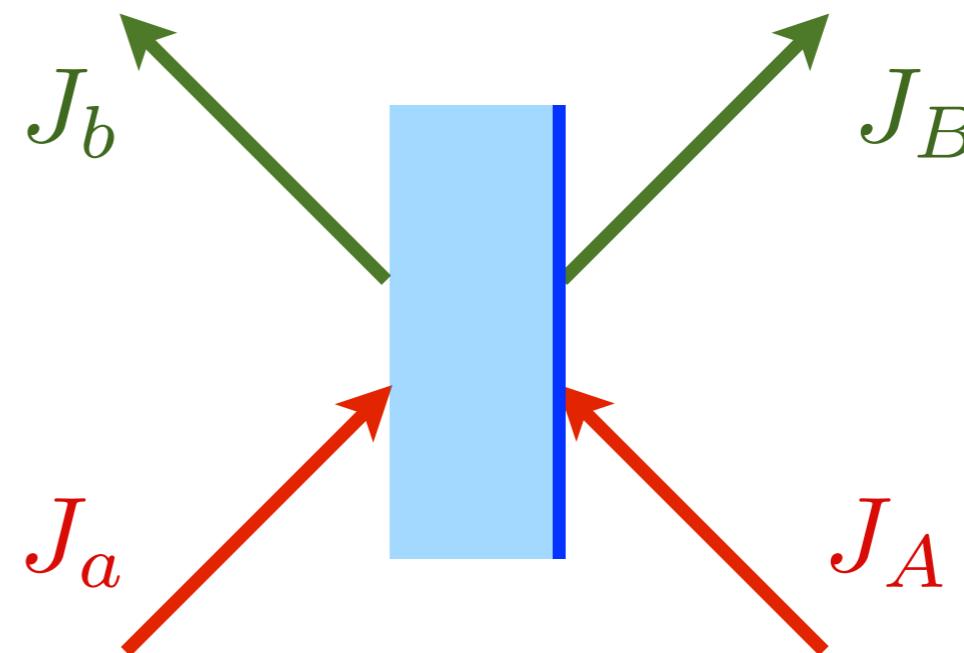
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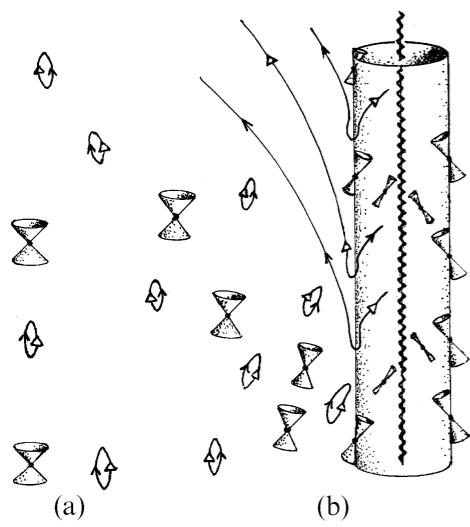
Conserved quantity: Particle current:

$$J_n := |A_n|^2 \Omega|_{\pm\infty} \frac{d\omega}{dk} \Big|_{k_n}$$



$$J_a + J_A = J_b + J_B$$

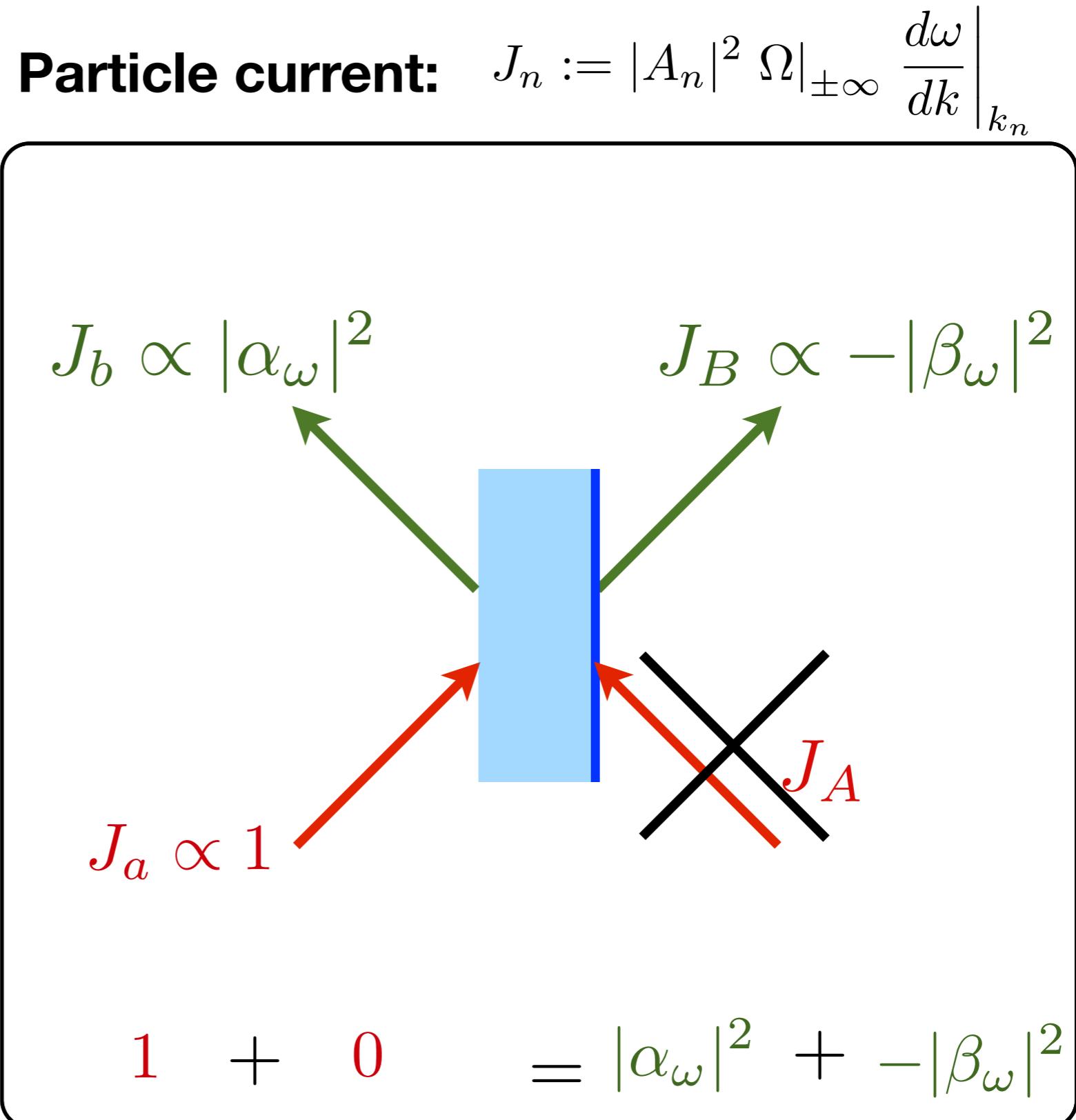
BHE process ➤ What is Hawking radiation?



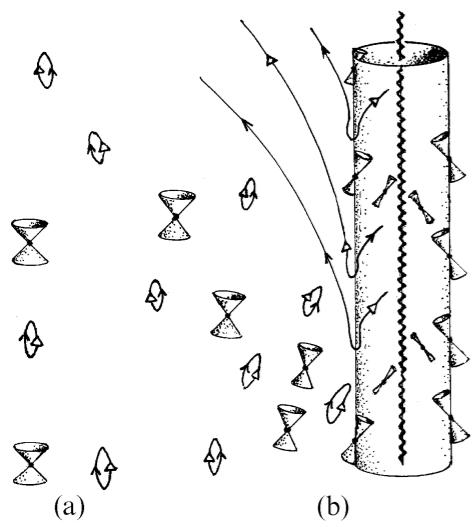
$$\phi_{\omega}^{\text{in}} = \alpha_+^{\text{out}} + \beta_-^{\text{out}}$$

$$\frac{|\beta_{\omega}|^2}{|\alpha_{\omega}|^2} = e^{-\frac{2\pi\omega}{g_H}} = e^{-\frac{\hbar\omega}{k_B T}}$$

$$|\alpha_{\omega}|^2 - |\beta_{\omega}|^2 = 1$$



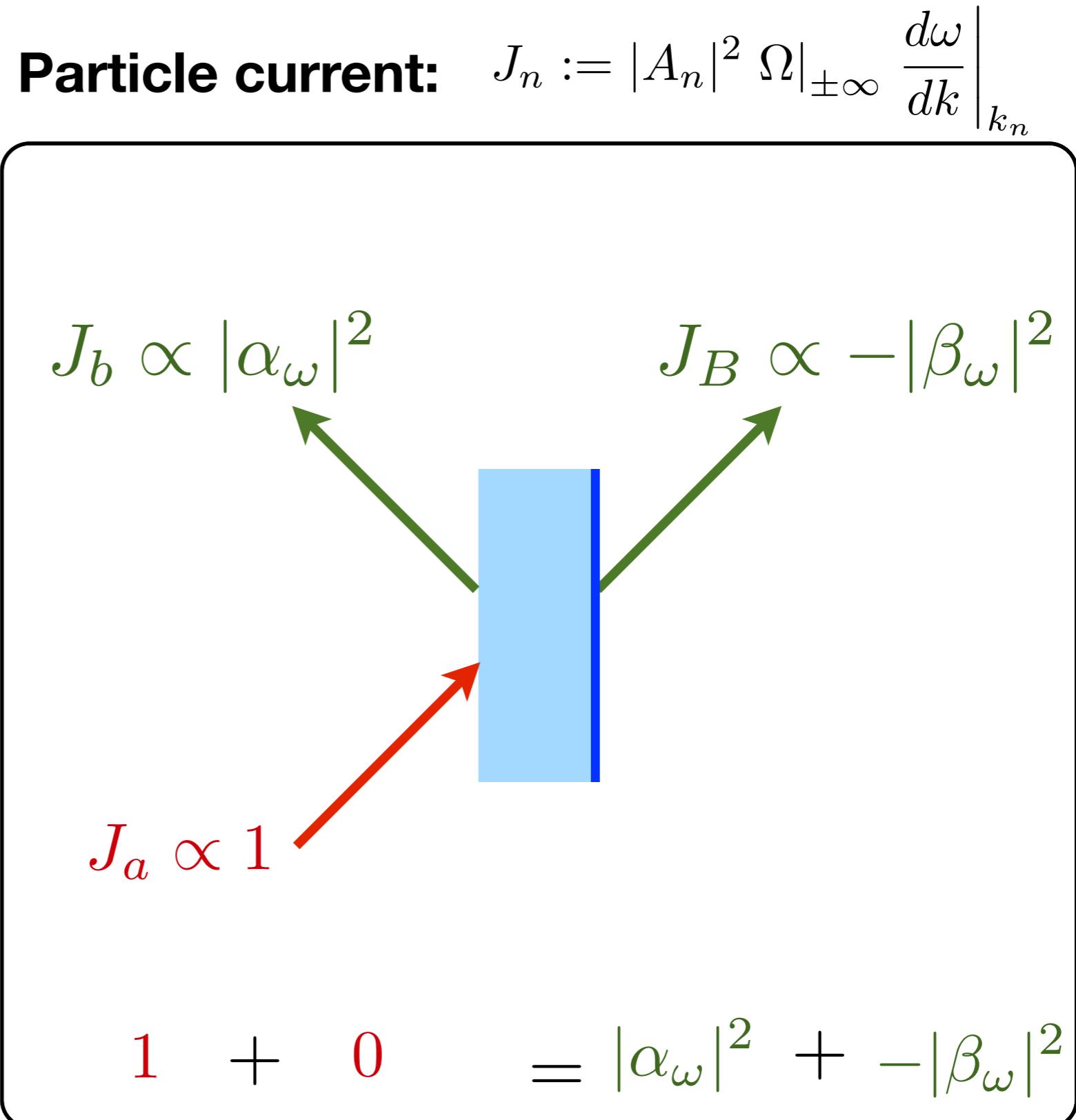
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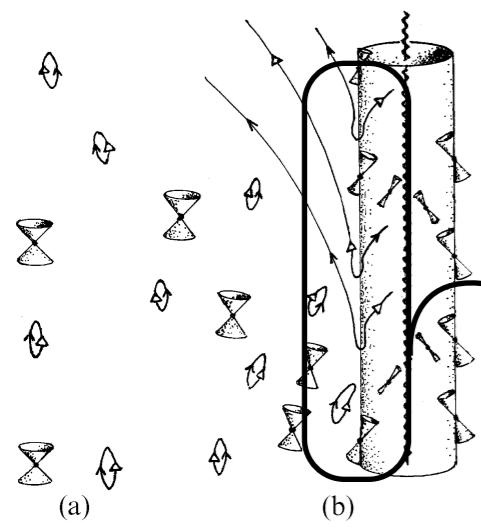
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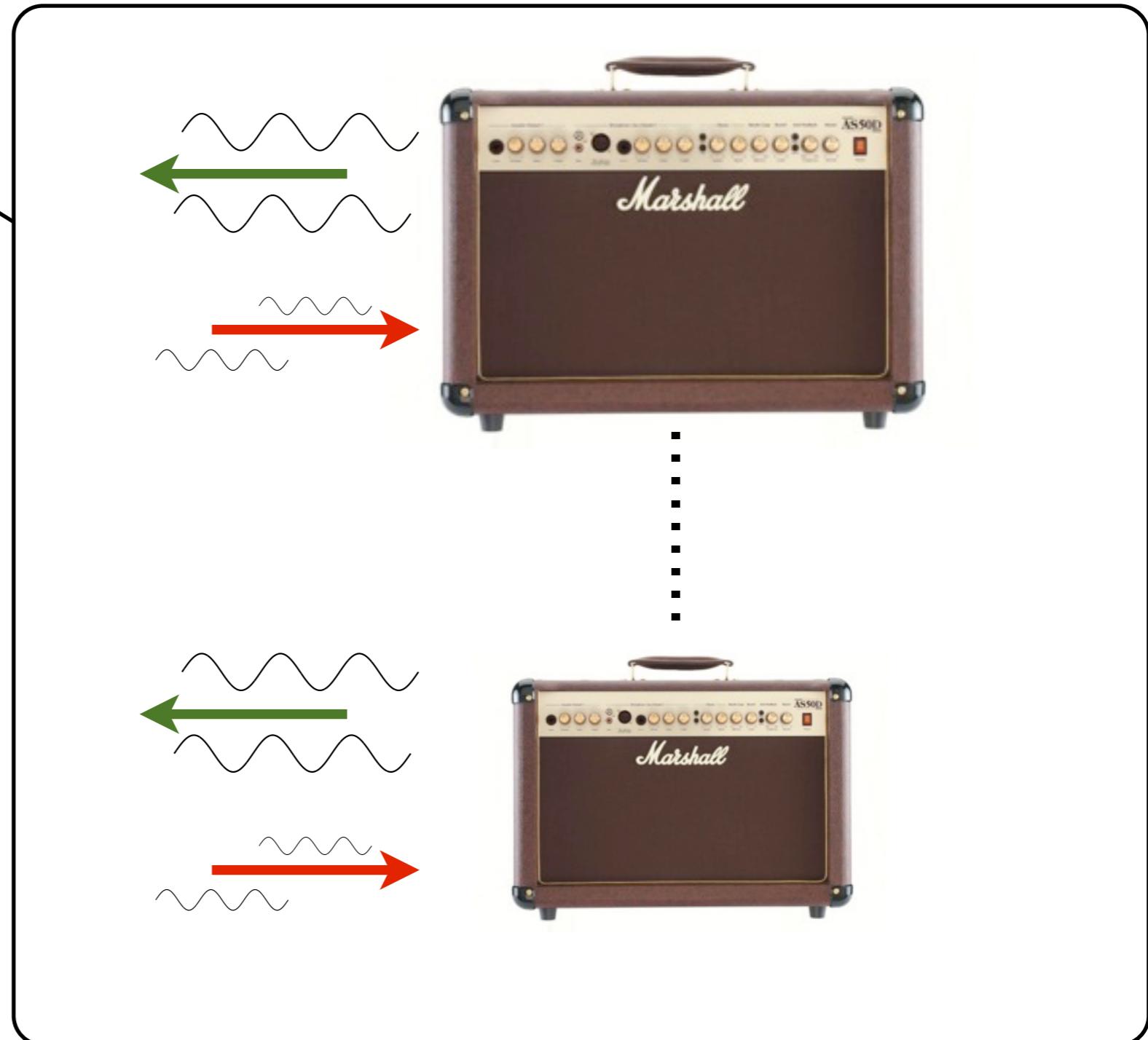
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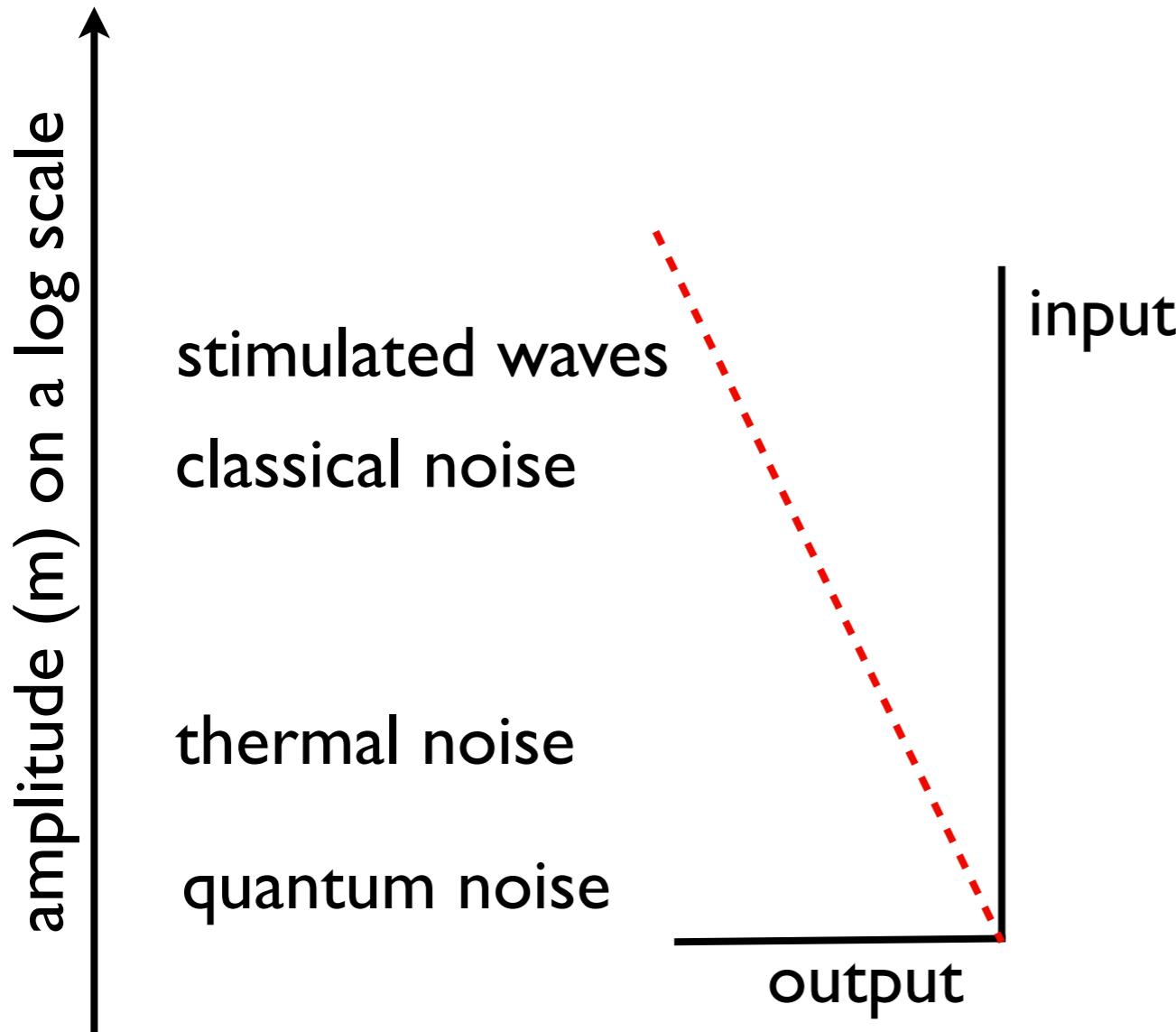
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- ✓ pair-creation process
- ✓ Boltzmann distribution
- ✓ surface gravity



BHE process ➤ What is being amplified?



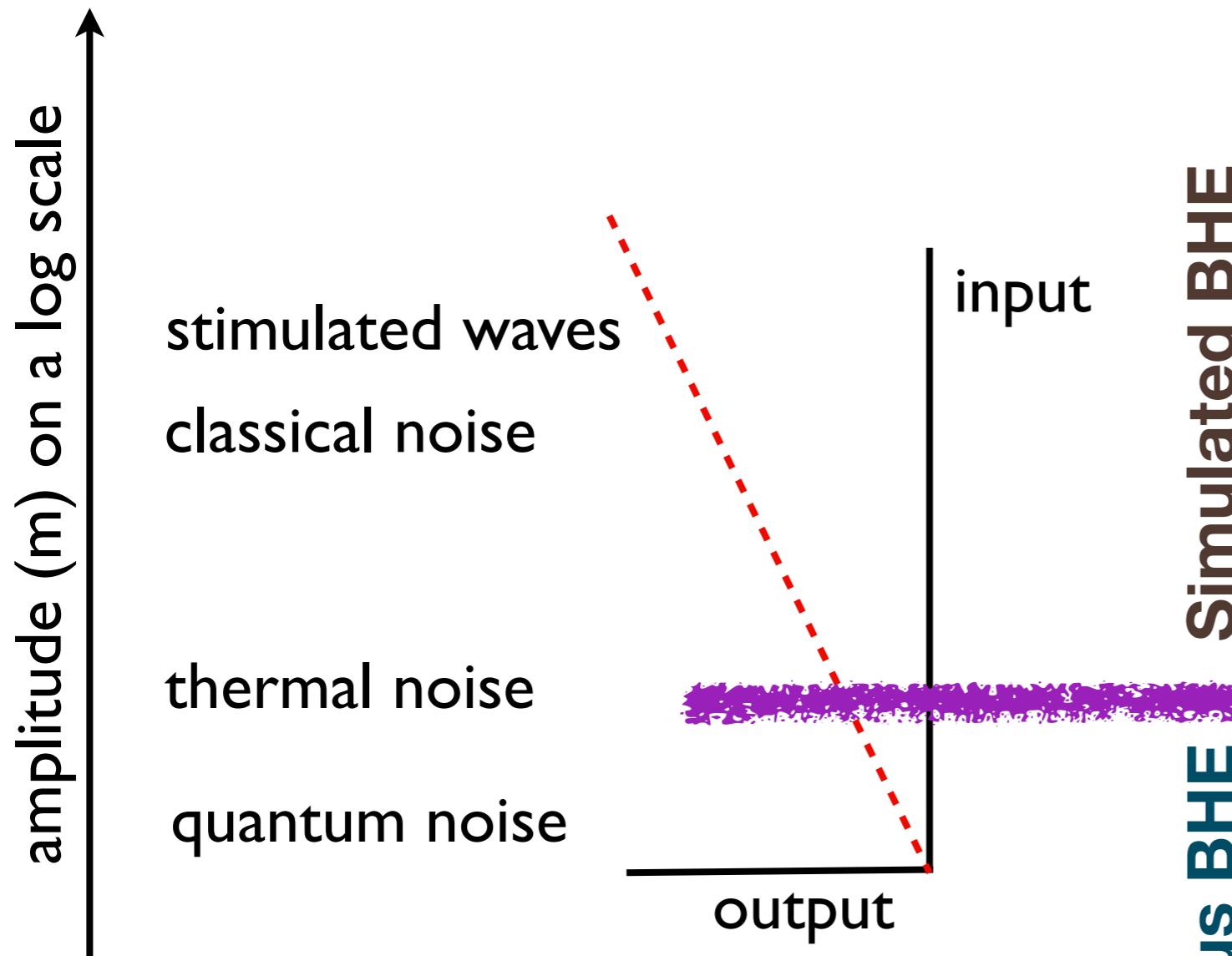
Assumption:

Linear amplifier over a huge range!

- ✓ pair-creation process (classical correlations)
- ✓ Boltzmann distribution
- ✓ surface gravity



BHE process ➤ What is being amplified?



Spontaneous BHE

Assumption:

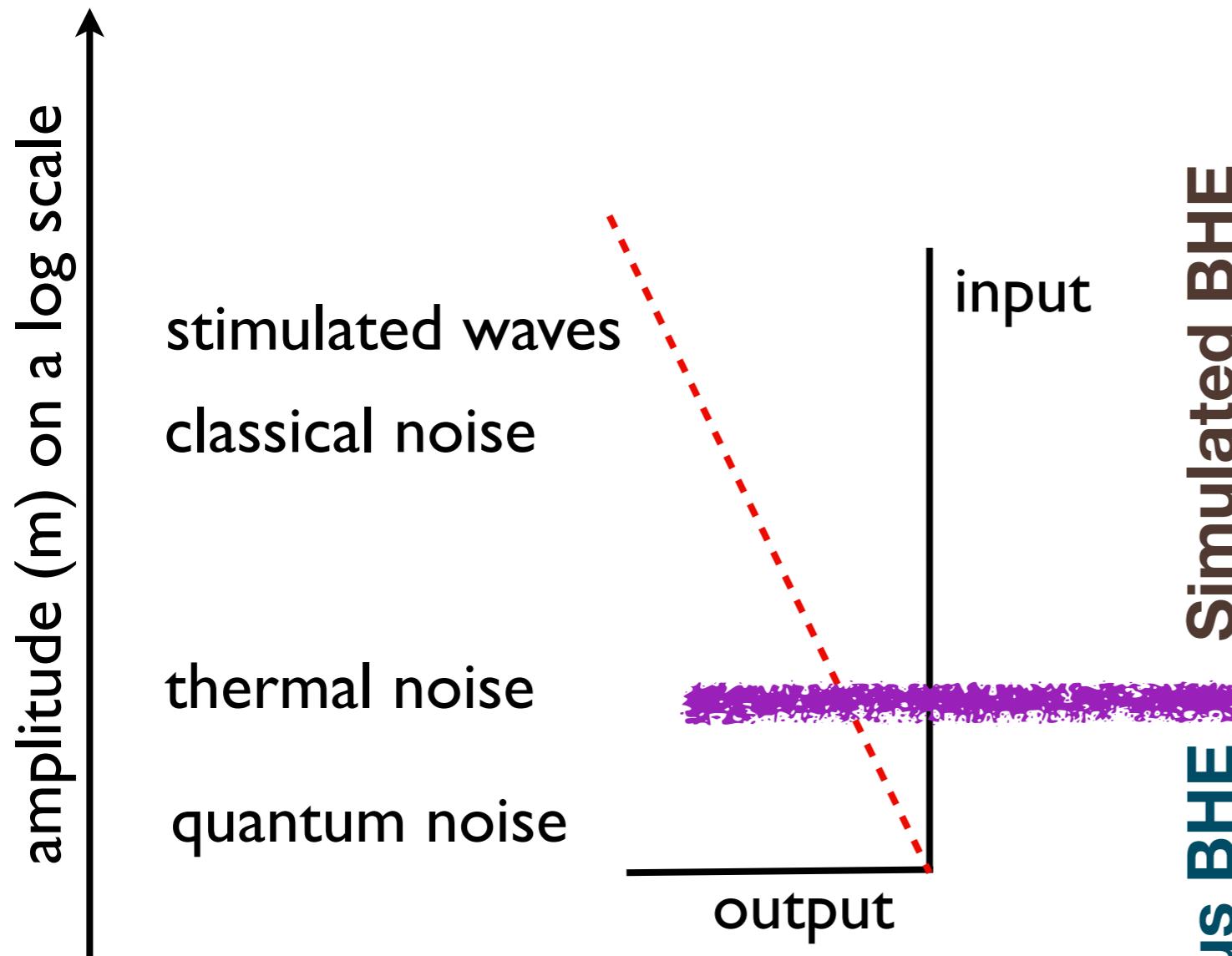
Linear amplifier over a huge range!

- ✓ pair-creation process (classical correlations)
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- ✓ surface gravity



- ✓ quantum correlations

BHE process ➤ What is being amplified?



why do we care: the UV-problem

Spontaneous BHE Simulated BHE

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- ✓ surface gravity



- ✓ quantum correlations

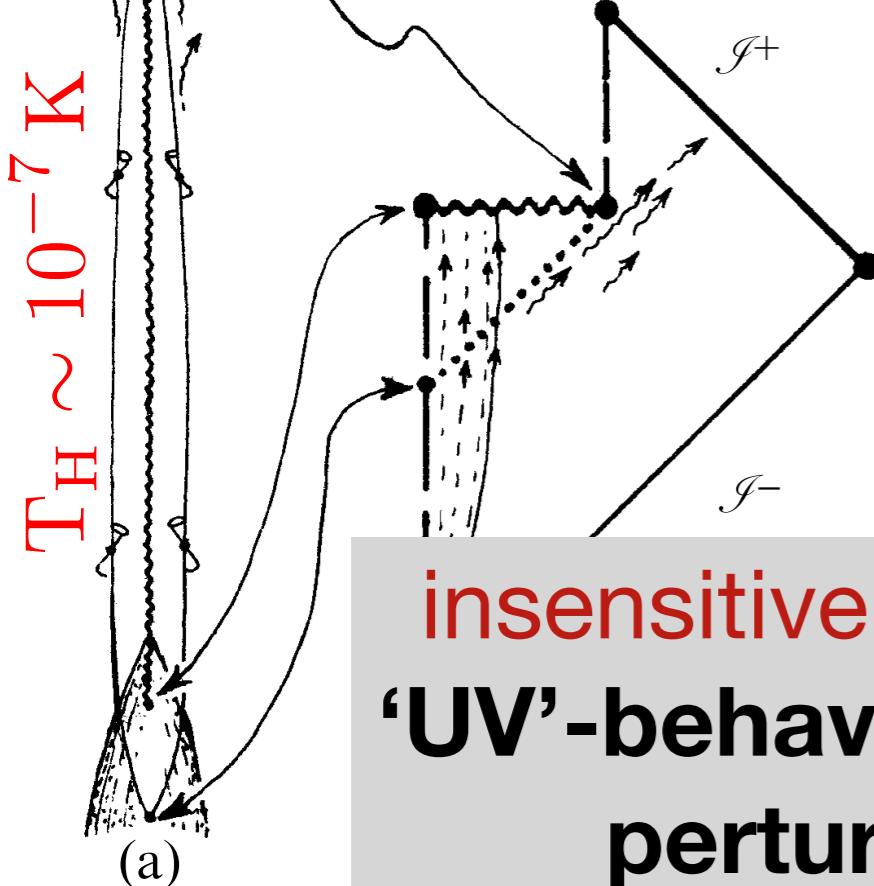
BHE process ➤ the UV-problem

Equation of motion for
linear perturbations in
analogue gravity systems:

[Wave equation on effective curved spacetime]

$$\frac{1}{\sqrt{-g}} \partial_a (\sqrt{-g} g^{ab} \partial_b \phi_1) = 0$$

1981: Experimental black hole evaporation ?, by Bill Unruh; Vol 46, #21, PRL.



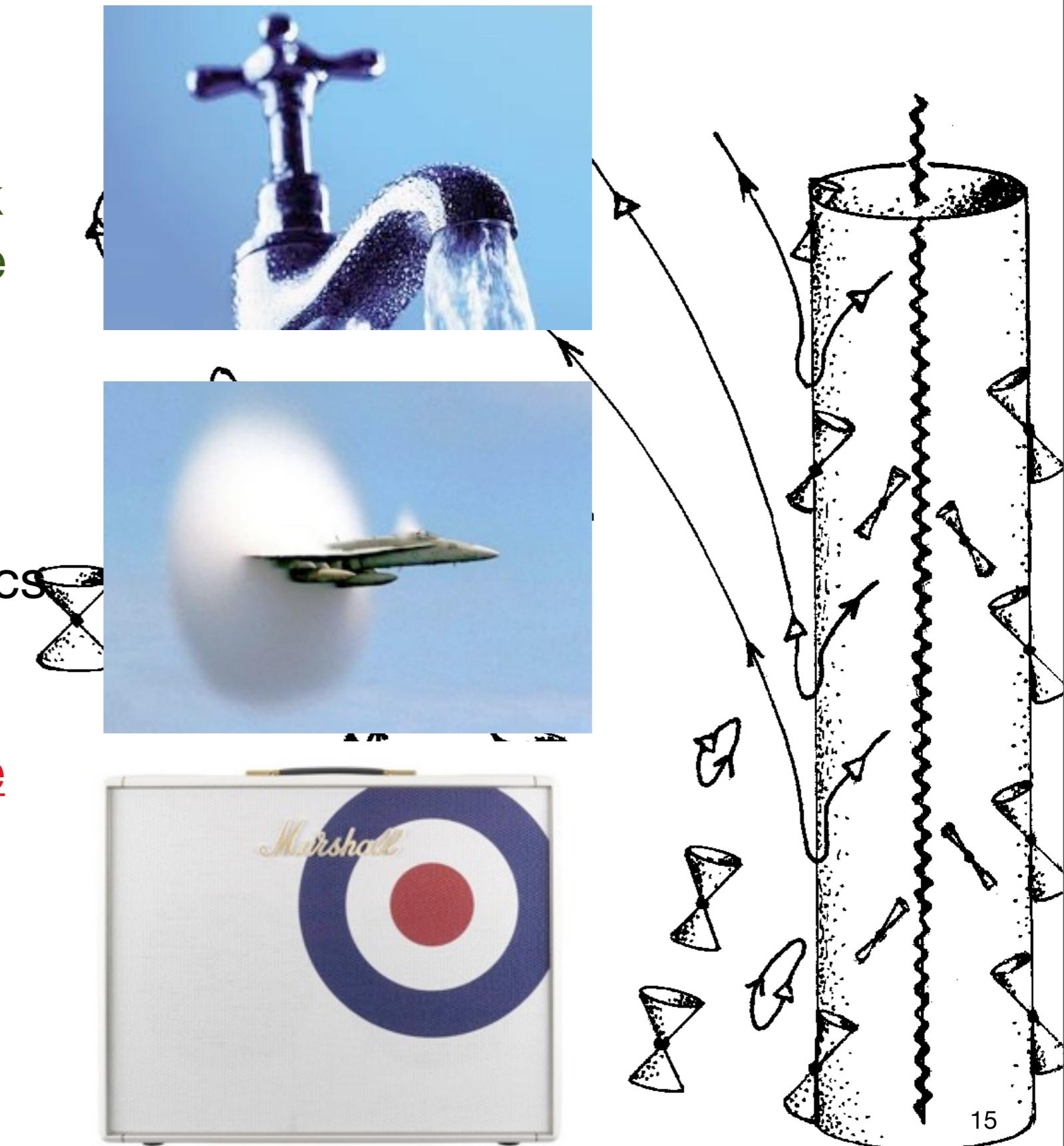
insensitive to particular
'UV'-behaviour of linear
perturbations

Possibility to test experimentally
the **generality** of the **Hawking**
process!

robust against
model-specific
dynamics

Scientific goal ➤ conclusive detection of BHE

- Spontaneous versus stimulated emission: Black holes are phase insensitive linear amplifiers...
- Nature of Hawking process: Semi-classical quantum gravity effect, where the Einstein dynamics is not taken into consideration.
- Black versus white hole emission: White holes are the time-reversal of black holes, and the Hawking process applies to both.



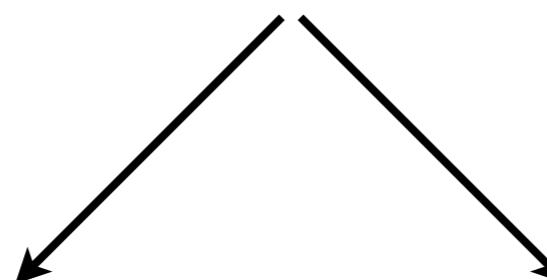
Our experiment ➤ Principle idea

2002: Schutzhold & Unruh: Gravity wave analogs of black holes (Phys. Rev. D66 044019)

Our experiment in a nutshell

Set-up: Surface waves on open channel flow with varying depth.

- stationary
- irrotational
- *incompressible*
- *inviscid*



$$v = v(x) = \frac{q}{h(x)} \propto \frac{1}{h(x)}$$

$$c = c(x) \approx \sqrt{gh(x)} \propto \sqrt{h(x)}$$

Let's recall the acoustic line-element:

$$g_{ab} \propto \begin{bmatrix} - (c^2 - v^2) & -\vec{v}^T \\ -\vec{v} & \mathbf{I}_{d \times d} \end{bmatrix}$$

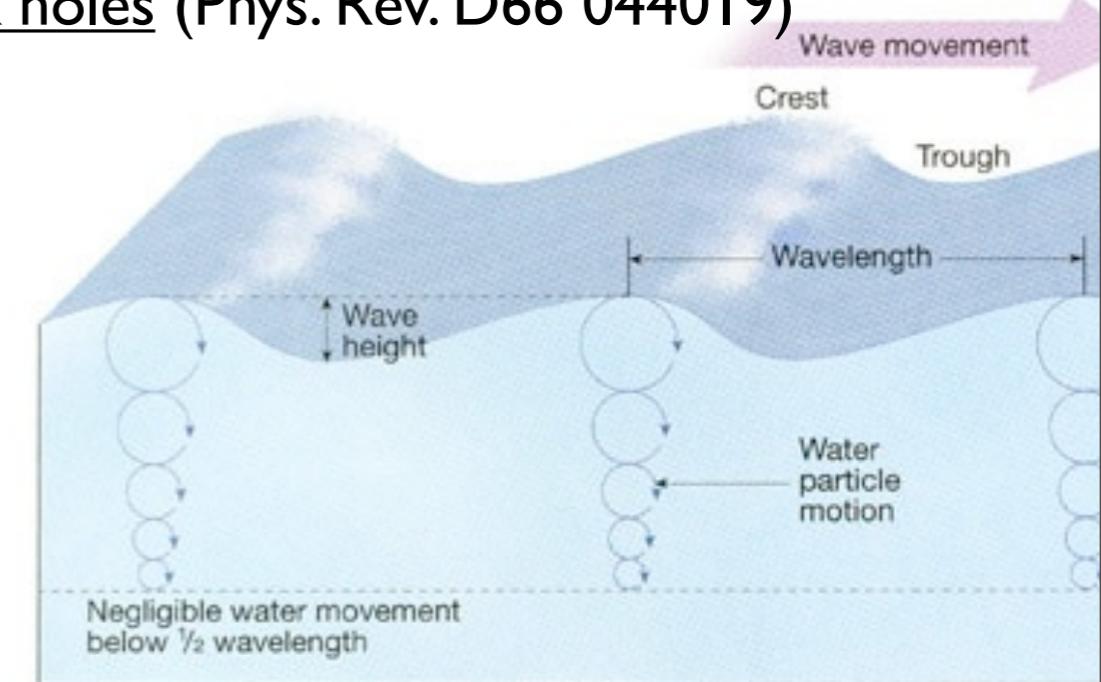


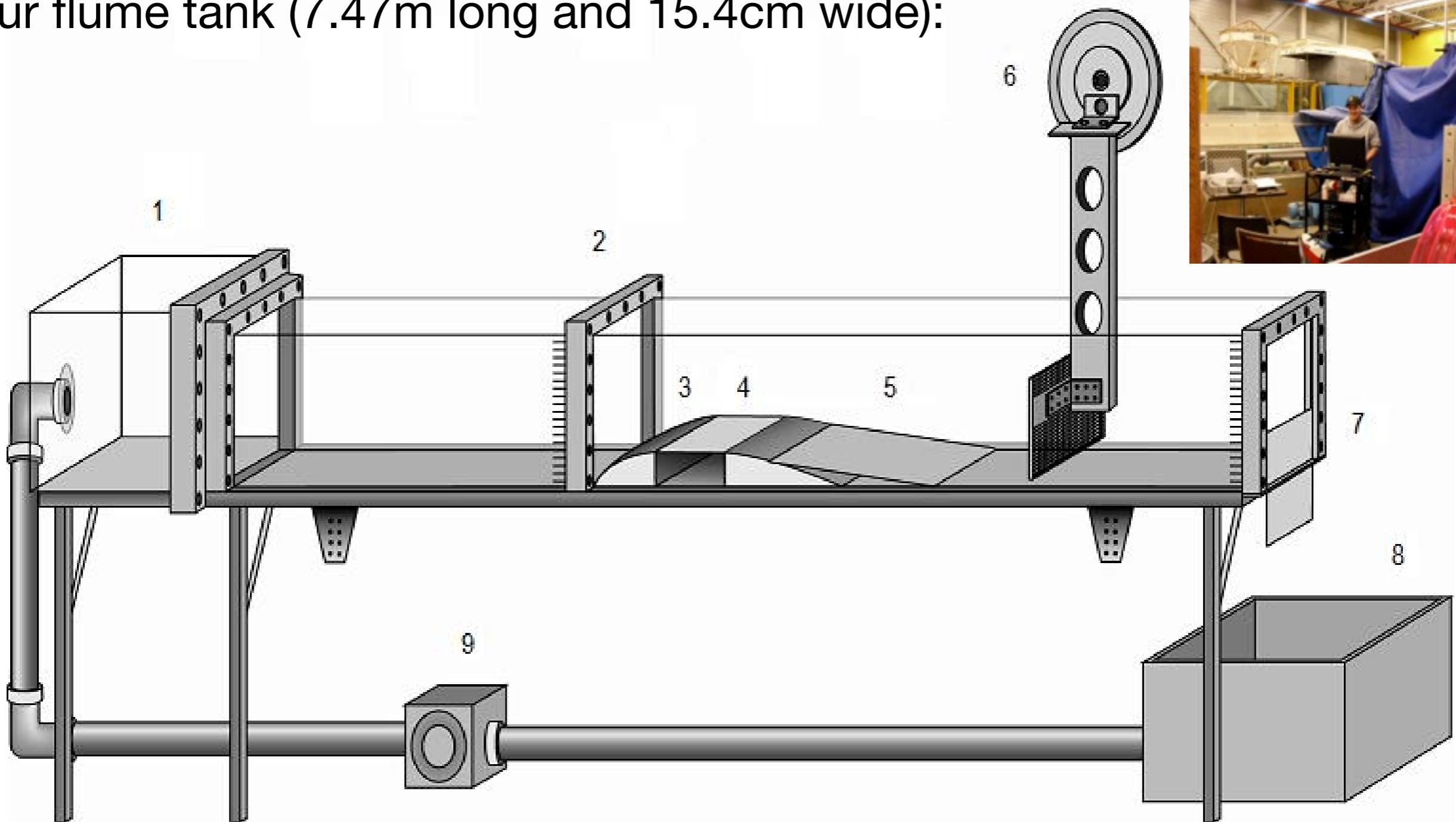
Figure 14.2 This diagram illustrates the basic parts of a wave as well as the movement of water particles in a wave. Negligible water movement occurs below a depth equal to one-half the wavelength.

Goal: Set up black and white horizon & detect stimulated conversion to pos. & neg. waves who's relative amplitudes obey Hawking's formula.

Our experiment ➤ Setup

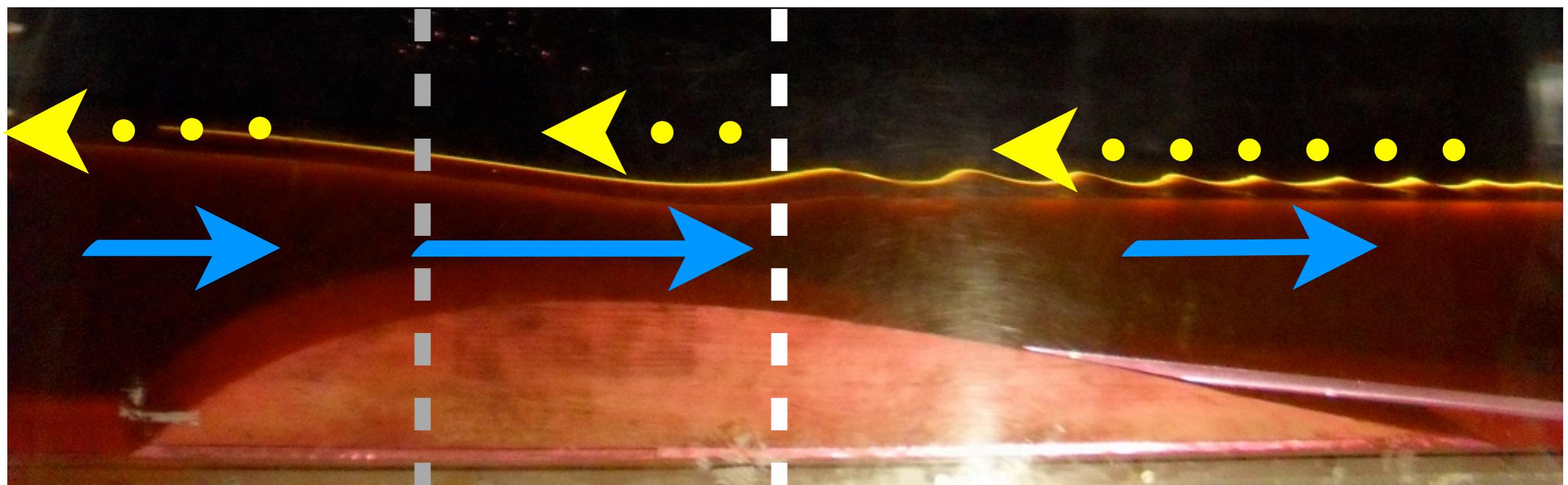


Our flume tank (7.47m long and 15.4cm wide):



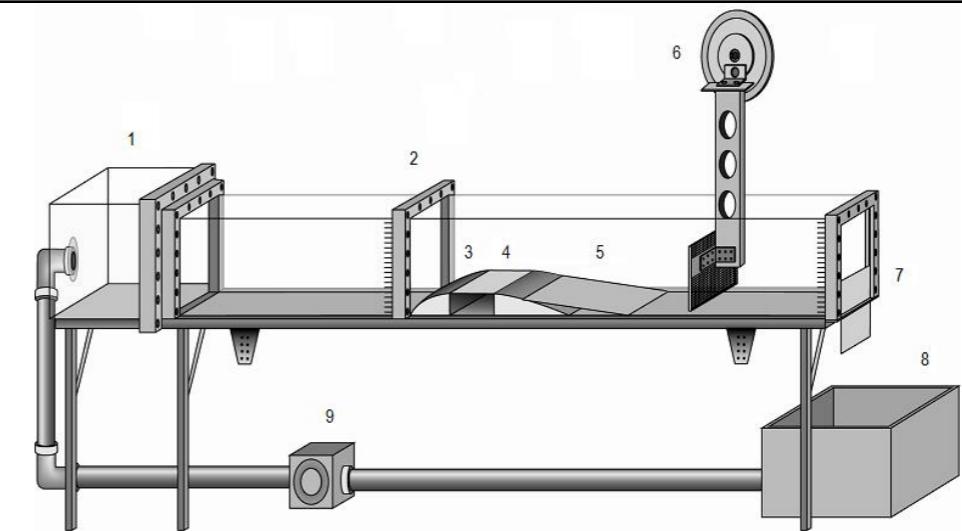
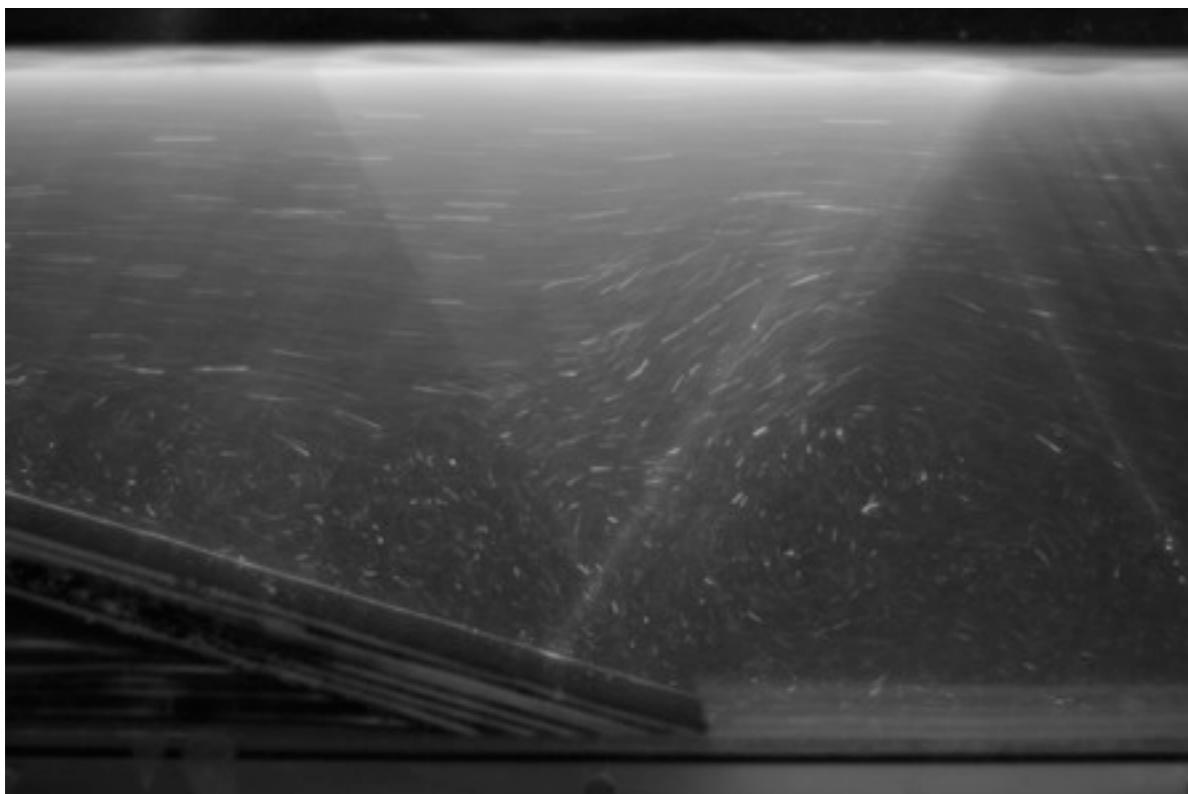
Our experiment ➤ Black & White hole horizons

effective
white hole

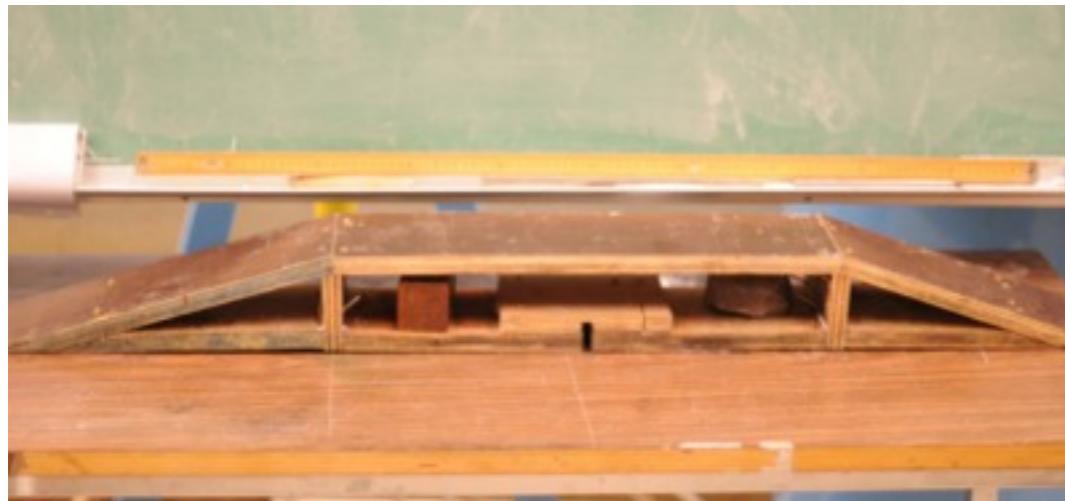


effective
black hole

Our experiment ➤ The design of our obstacle



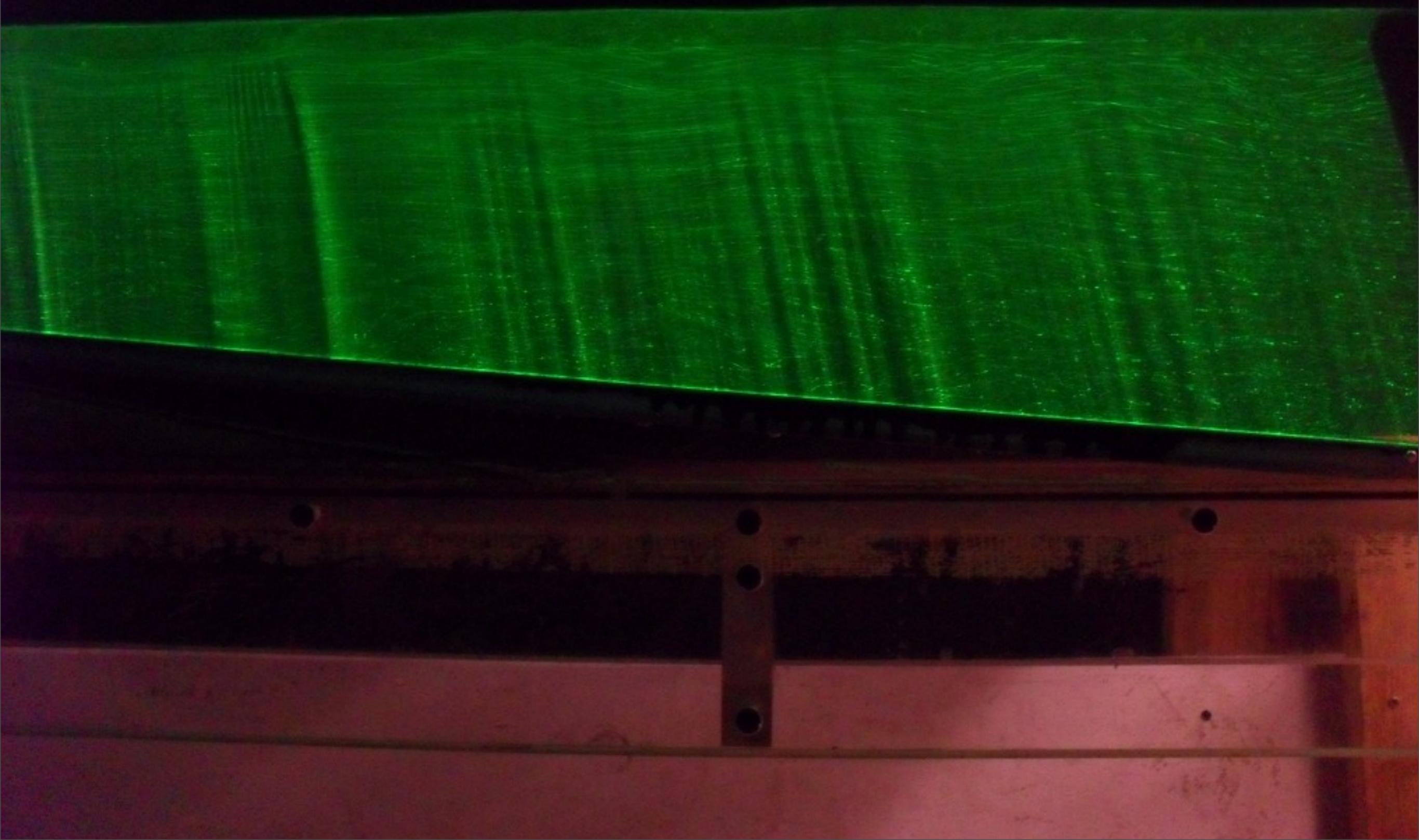
Initial design for our experiment



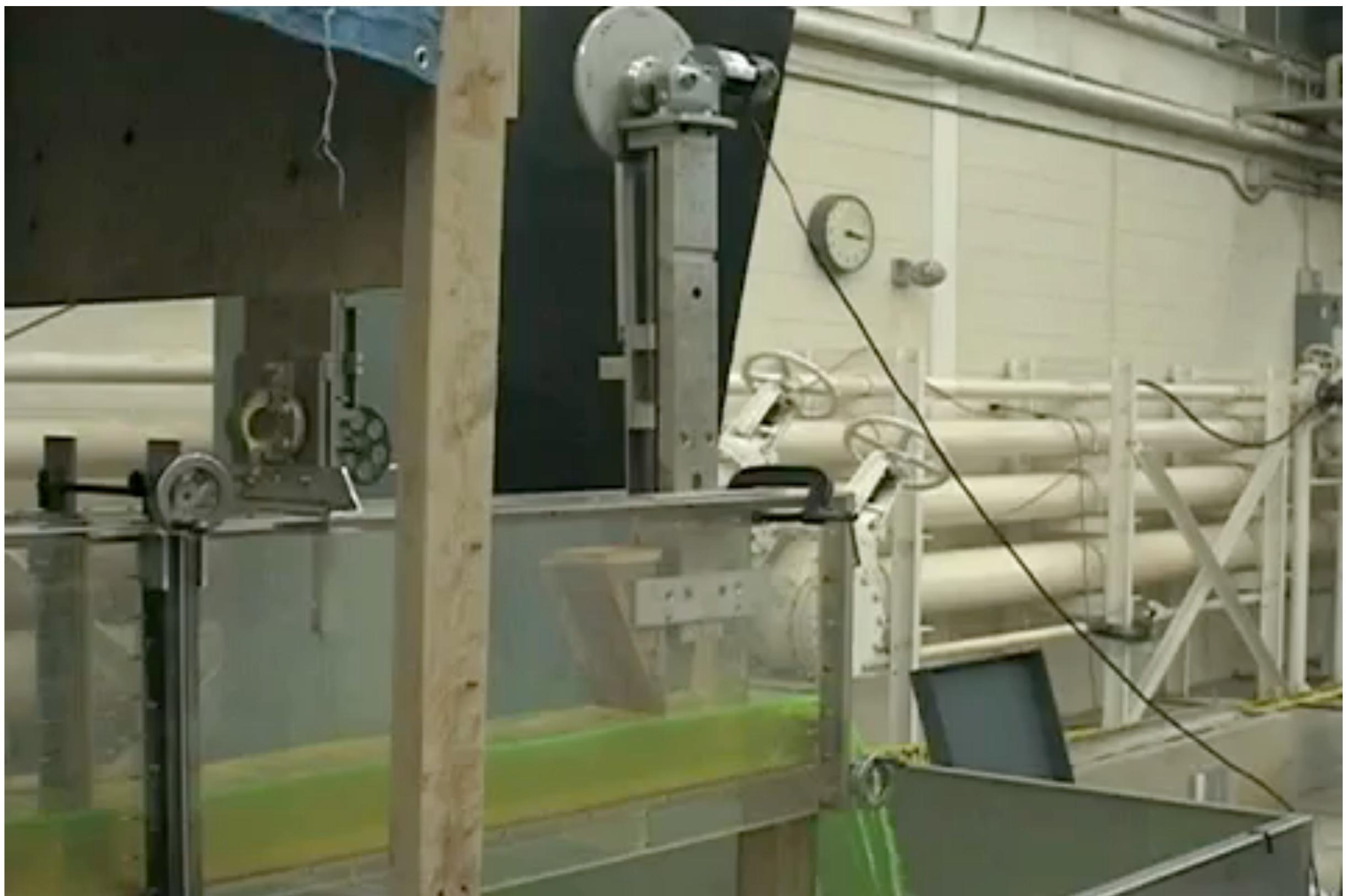
Down-scaled version of Germain Rousseaux et al. obstacle.
[length: 14m to 1m]



Our experiment ➤ The design of our obstacle



Our experiment ➤ early experiment with bigger waves



Field theory ➤ physics of surface waves

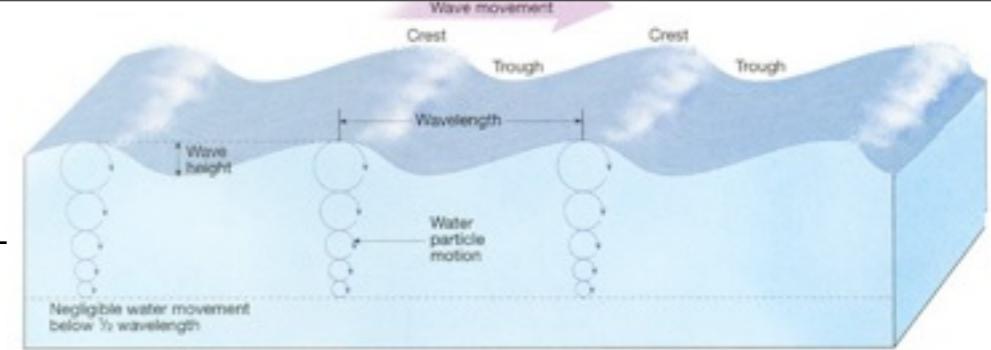
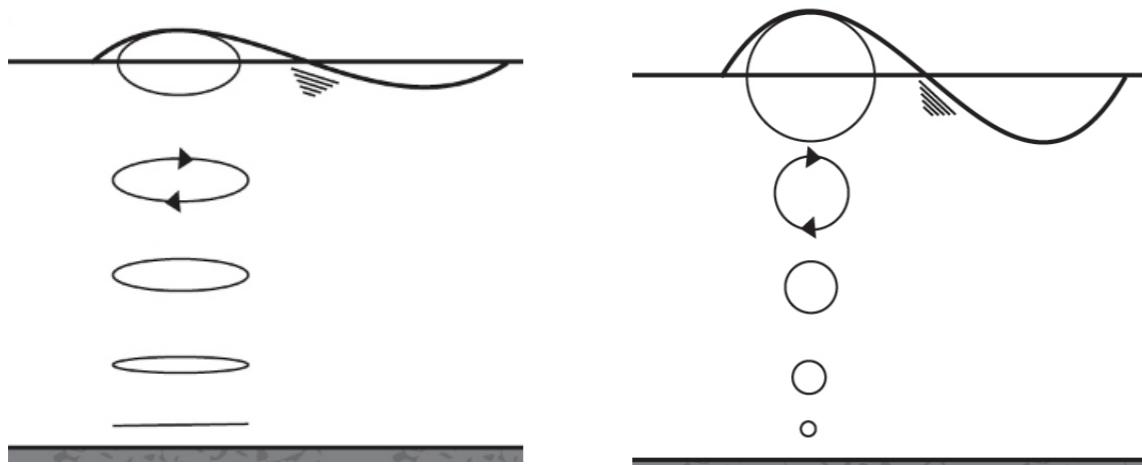


Figure 14.2 This diagram illustrates the basic parts of a wave as well as the movement of water particles with the passage of the wave. Negligible water movement occurs below a depth equal to one-half the wavelength (the level of the dashed line).

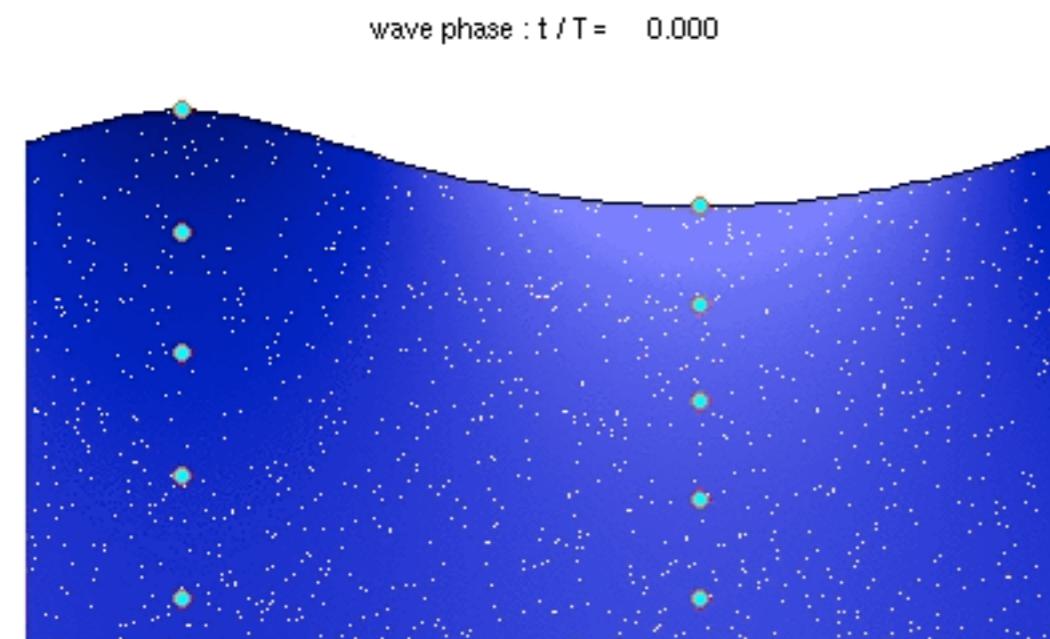


$$\Omega^2 = \left(g k + \frac{\sigma}{\rho} k^3 \right) \tanh(k h)$$

$$\omega_0 = \pm \Omega_x (\pm k), \text{ where } v_0 = 0$$

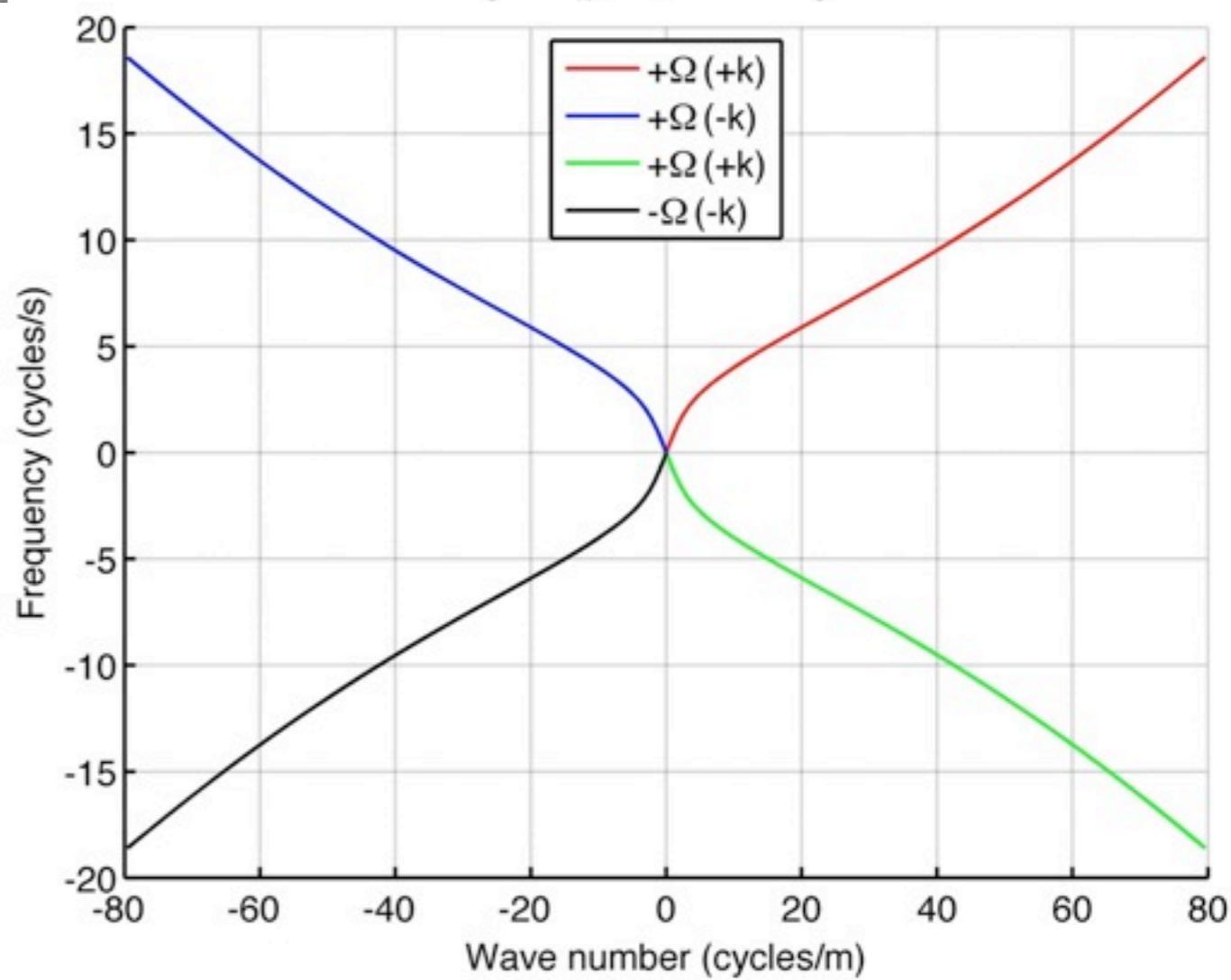
shallow:

$$\Omega = \sqrt{gh} k$$

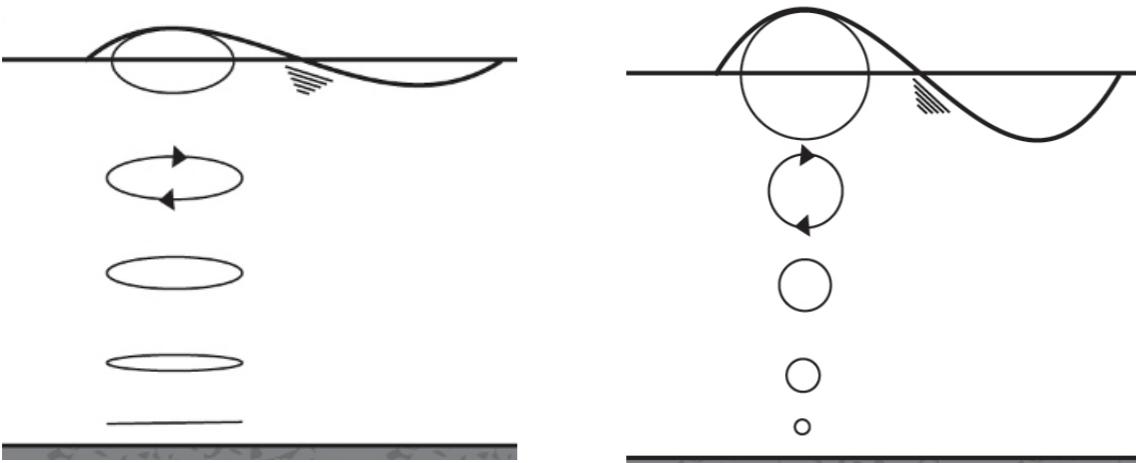
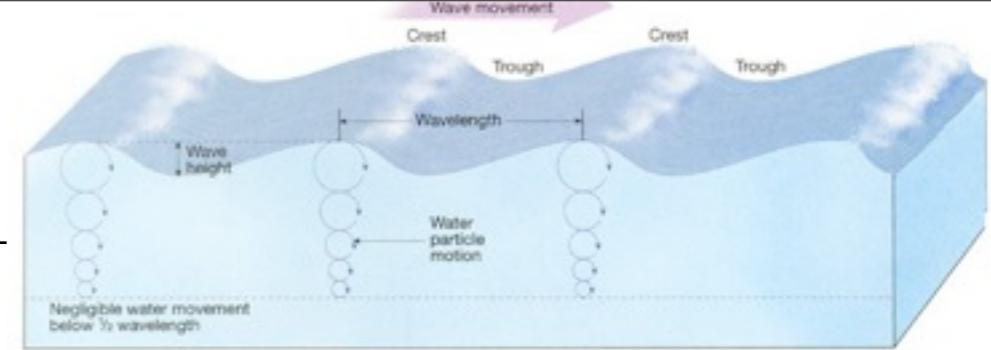


deep:

$$\Omega = \sqrt{gk}$$



Field theory ➤ physics of surface waves

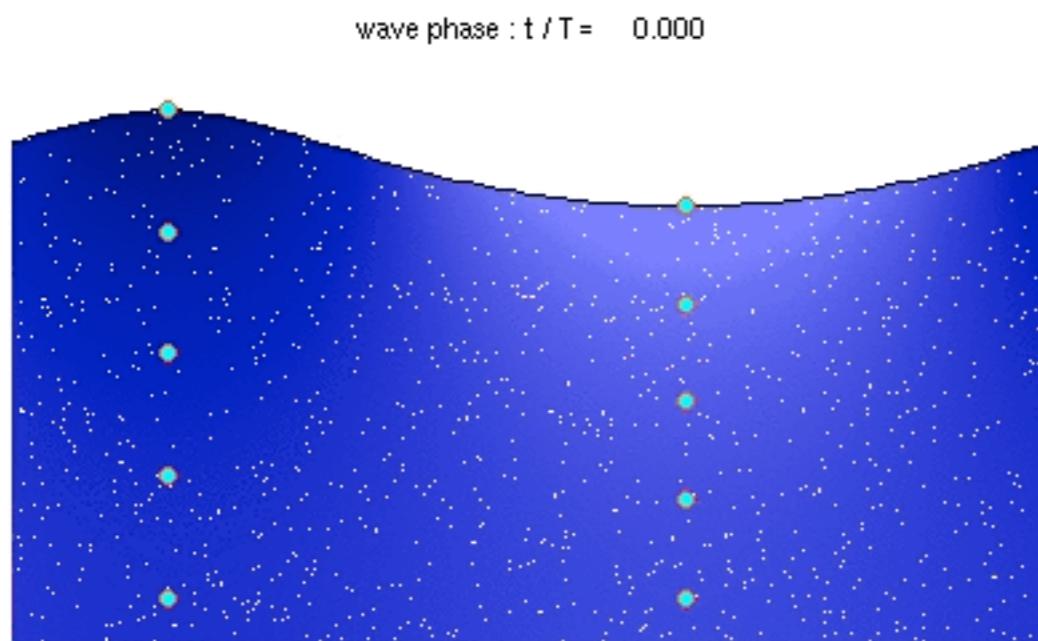


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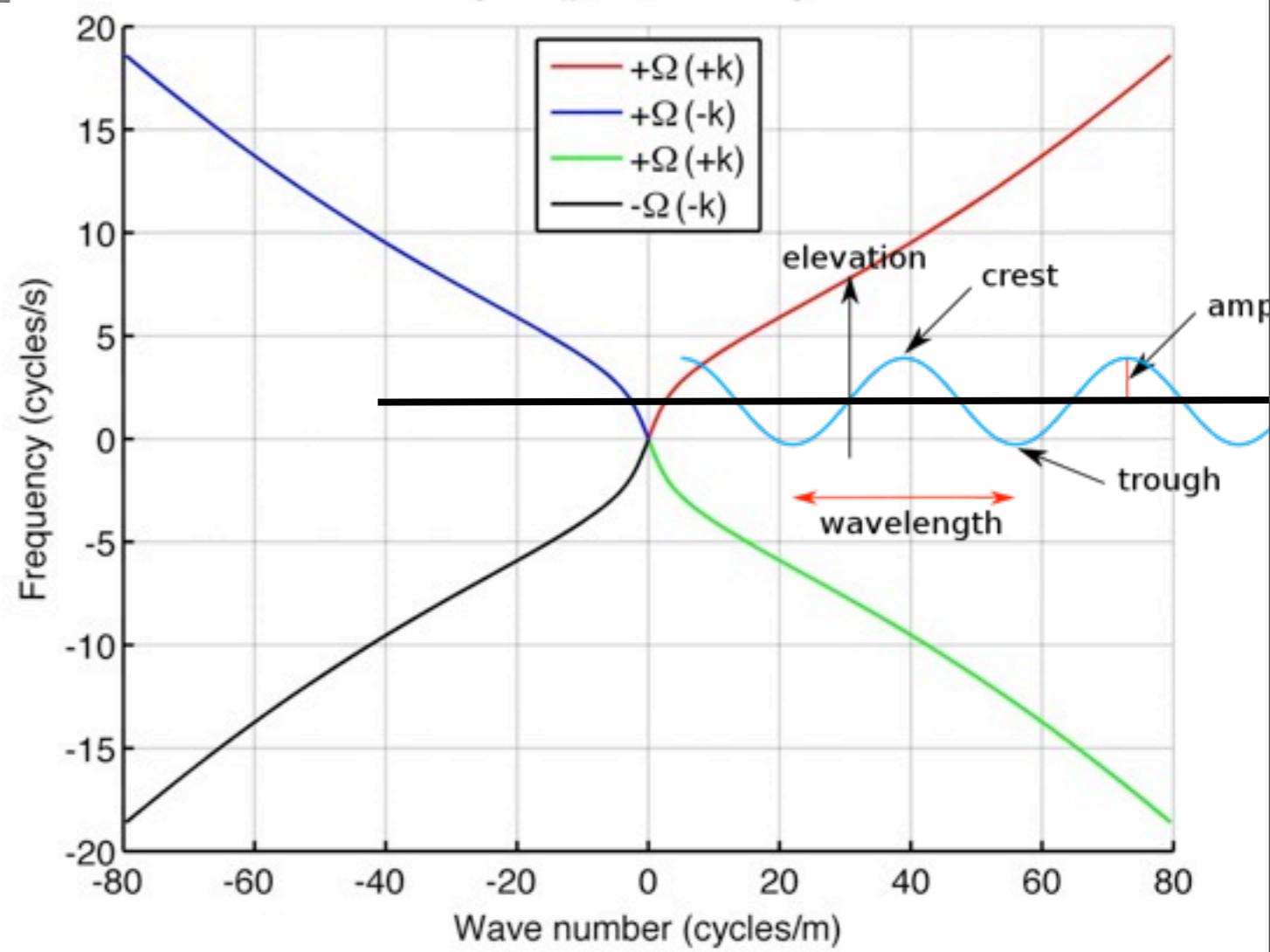
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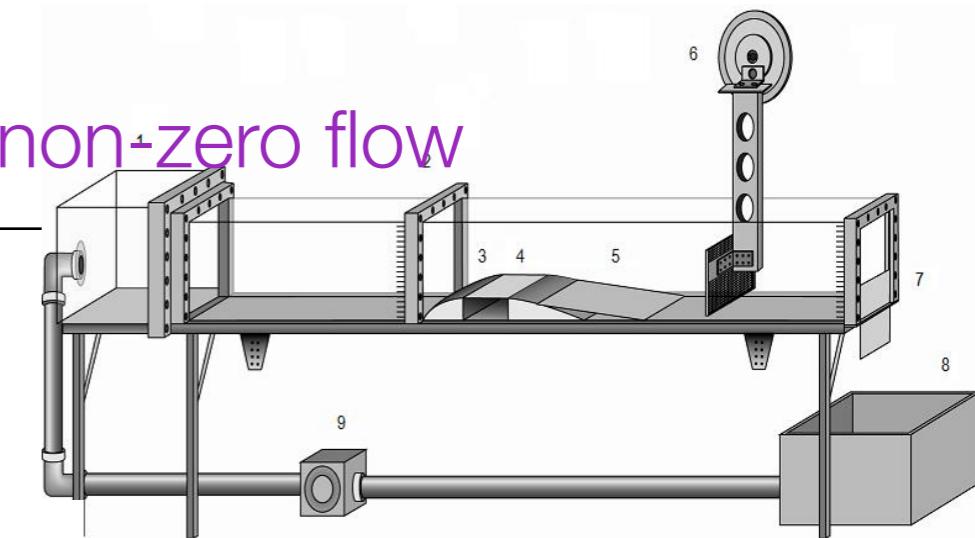


deep:

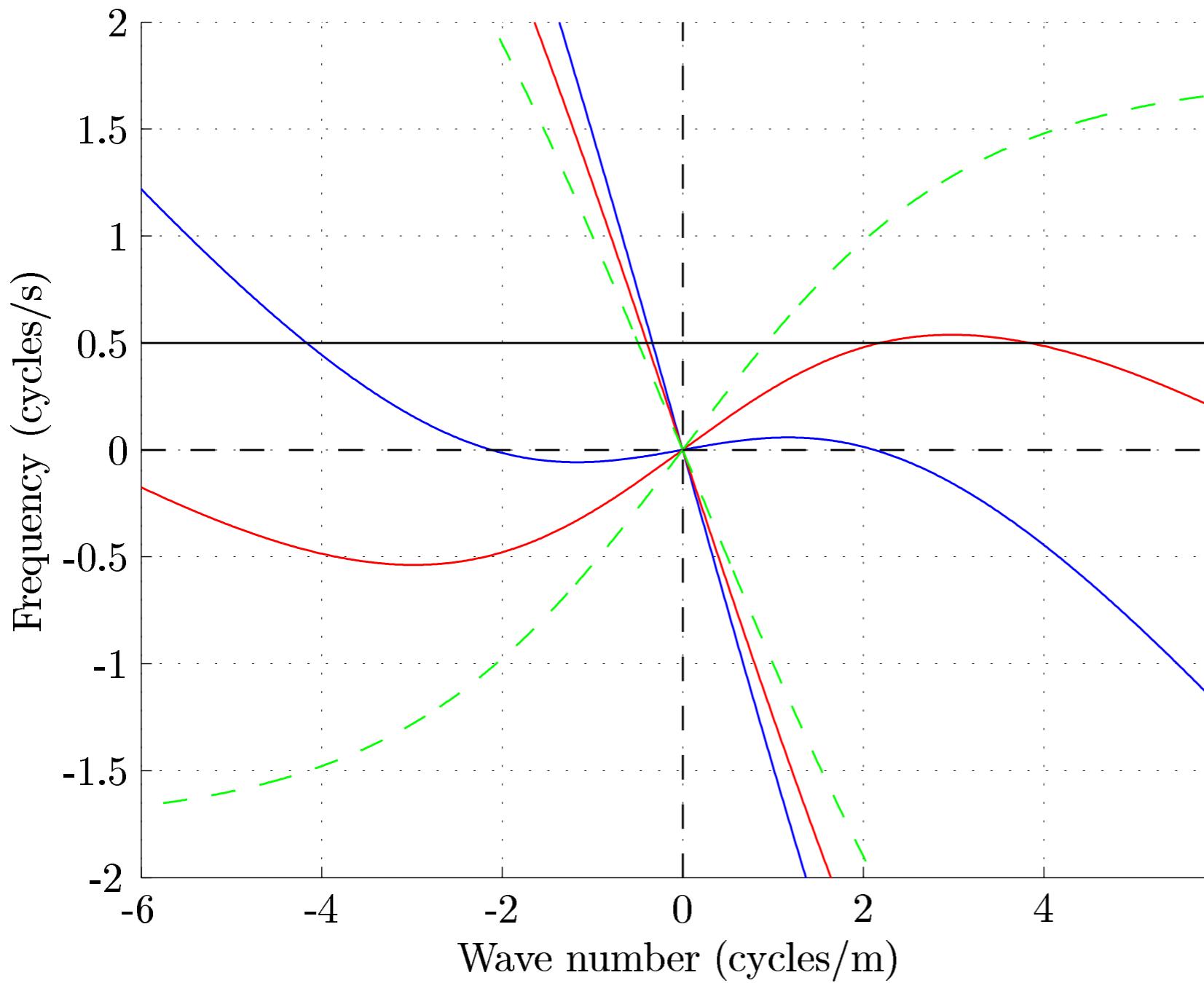
$$\Omega = \sqrt{gk}$$



Field theory ➤ physics of surface waves non-zero flow



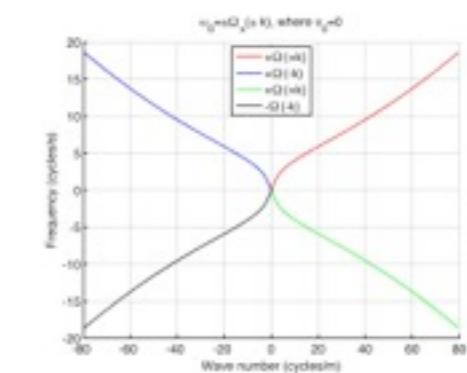
$$\Omega_{\text{LAB}} = \Omega_{\text{WATER}} \pm v k$$



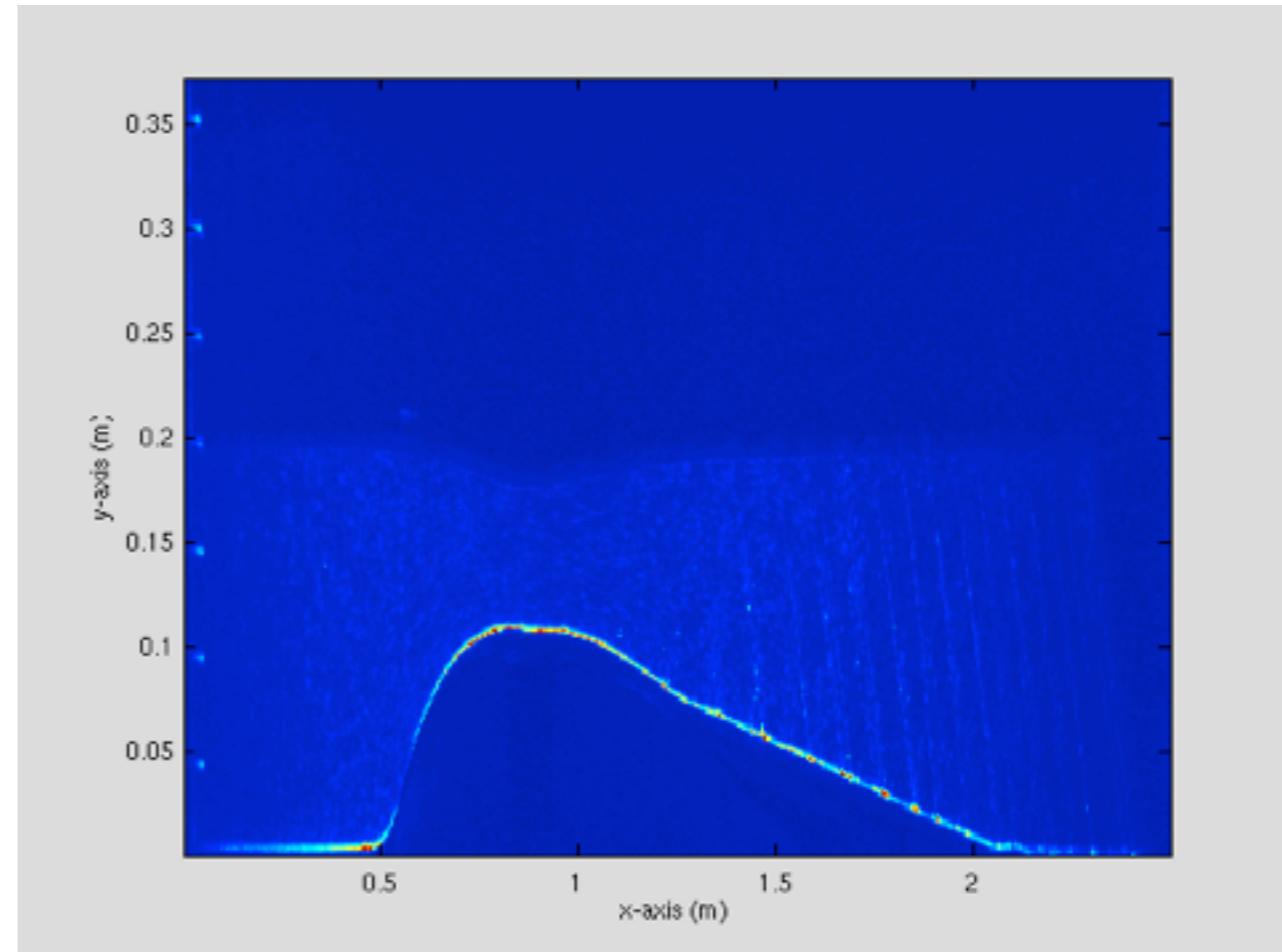
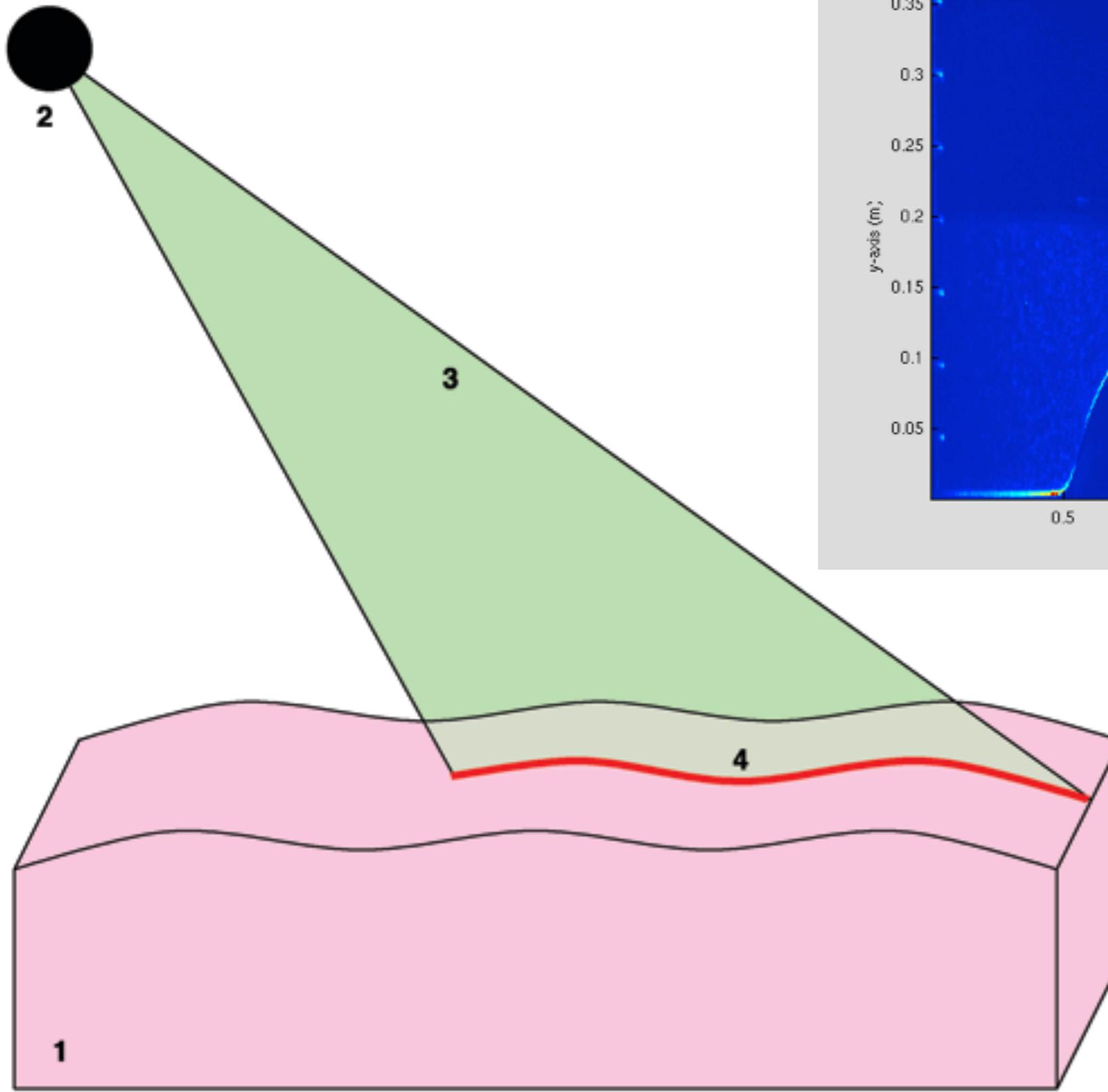
Dispersion relation for
maximum height
conversion point
minimum height

shallow: $\Omega = \sqrt{gh} k$

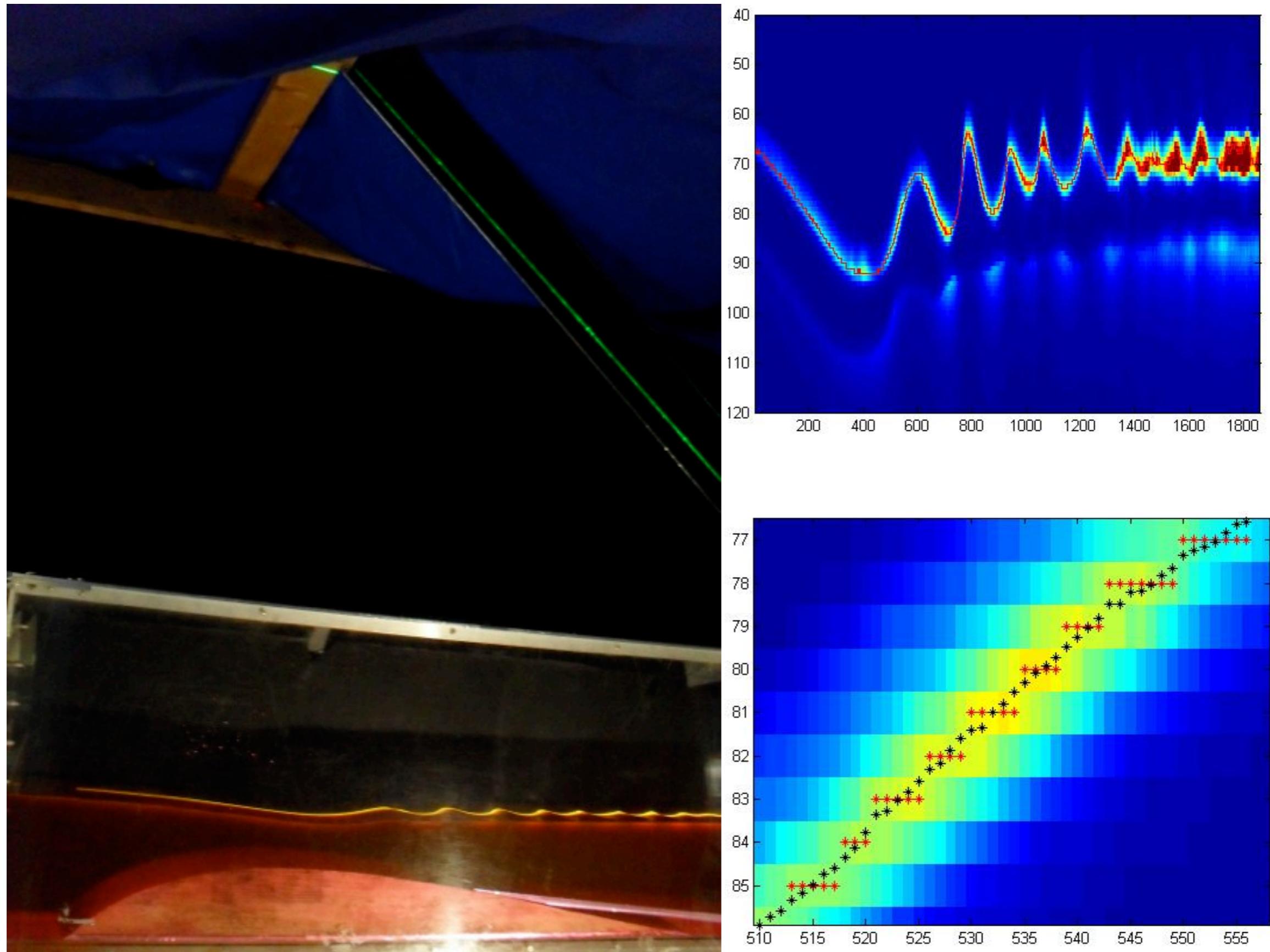
deep: $\Omega = \sqrt{gk}$

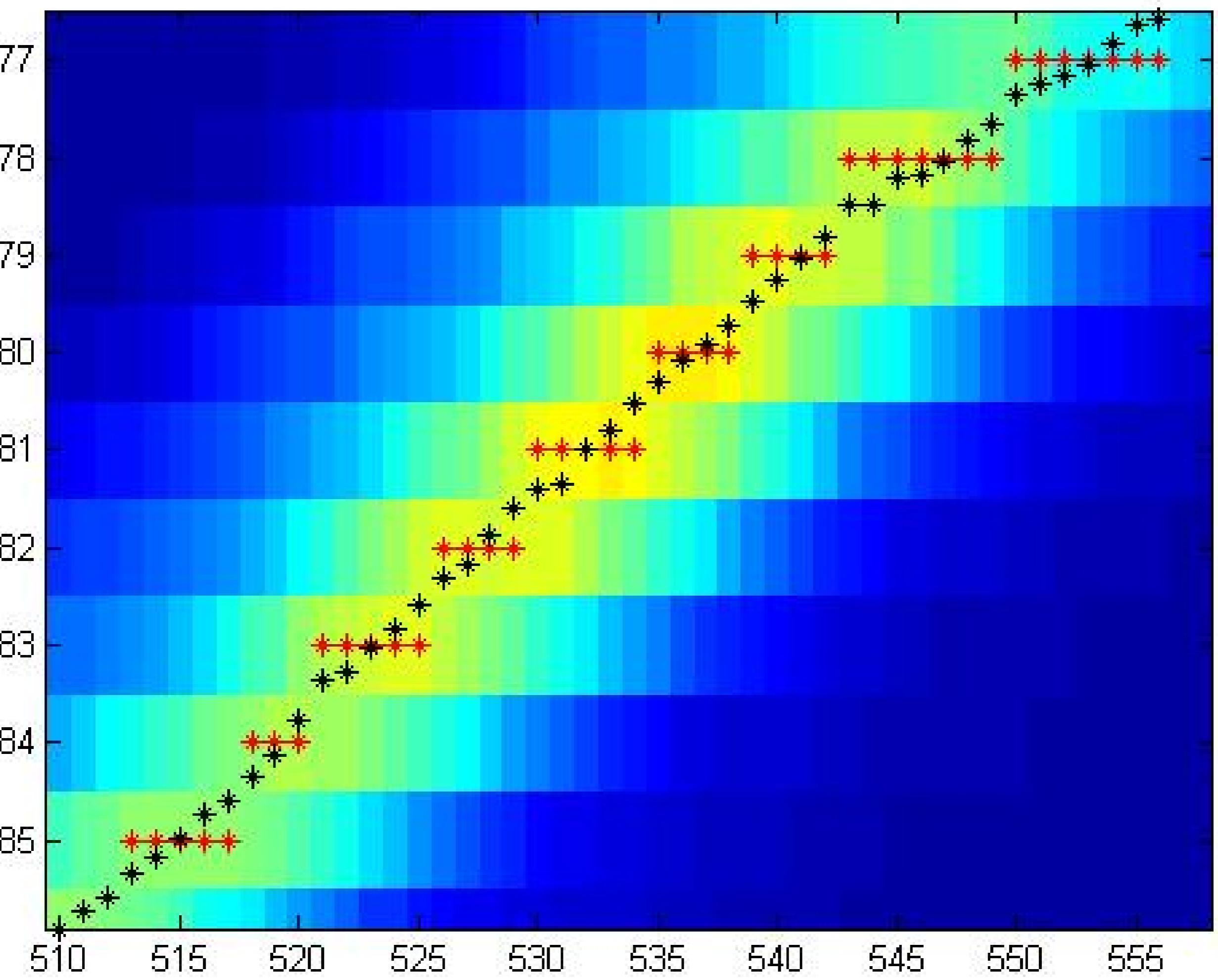


Our experiment ➤ Observable



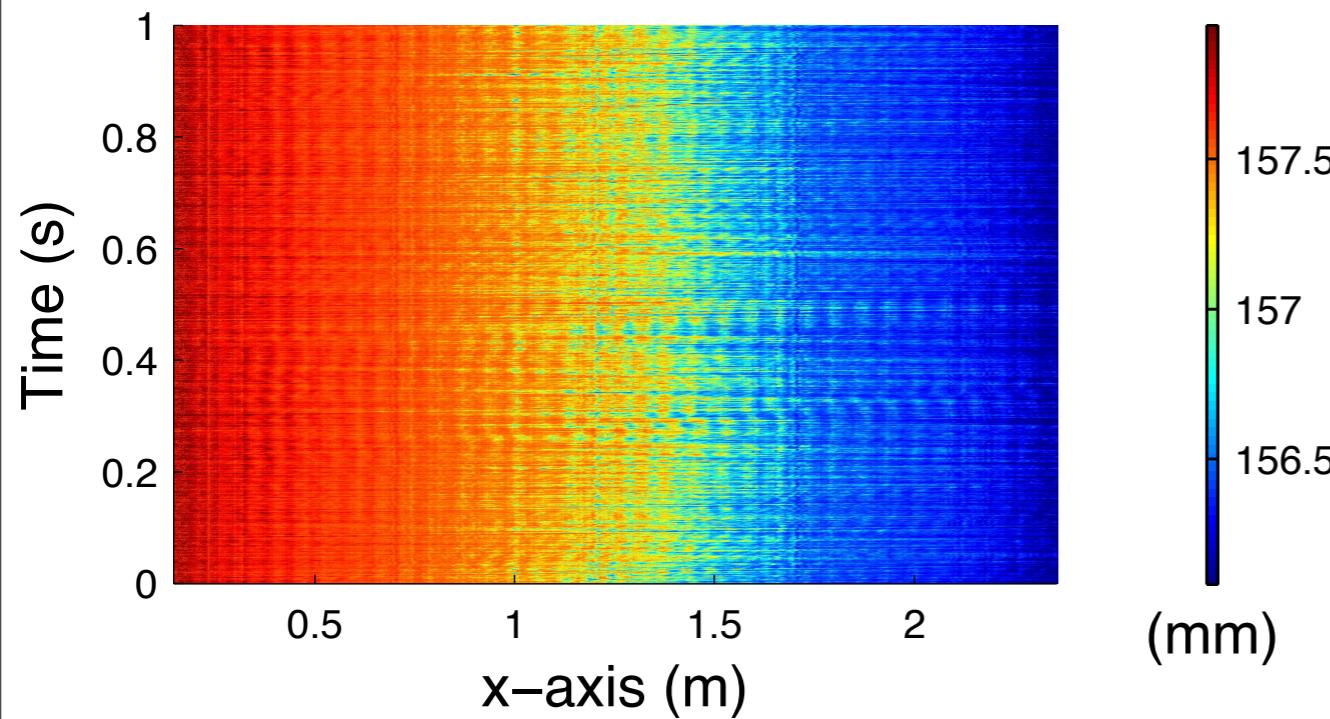
Our experiment ➤ Data analysis



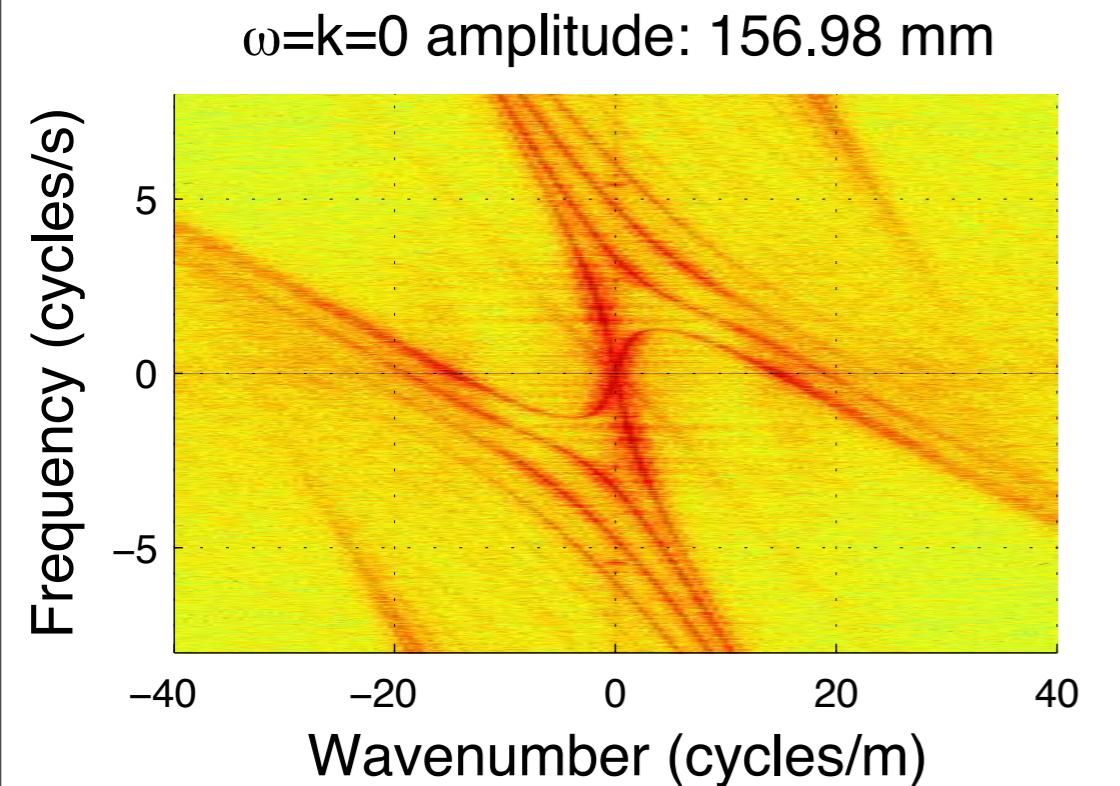


Data analysis ➤ from wave characteristic to dispersion rel.

$\omega=k=0$ amplitude: 156.98 mm



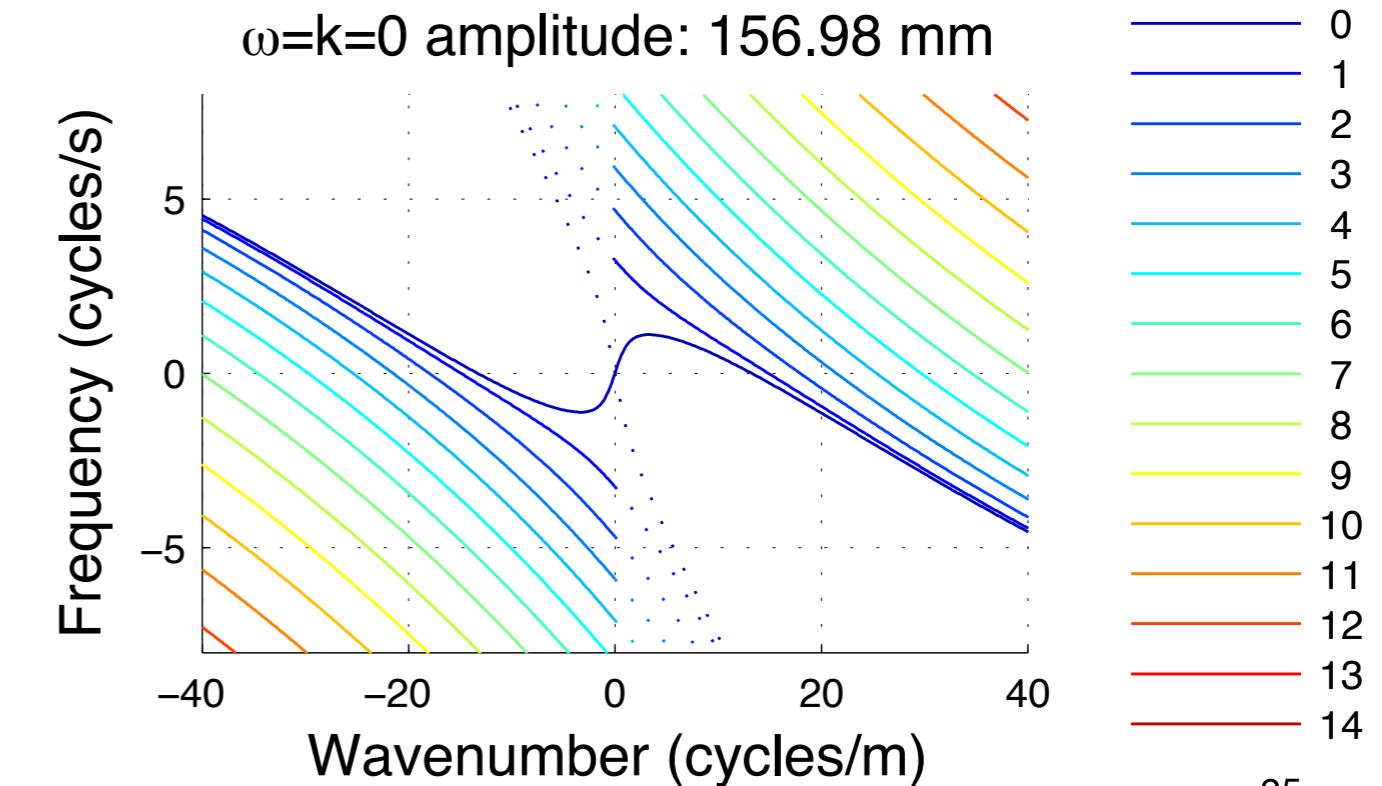
$\omega=k=0$ amplitude: 156.98 mm



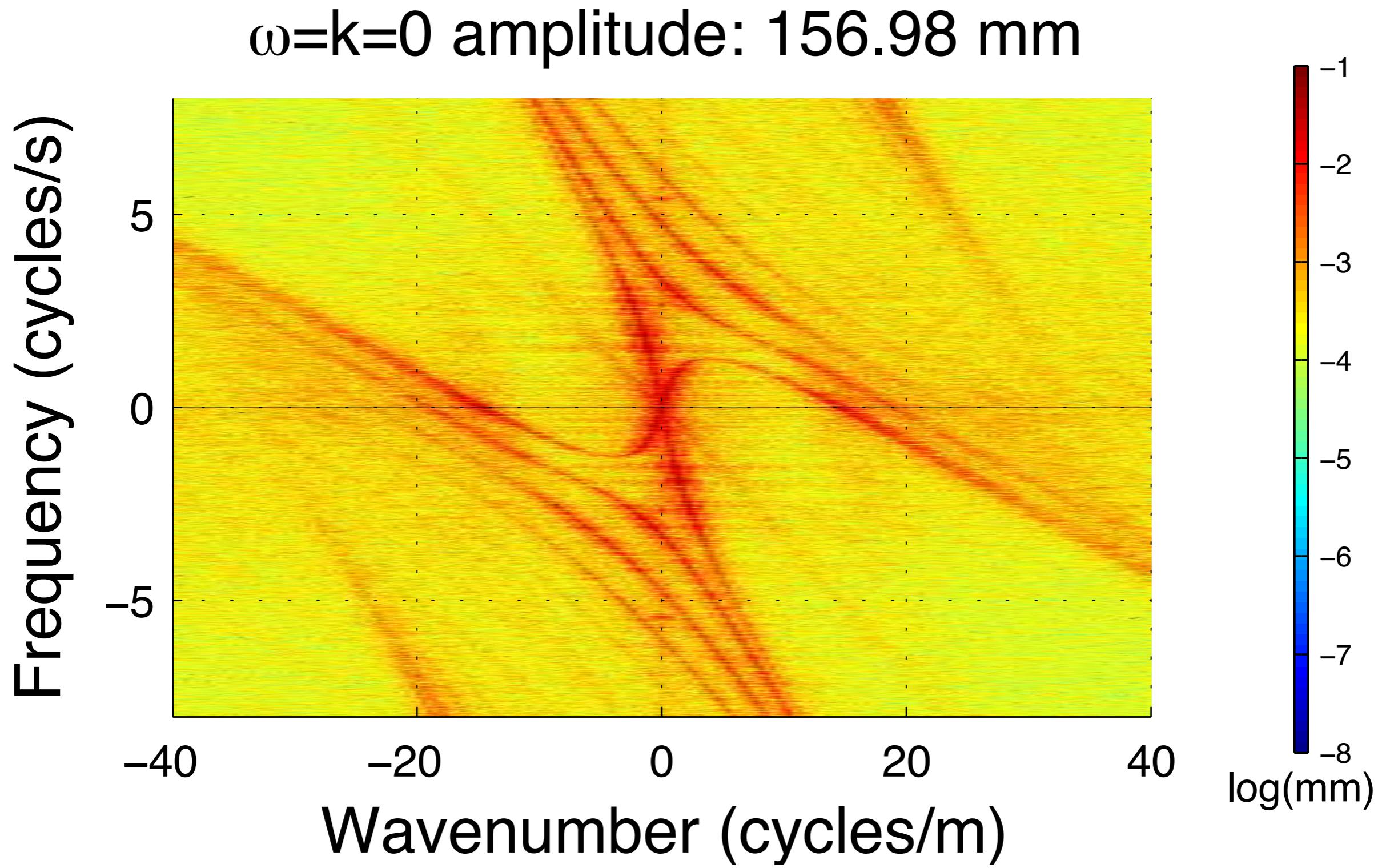
$$(f + \tilde{v} k)^2 = \left(\frac{g k}{2\pi}\right) \cdot \tanh(2\pi k h)$$

$$k = \sqrt{k_{||}^2 + k_{\perp}^2} = \sqrt{(1/\lambda)^2 + (n/l_w)^2},$$

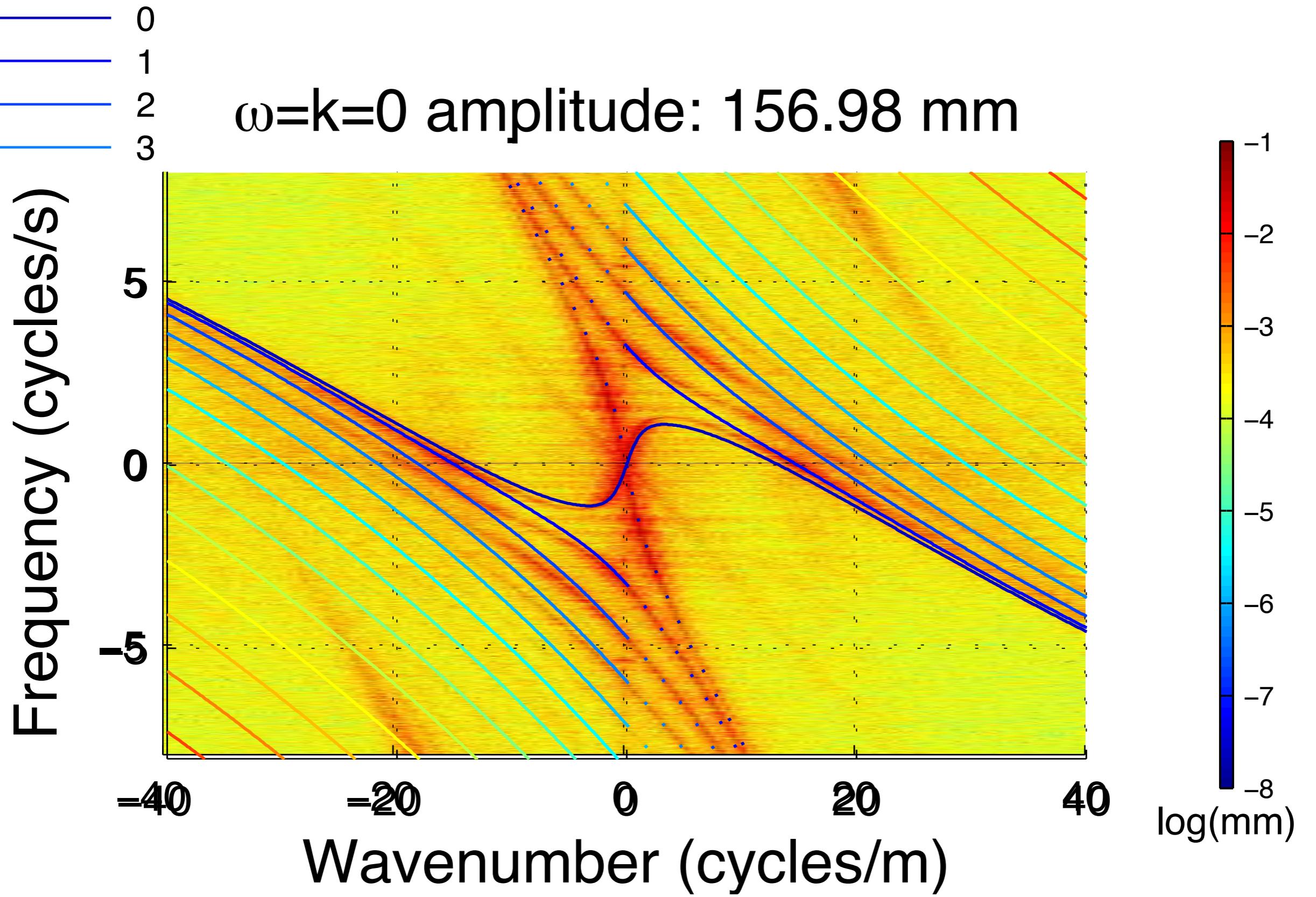
$\omega=k=0$ amplitude: 156.98 mm



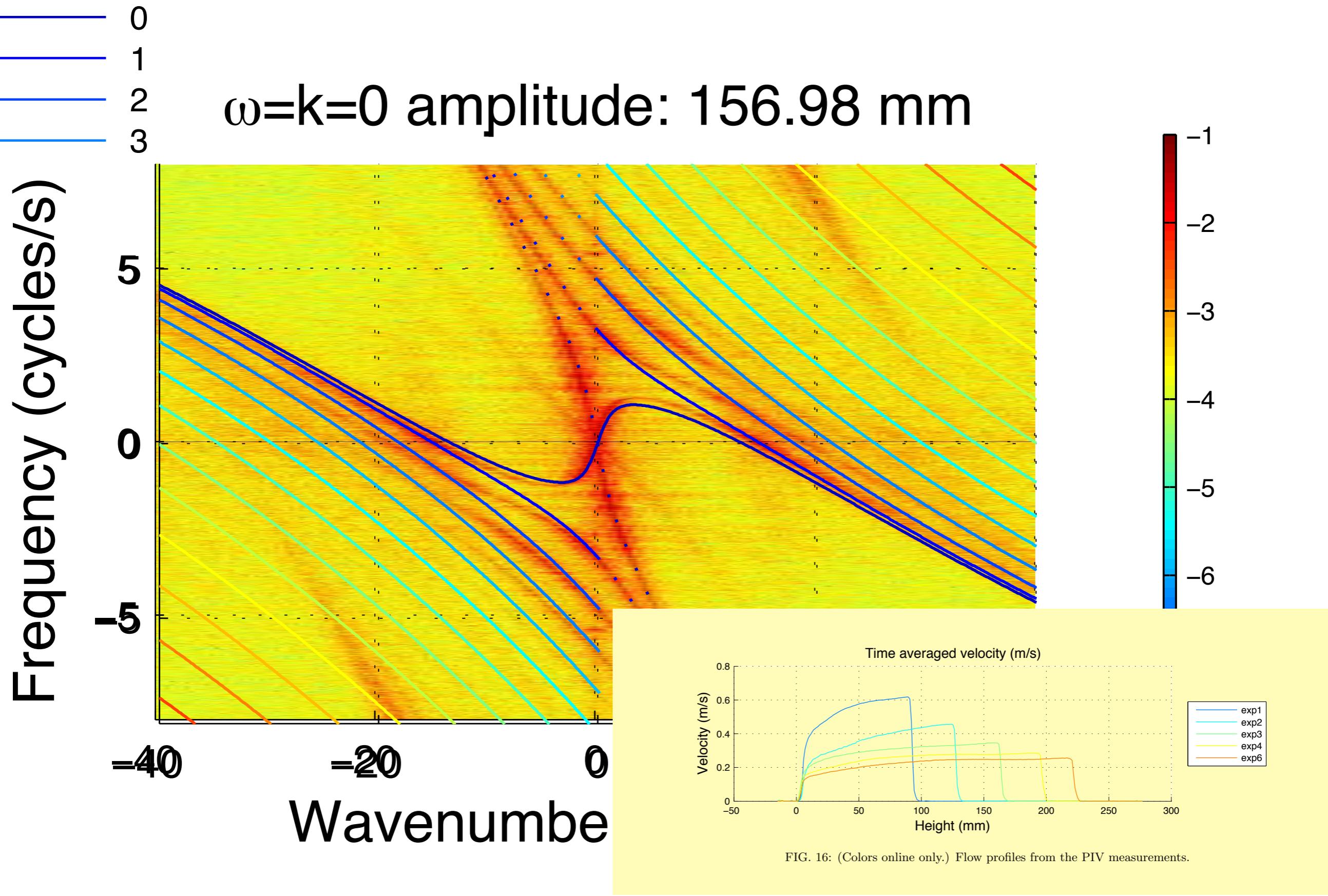
Data analysis ➤ from wave characteristic to dispersion rel.



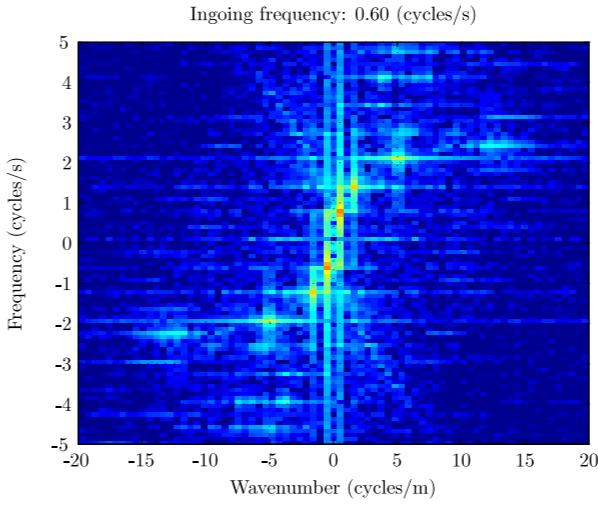
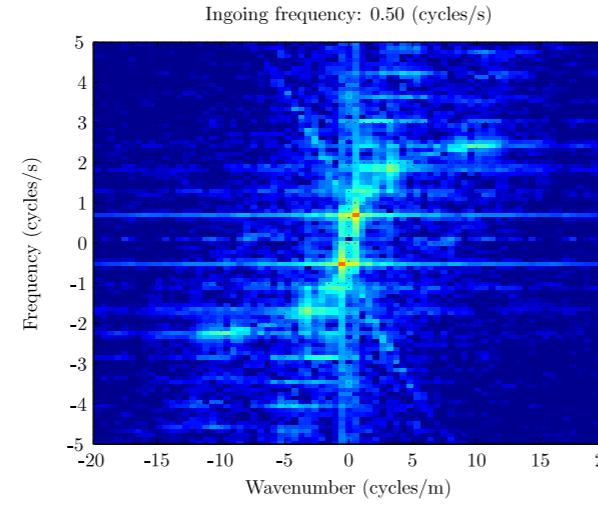
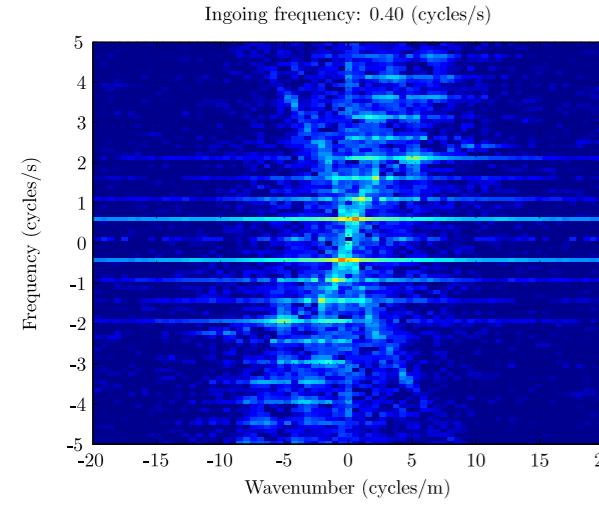
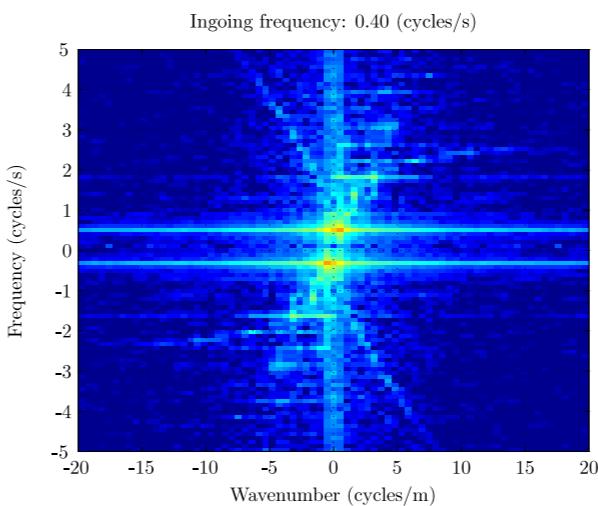
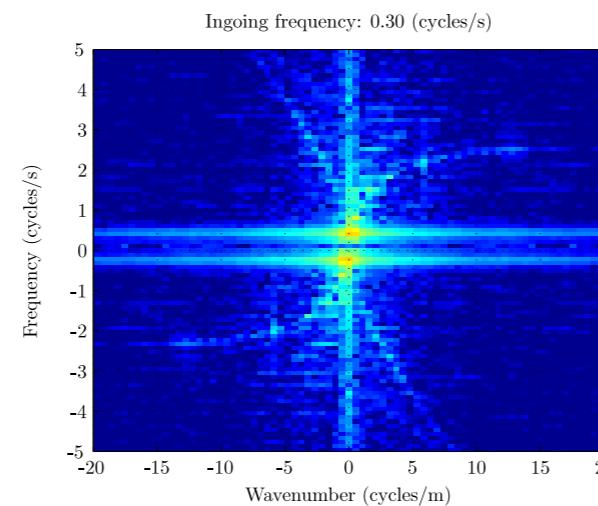
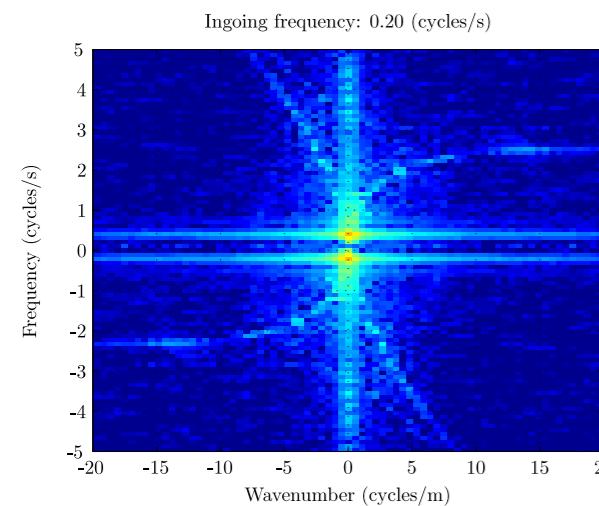
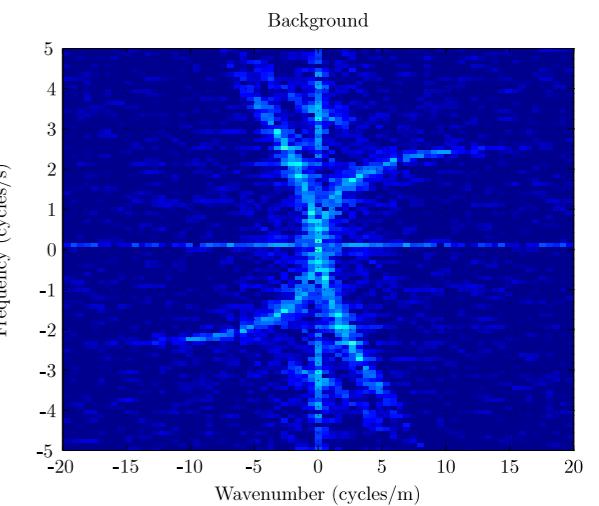
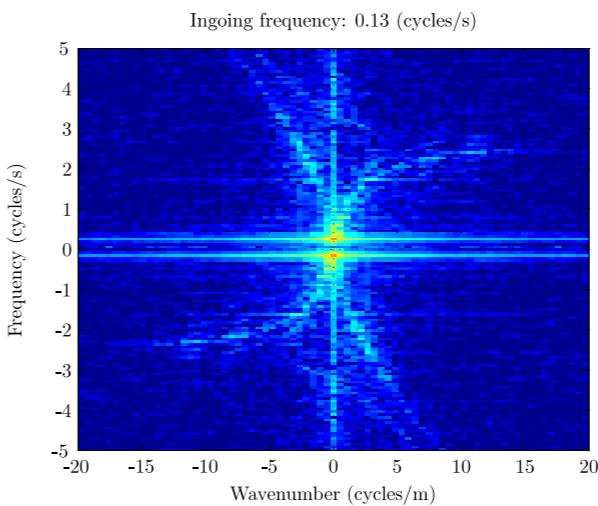
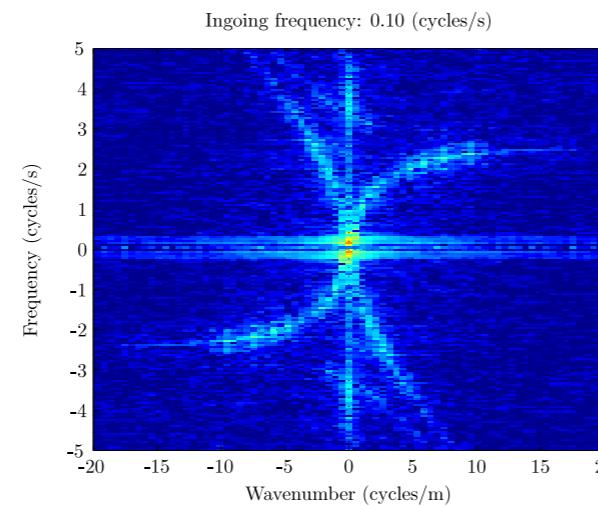
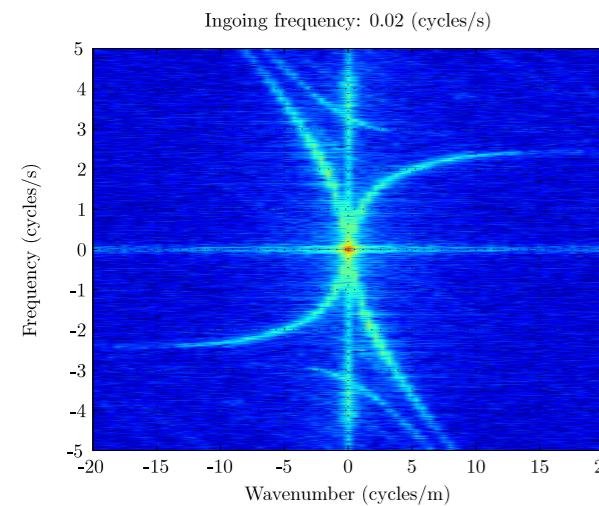
Data analysis ➤ from wave characteristic to dispersion rel.



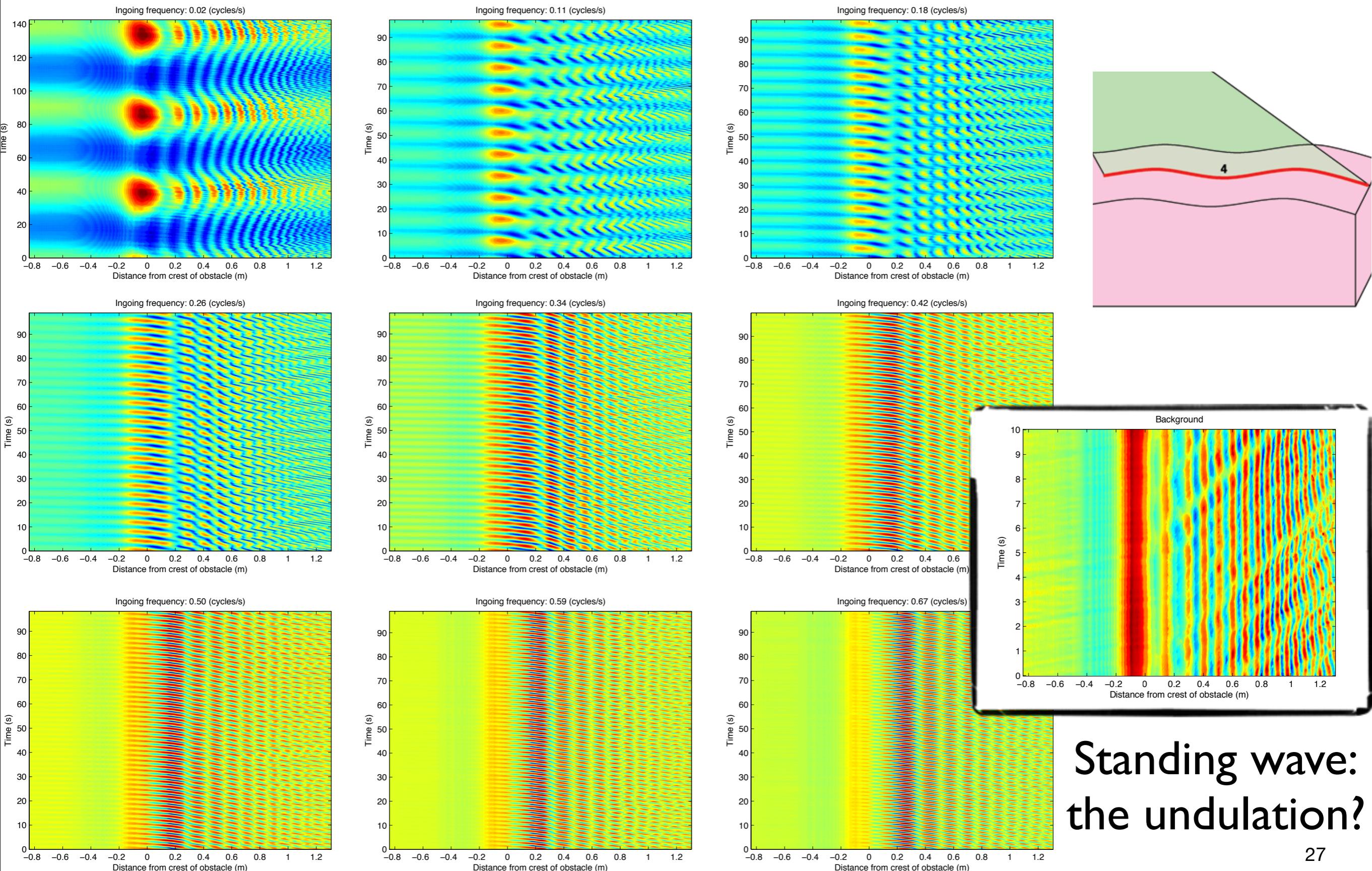
Data analysis ➤ from wave characteristic to dispersion rel.



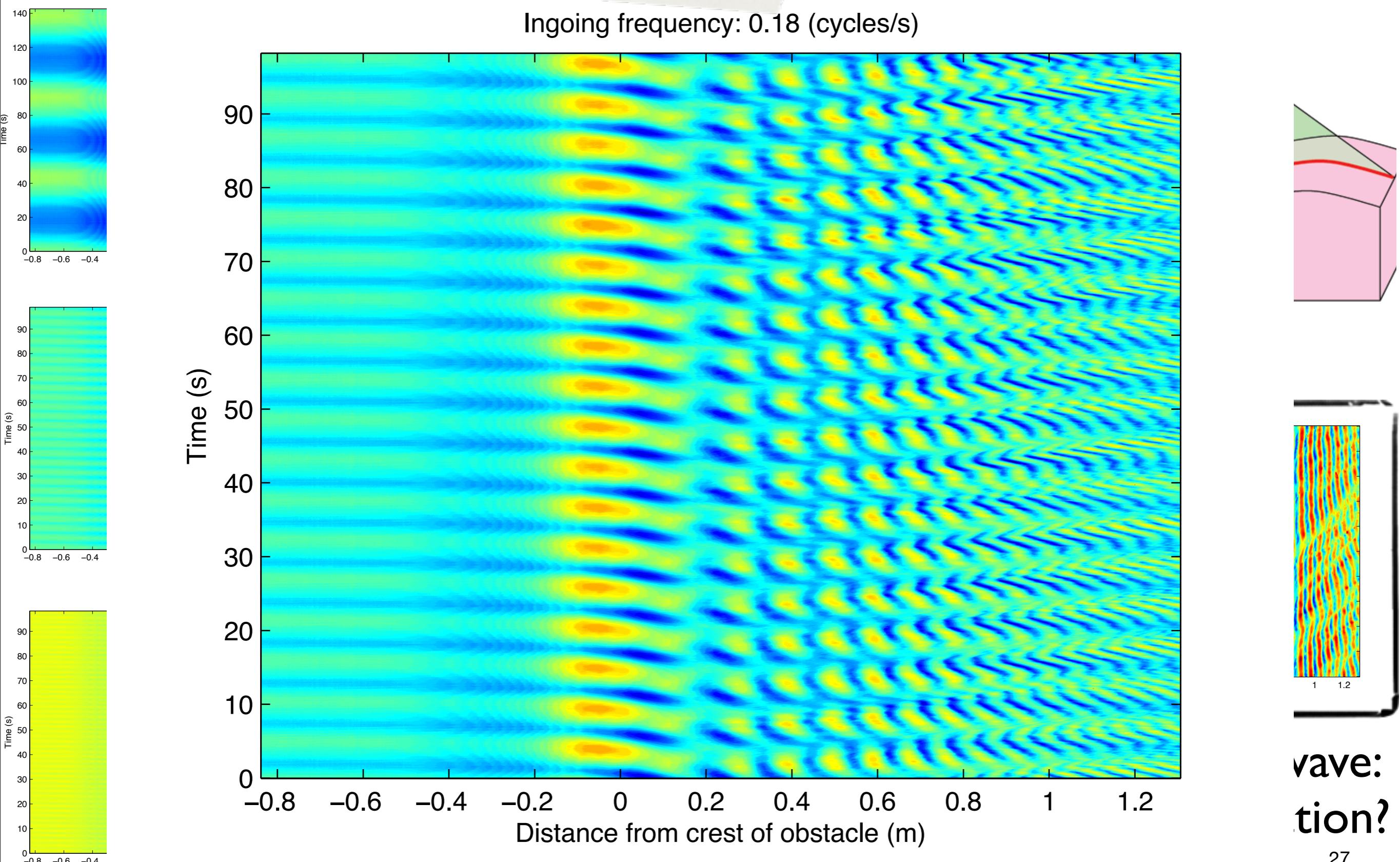
Our experiment ➤ Exciting classical field modes



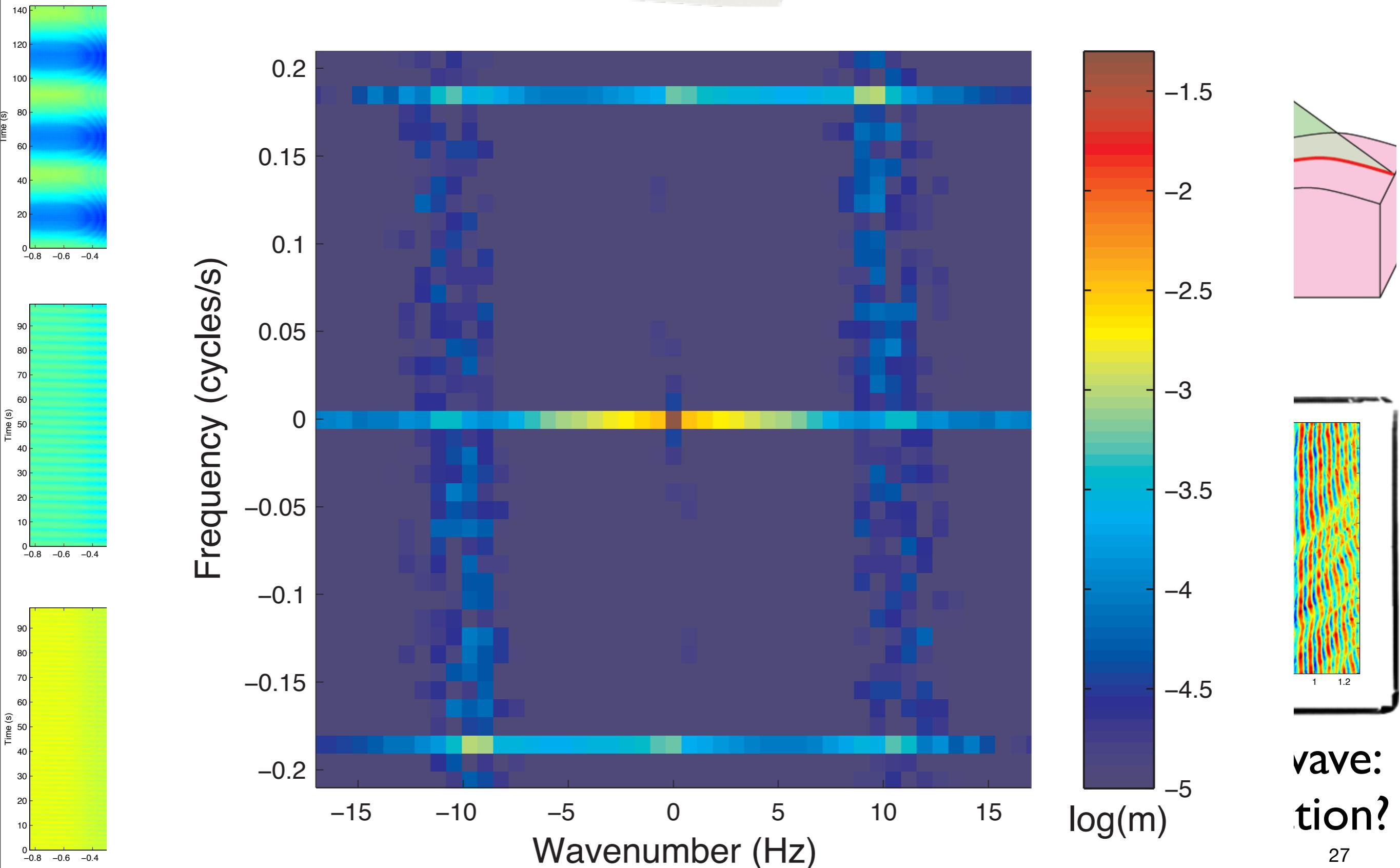
Our experiment ➤ Experimental procedure



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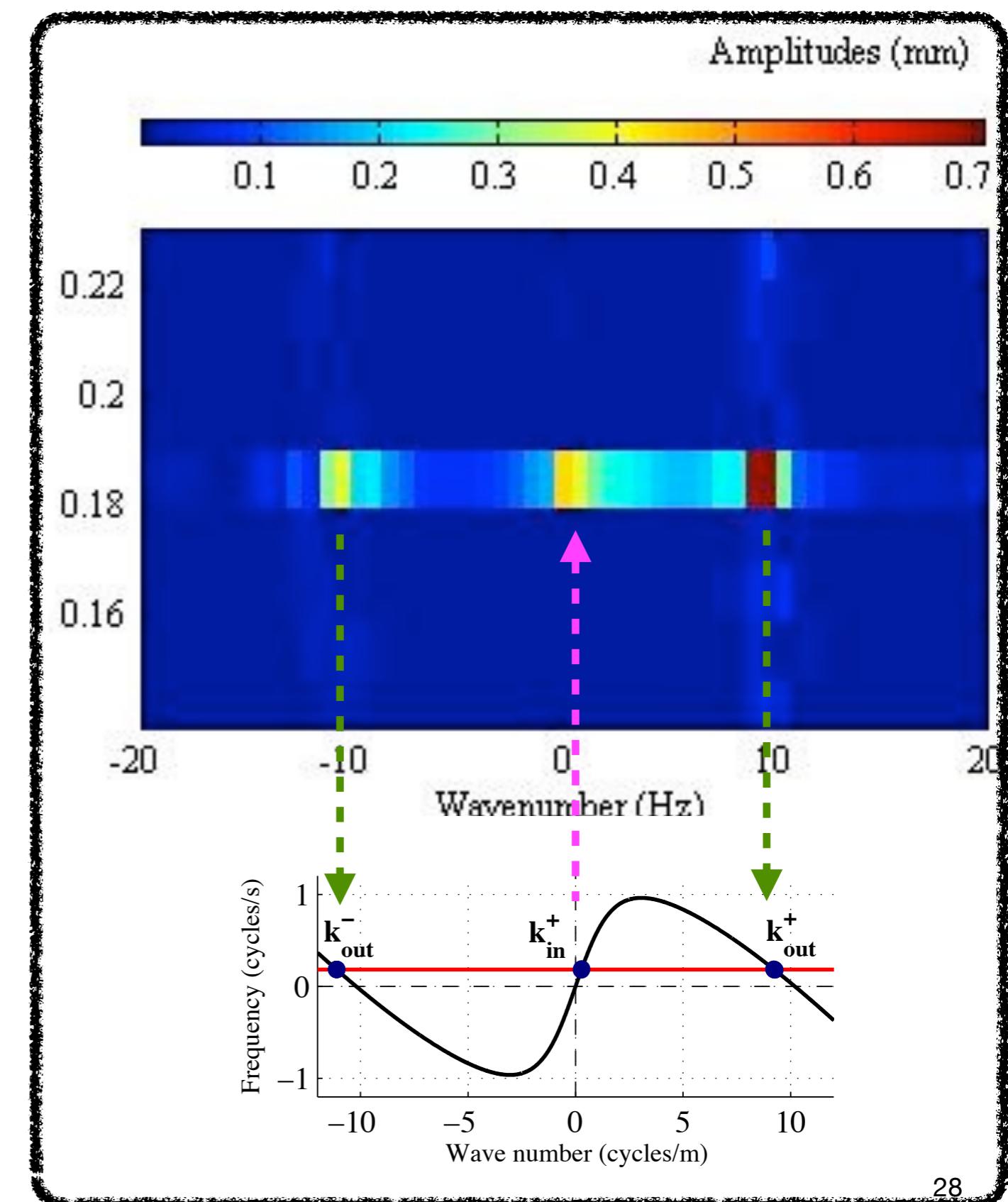
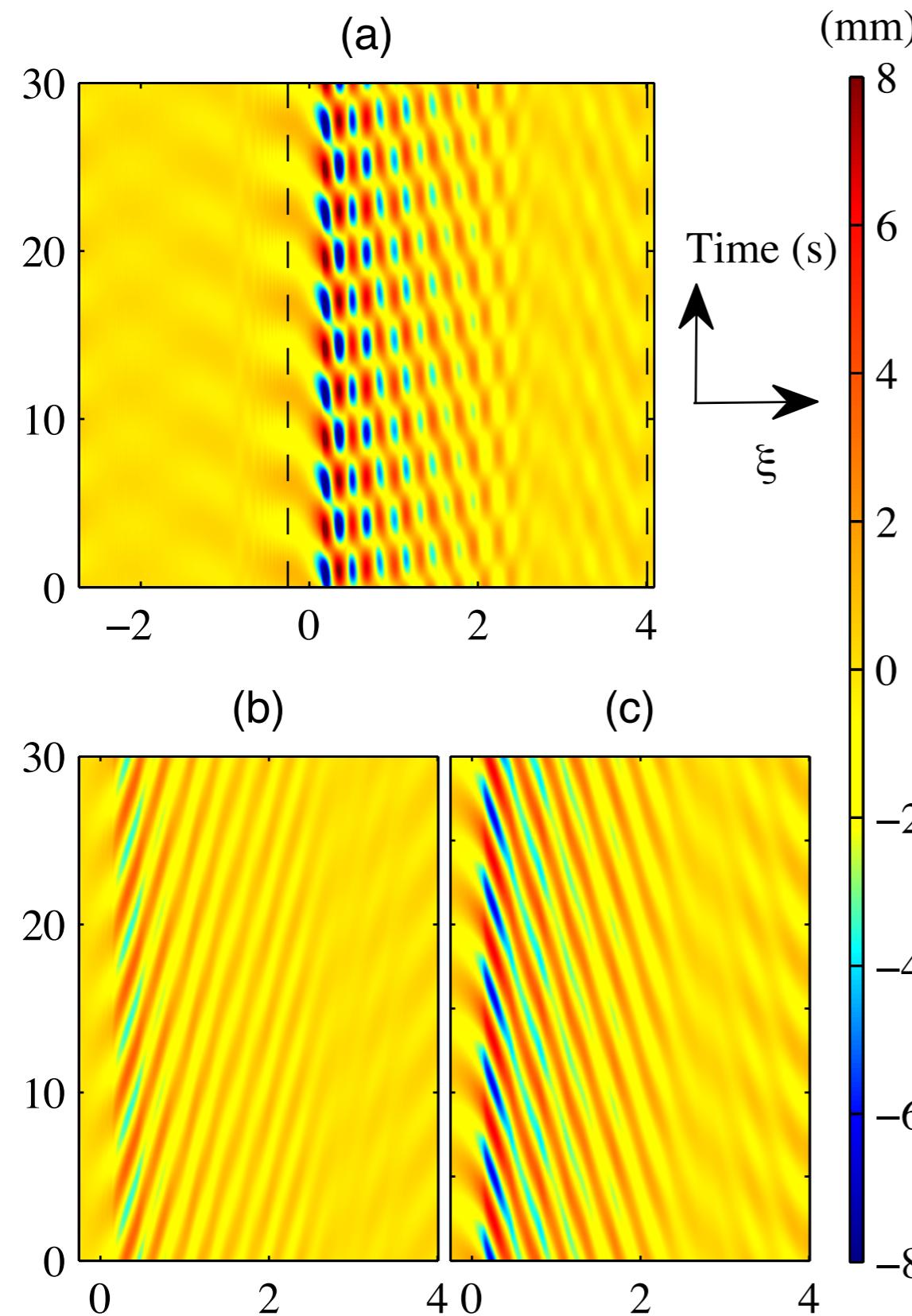


Our experiment ➤ Experimental procedure

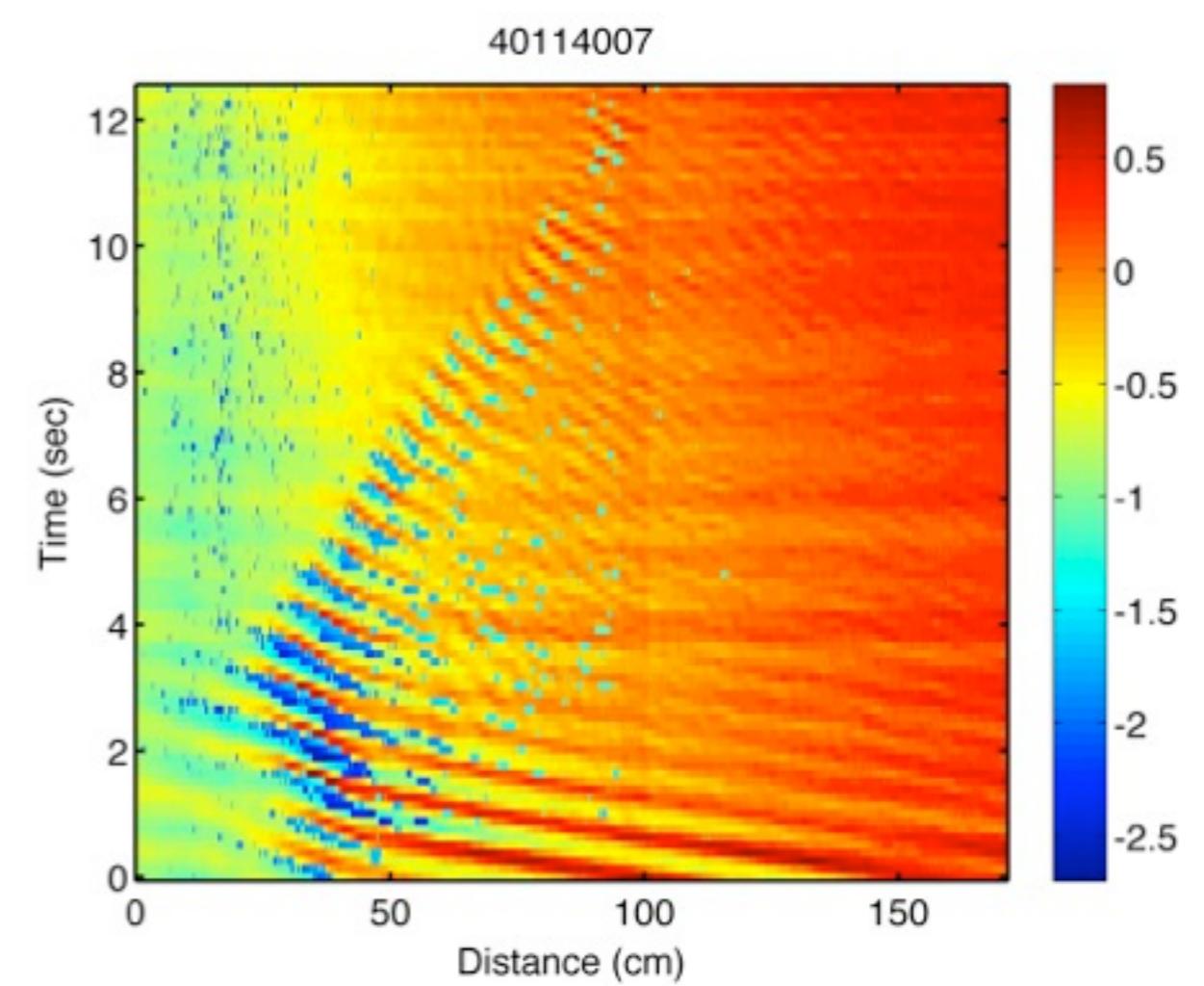
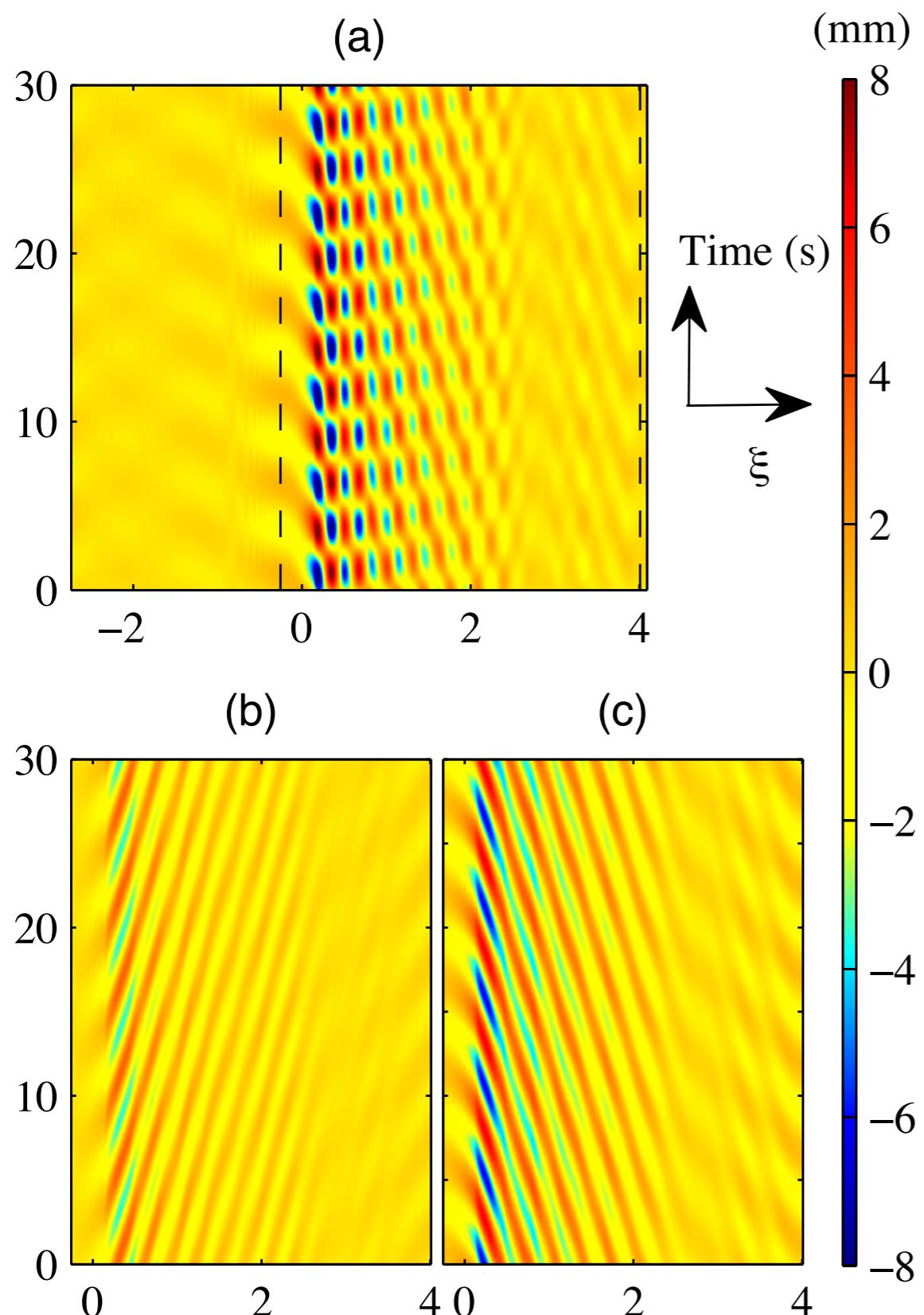


Wave: tion?

Our experiment ➤ Pair-creation process

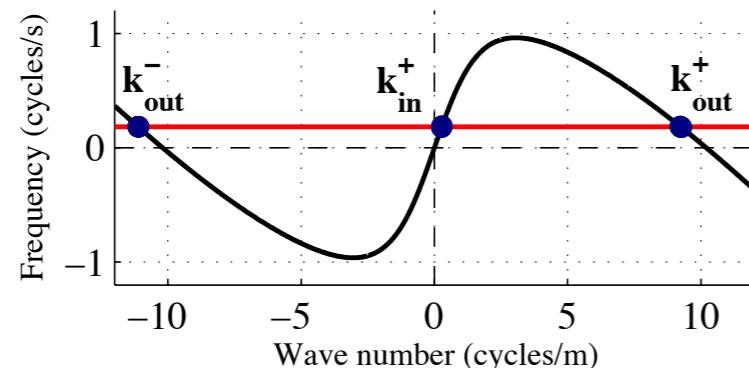


Our experiment ➤ Group versus phase velocity horizon

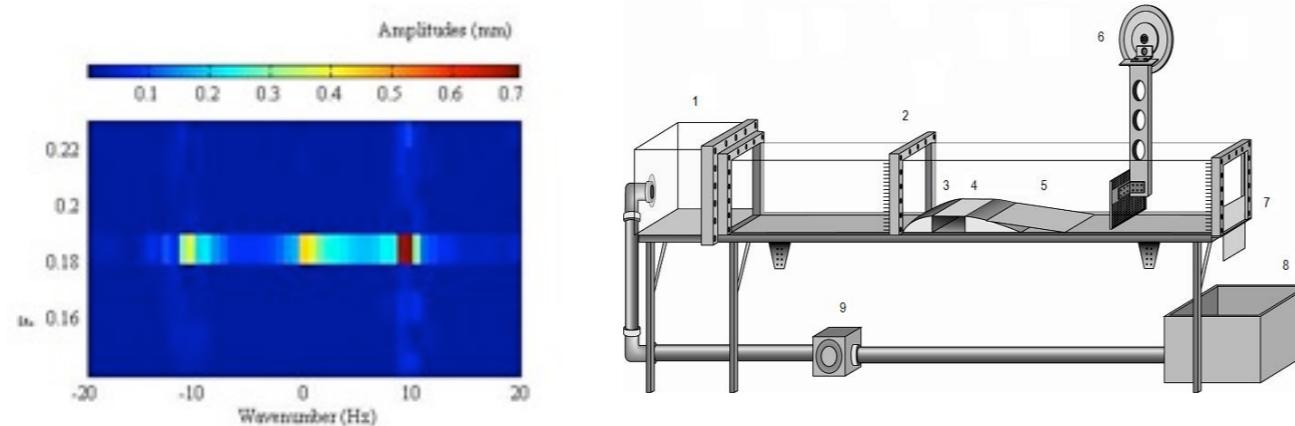


Our experiment ➤ Boltzmann distribution

(i) Amplitudes of converted waves depending on ingoing frequency:



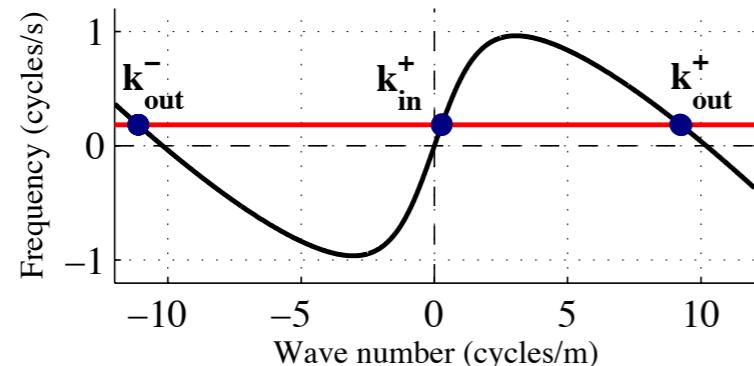
(ii) what is a wave (particle)
nearbythe white hole horizon..?



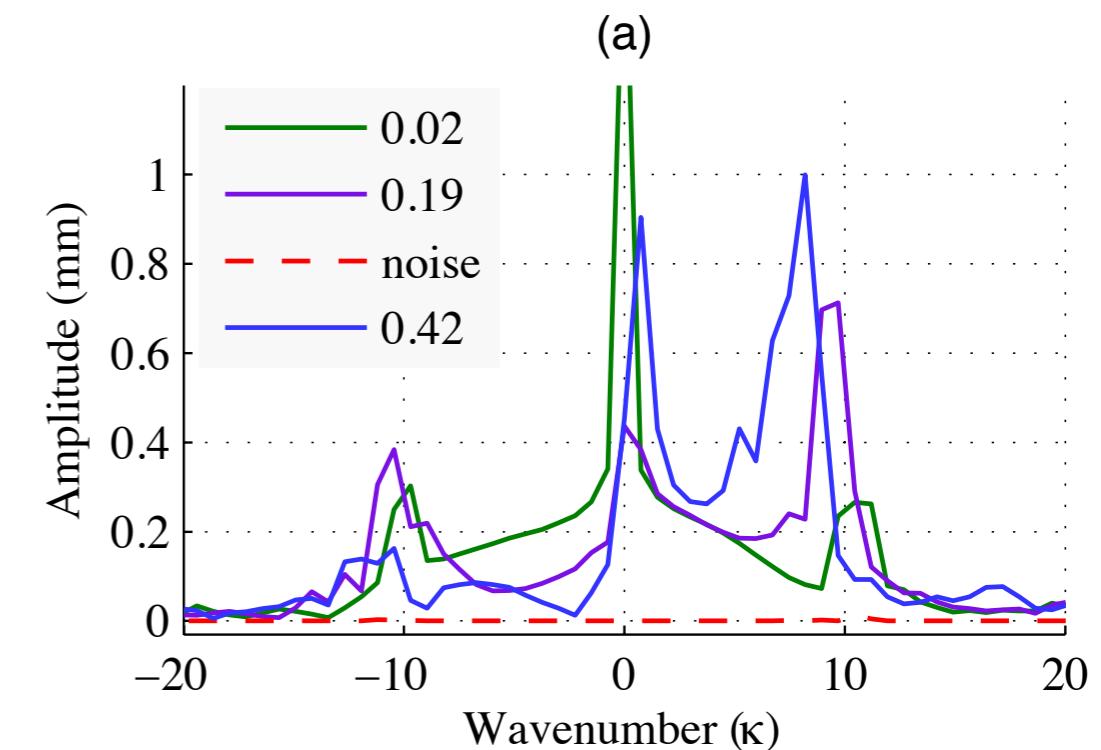
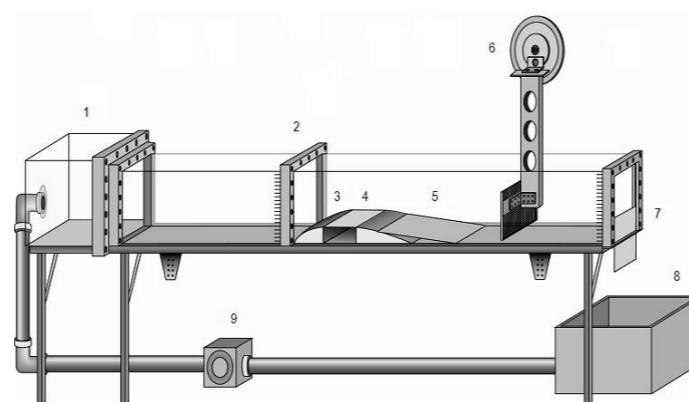
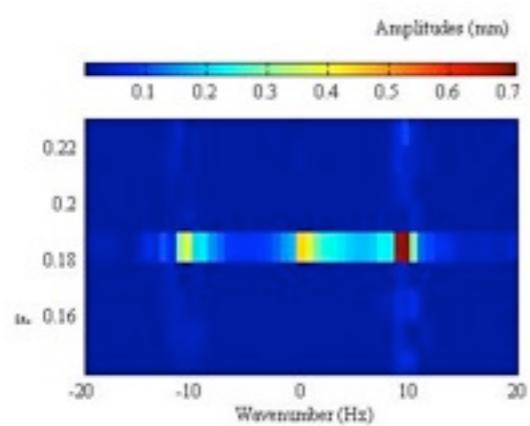
(ii) Norm is conserved: $\int \frac{|A(f, \kappa)|^2}{f + \kappa} d\kappa$

Our experiment ➤ Boltzmann distribution

(i) Amplitudes of converted waves depending on ingoing frequency:



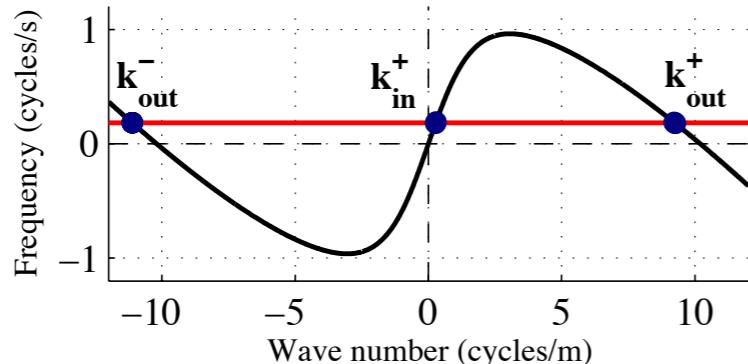
(ii) what is a wave (particle) nearby the white hole horizon..?



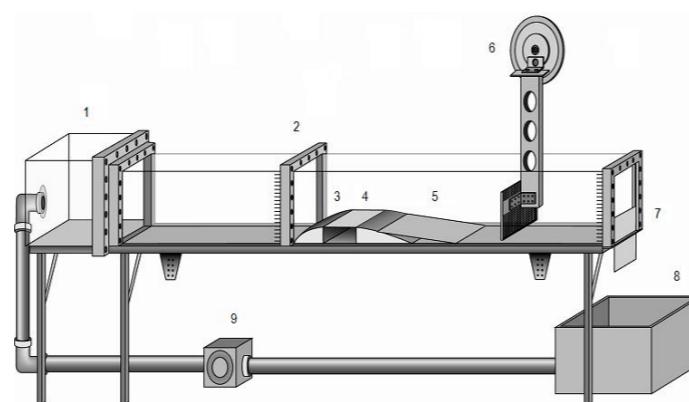
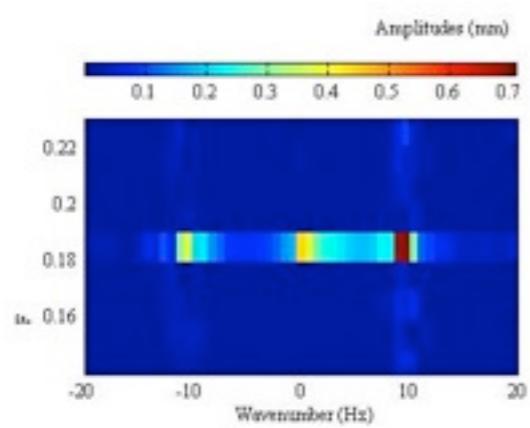
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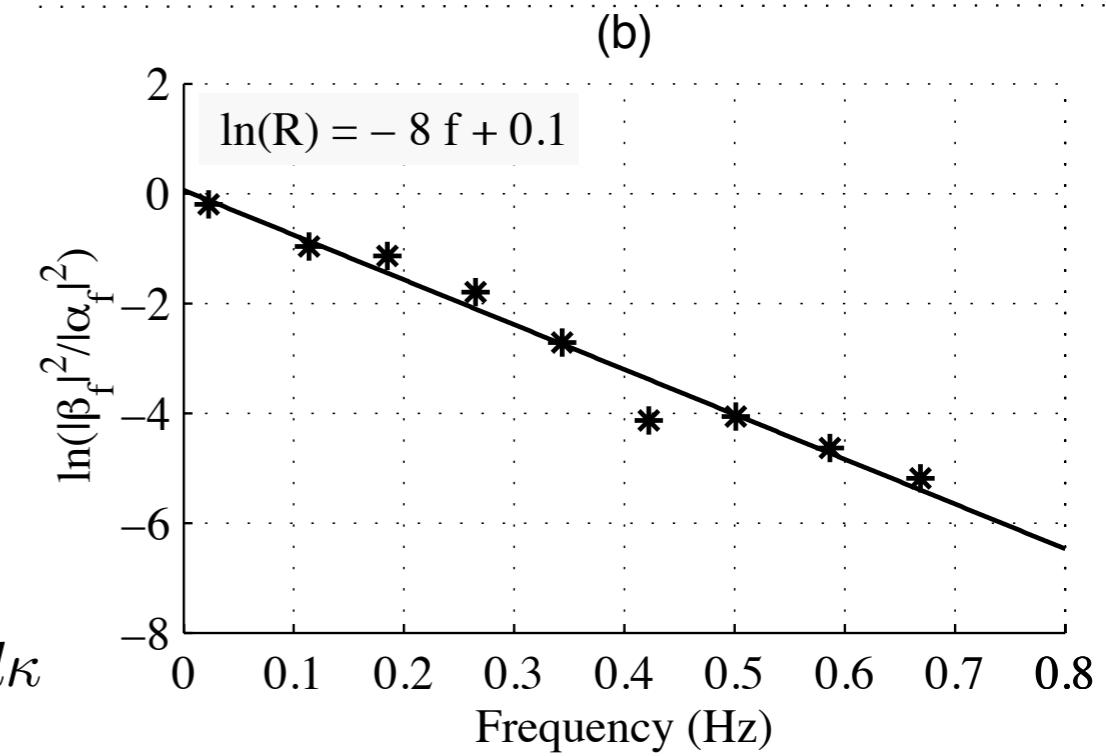
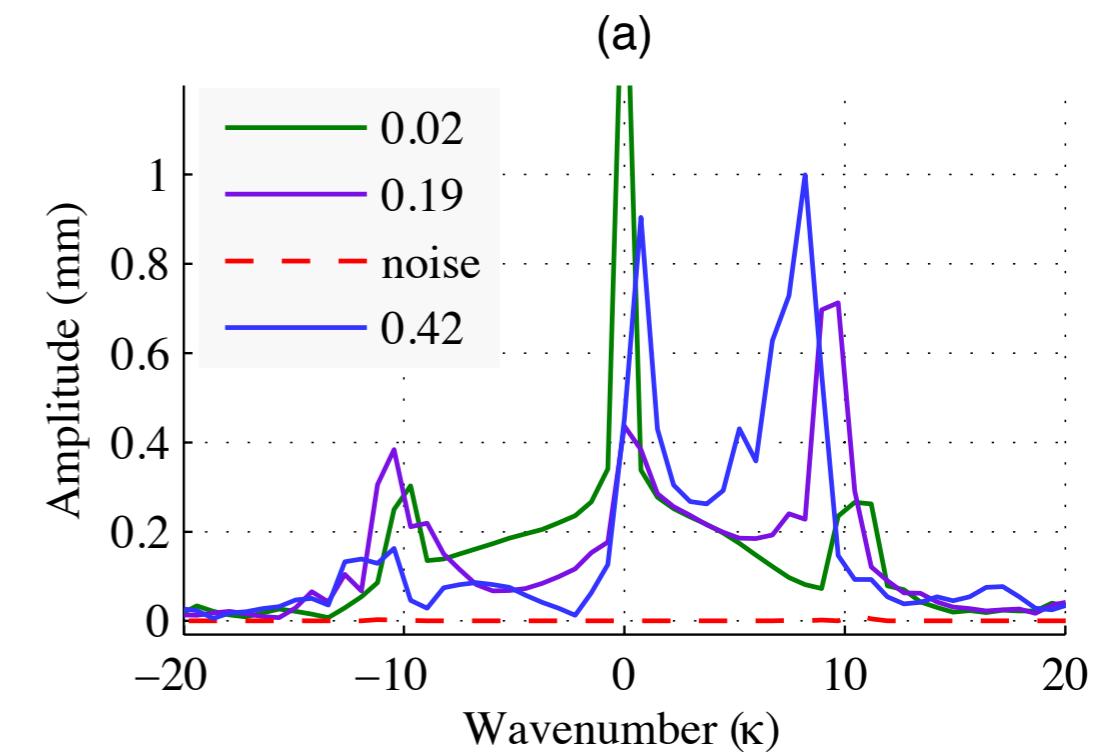


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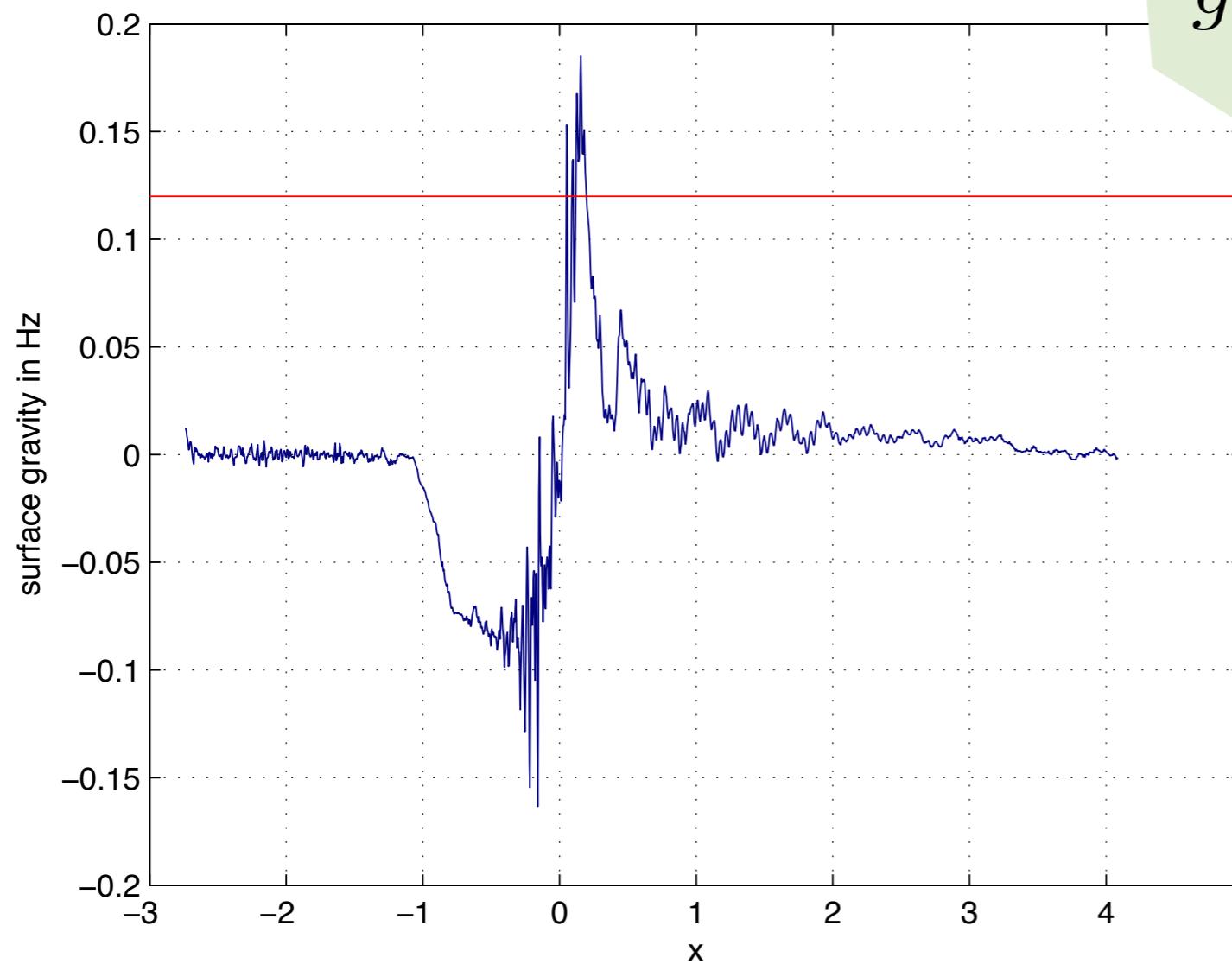
(ii) Norm is conserved:

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Our experiment ➤ Surface gravity

- BH evaporation: $|\beta_\omega|^2 = e^{-\frac{2\pi\omega}{g_H}} |\alpha_\omega|^2$



$$g_H = \frac{1}{2} \frac{\partial(c^2 - v^2)}{\partial n}$$

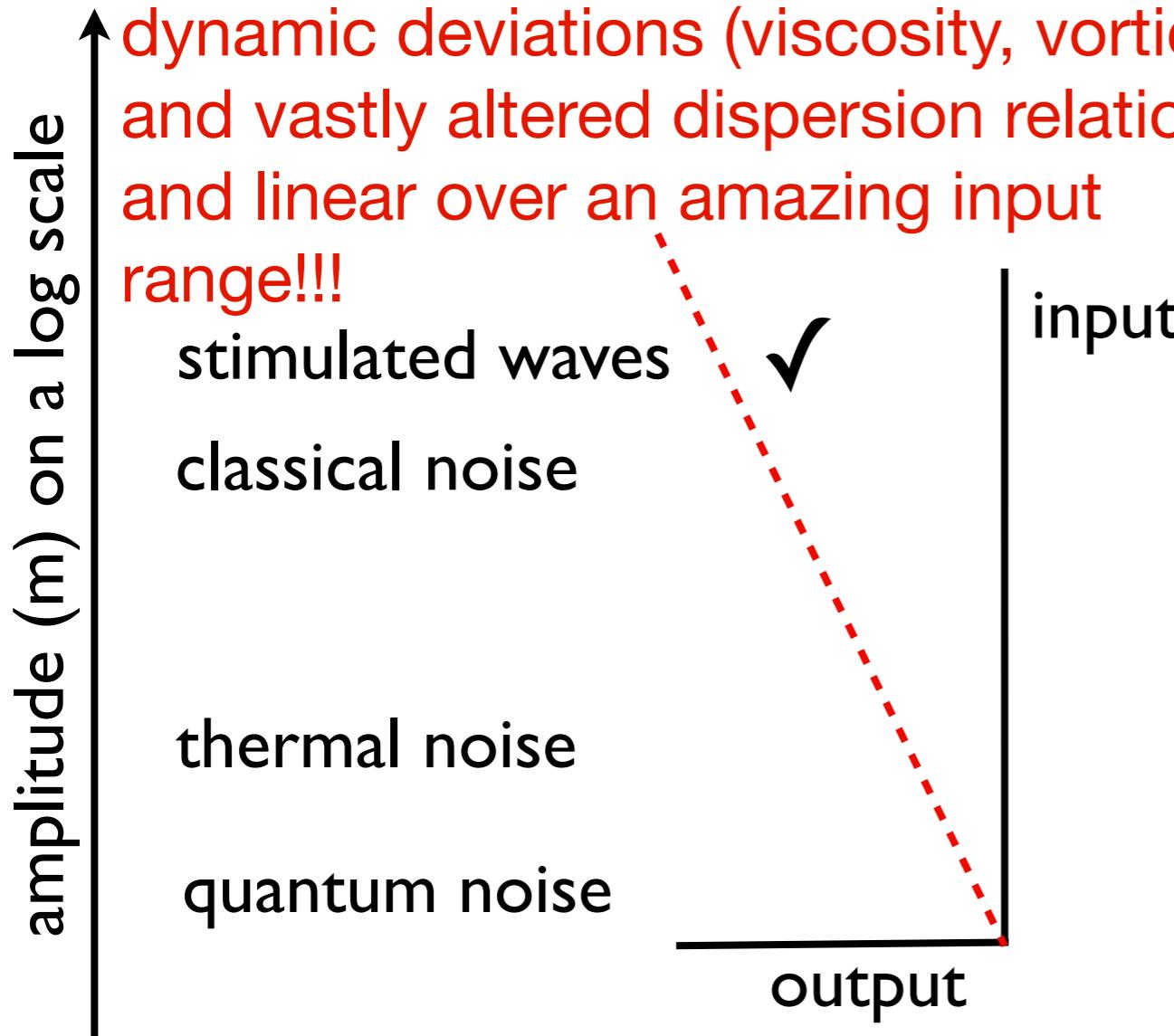
surface gravity (Hz)
via excitations:
0.12 Hz

surface gravity (Hz)
via background:
0.08-0.18 Hz



Our experiment ➤ Summary

Lesson: The thermal emission is a universal phenomenon, surviving fluid-dynamic deviations (viscosity, vorticity) and vastly altered dispersion relations, and linear over an amazing input range!!!



Assumption:

Linear amplifier over a huge range!

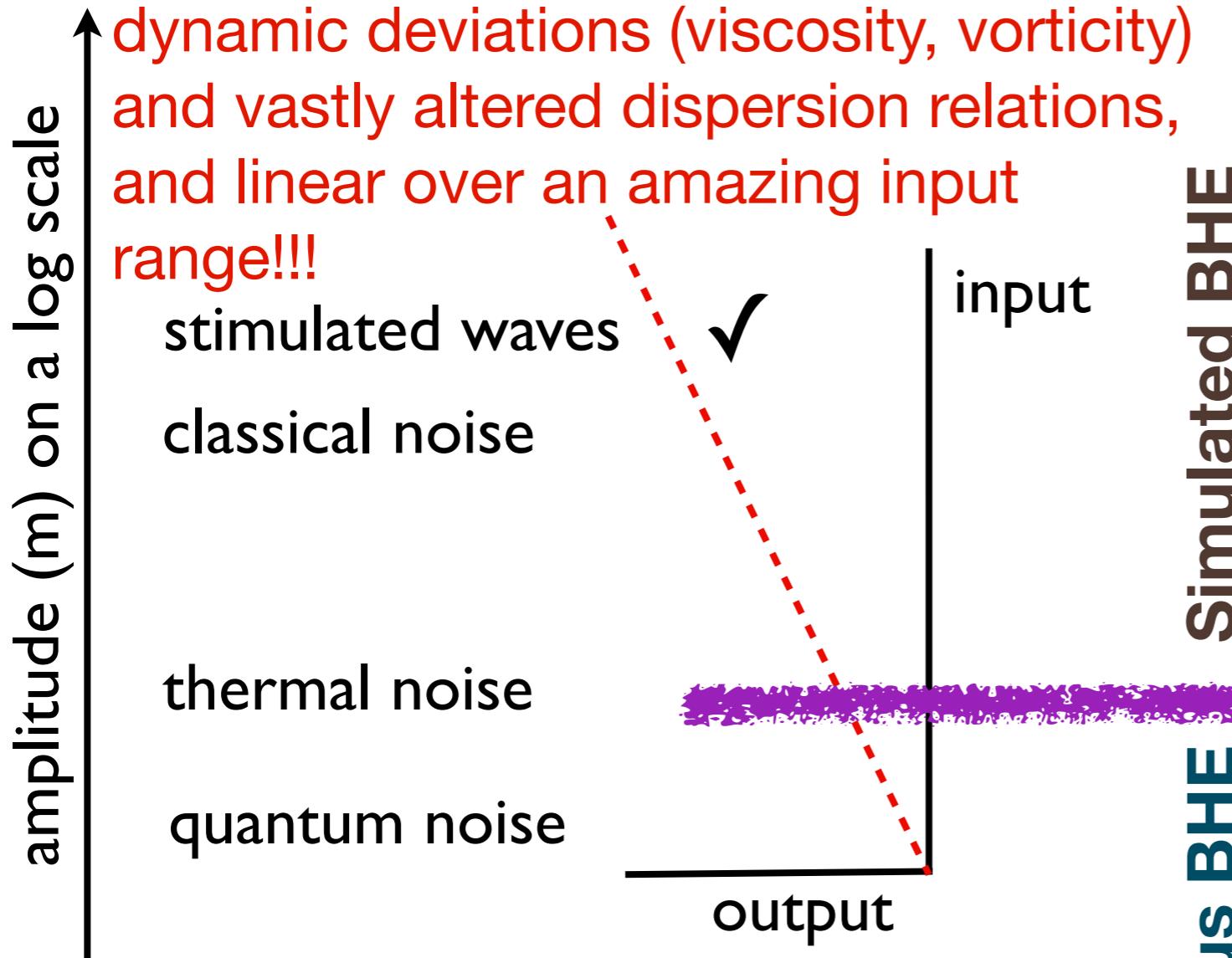
- ✓ pair-creation process (classical correlations)
- ✓ Boltzmann distribution
- ✓ surface gravity



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Spontaneous BHE Simulated BHE

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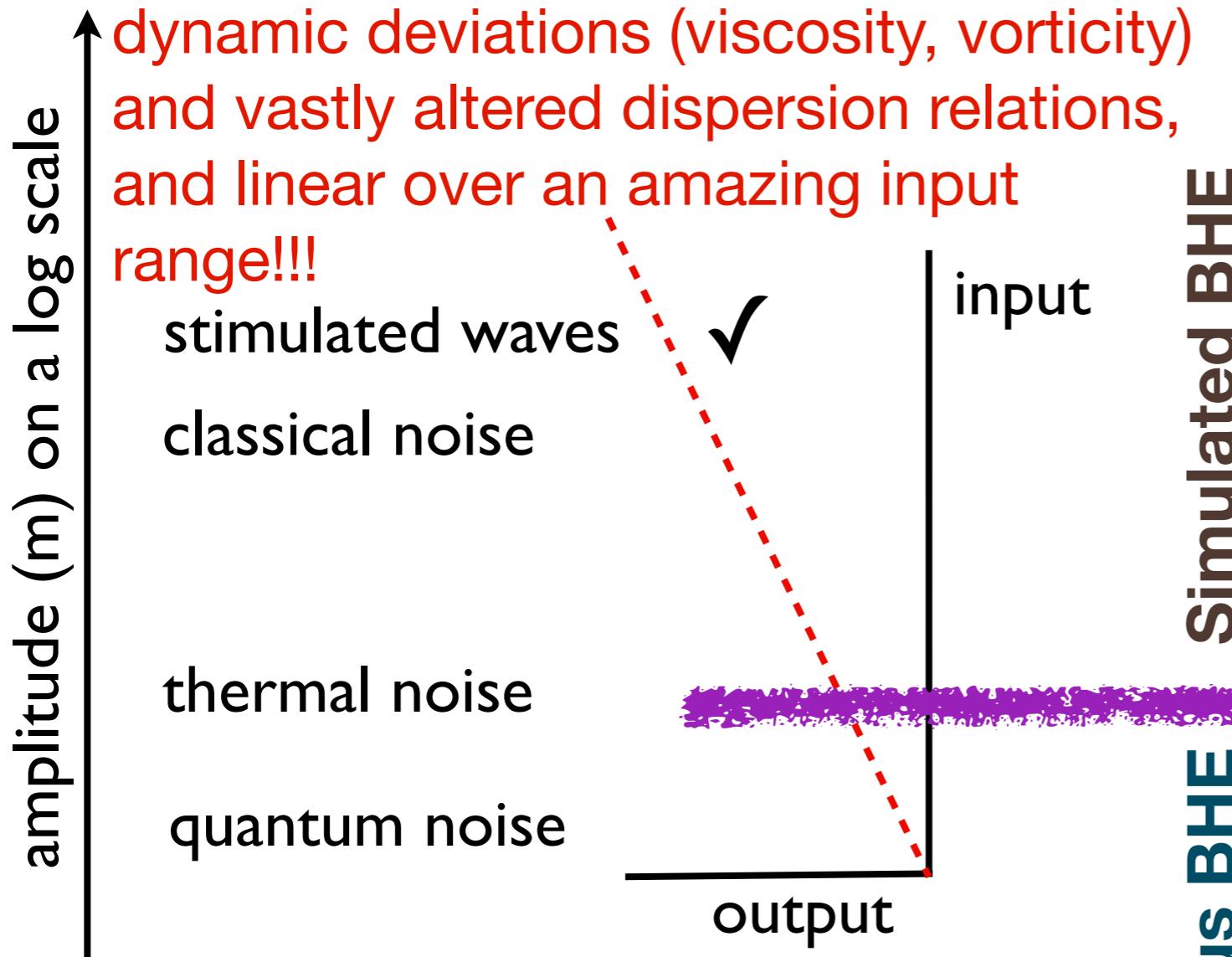


- ✓ quantum correlations



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there is **NO UV-problem
in our system...**

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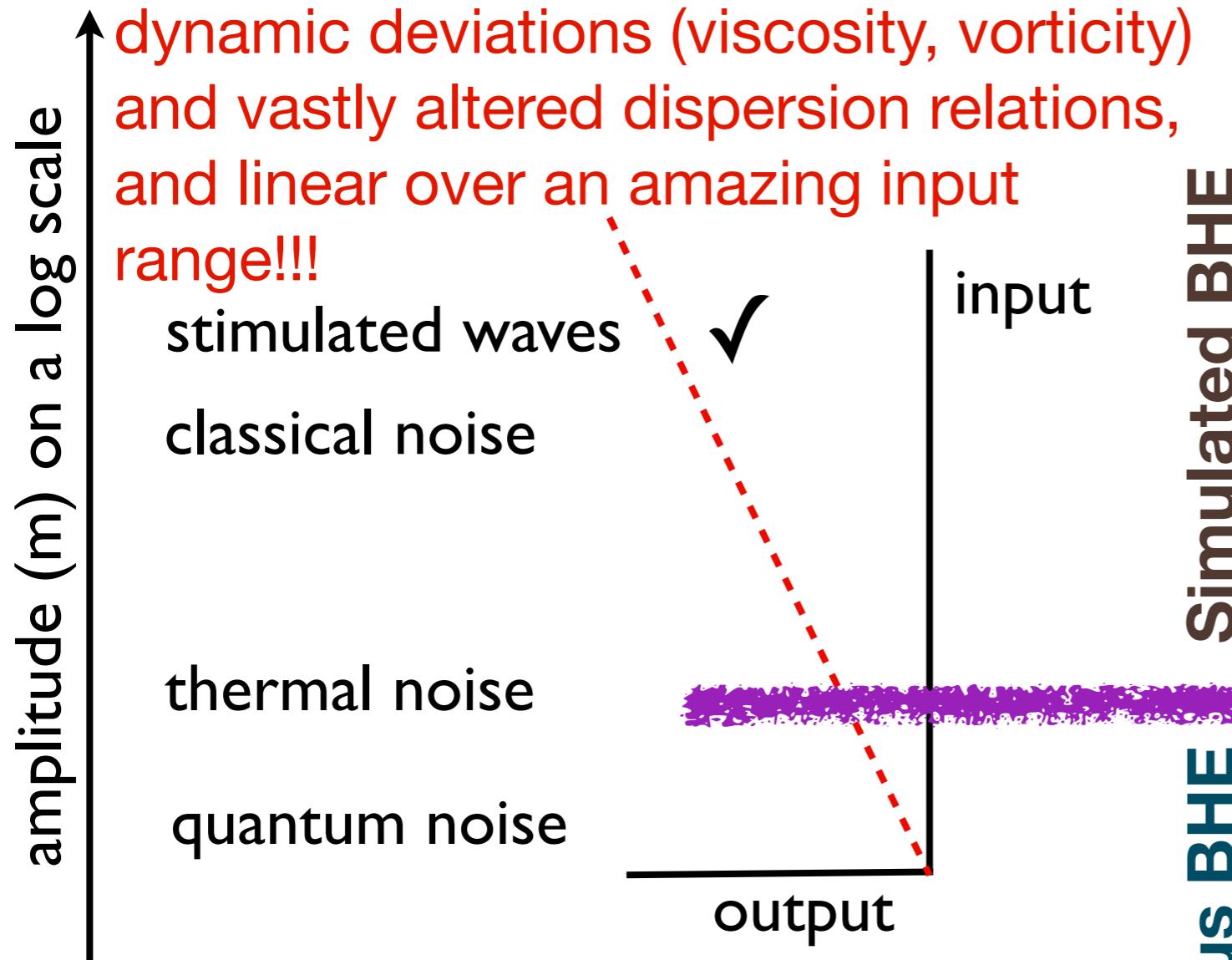


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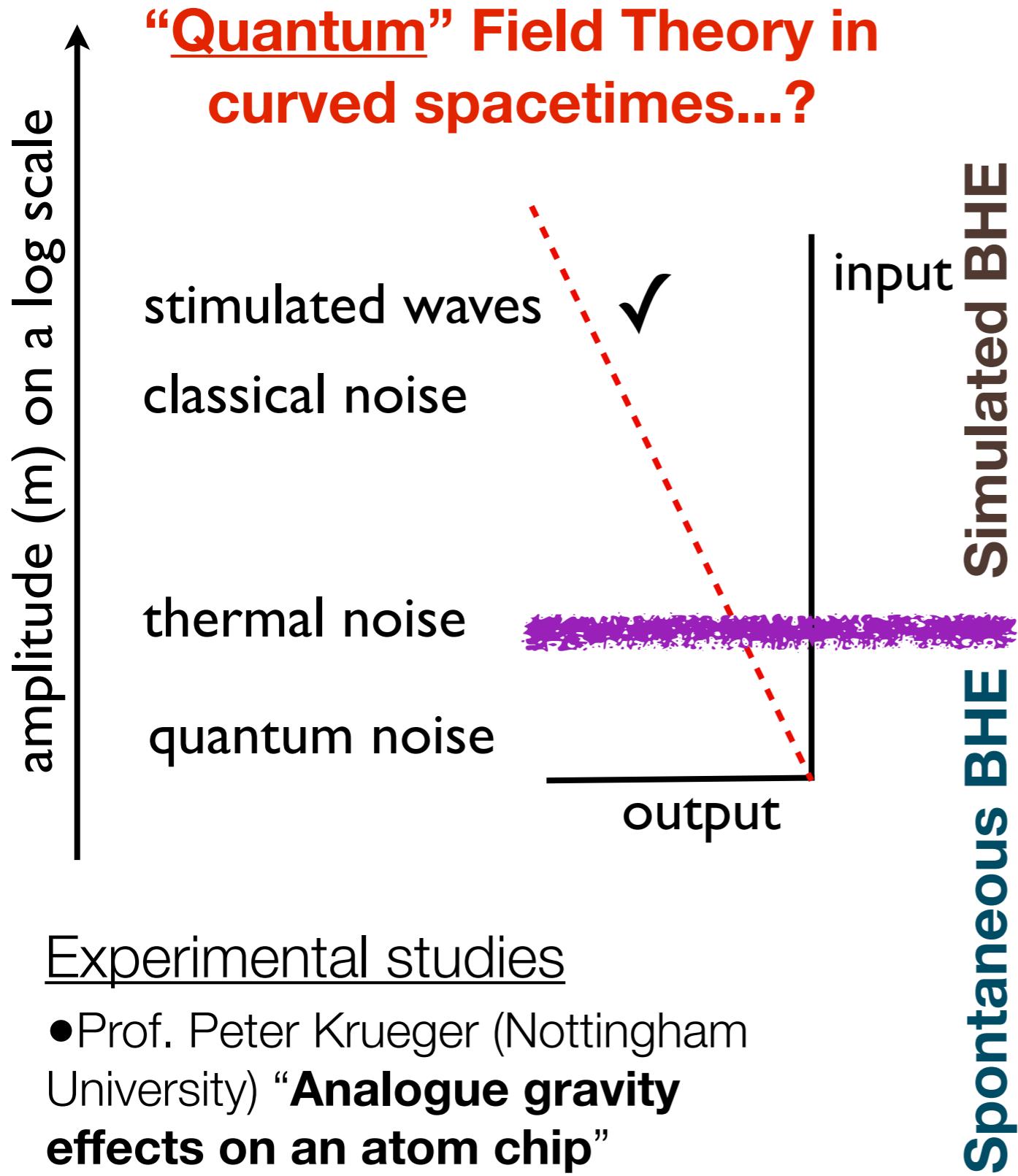
- ✓ pair-creation process (classical correlations)
- ✓ Boltzmann distribution
- ✓ surface gravity



However: Spontaneous emission straightforward, but un- detectable (6×10^{-12} K); superfluid experiments necessary...

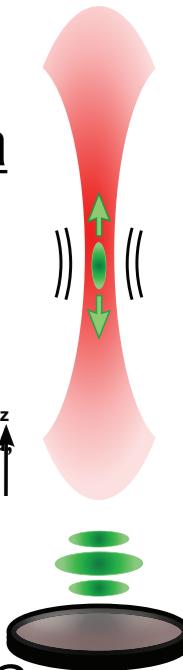
- ✓ quantum correlations

Future experiments ➤ “Quantum” field theory in



An acoustic analog to the dynamical Casimir effect in a Bose--Einstein condensate: Classical or quantum correlations?

Jean-Christophe Jaskula, Guthrie B. Partridge, Marie Bonneau,
Raphael Lopes, Josselin Ruadet, Denis Boiron, Christoph I.
Westbrook



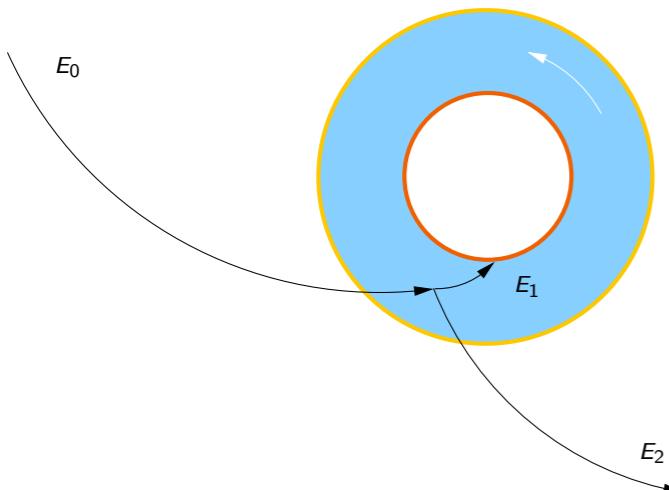
Theoretical studies in progress

- “**On the robustness of entanglement in analogue gravity systems**” in collaboration with Ivette Fuentes, Nicolai Friis, David Bruschi.
- “**Entanglement measures in parametrically excited Bose-Einstein condensates**” in collaboration with Piyush Jain.
- “**Analogue relativistic quantum information**” in collaboration with Ivette Fuentes and Piyush Jain.

New experiment - ongoing experiments at SISSA/ICTP/Elettra

Description: Experimental studies of effective rotating black holes, to detect:

- superradiant wave-scattering
- stimulated black-hole emission



Surface waves on stationary draining water / bathtub vortex / analogue rotating black hole...



...superfluid bathtub vortex flows

Theoretical studies:

- * Vortex geometry for the equatorial slice of the Kerr black hole (M. Visser, S.W.);
- * **In preparation:** Generalized superradiant scattering (M. Richartz, S.W., A.J. Penner, W.G. Unruh);
- * **ArXiv:** Dispersive superradiant scattering (A. Prain, M. Richartz, S.W., S. Liberati)

Numerical studies:

- * In preparation: Experimental superradiant scattering (M. Richartz, J. Penner, A. Prain, J. Niemela, S.W.)

Experiment studies:

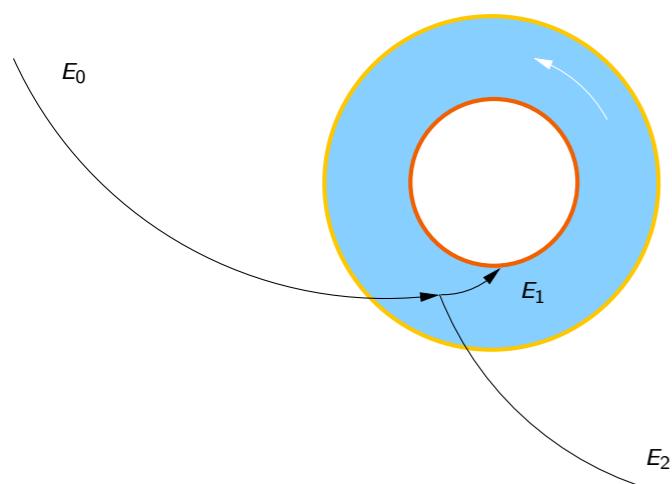
- * surface wave detection
- * design for water flume
- * prototype ready for experiments
- * big water flume
($3 \times 1.5 \times 0.5$ meter)
under construction



The team:

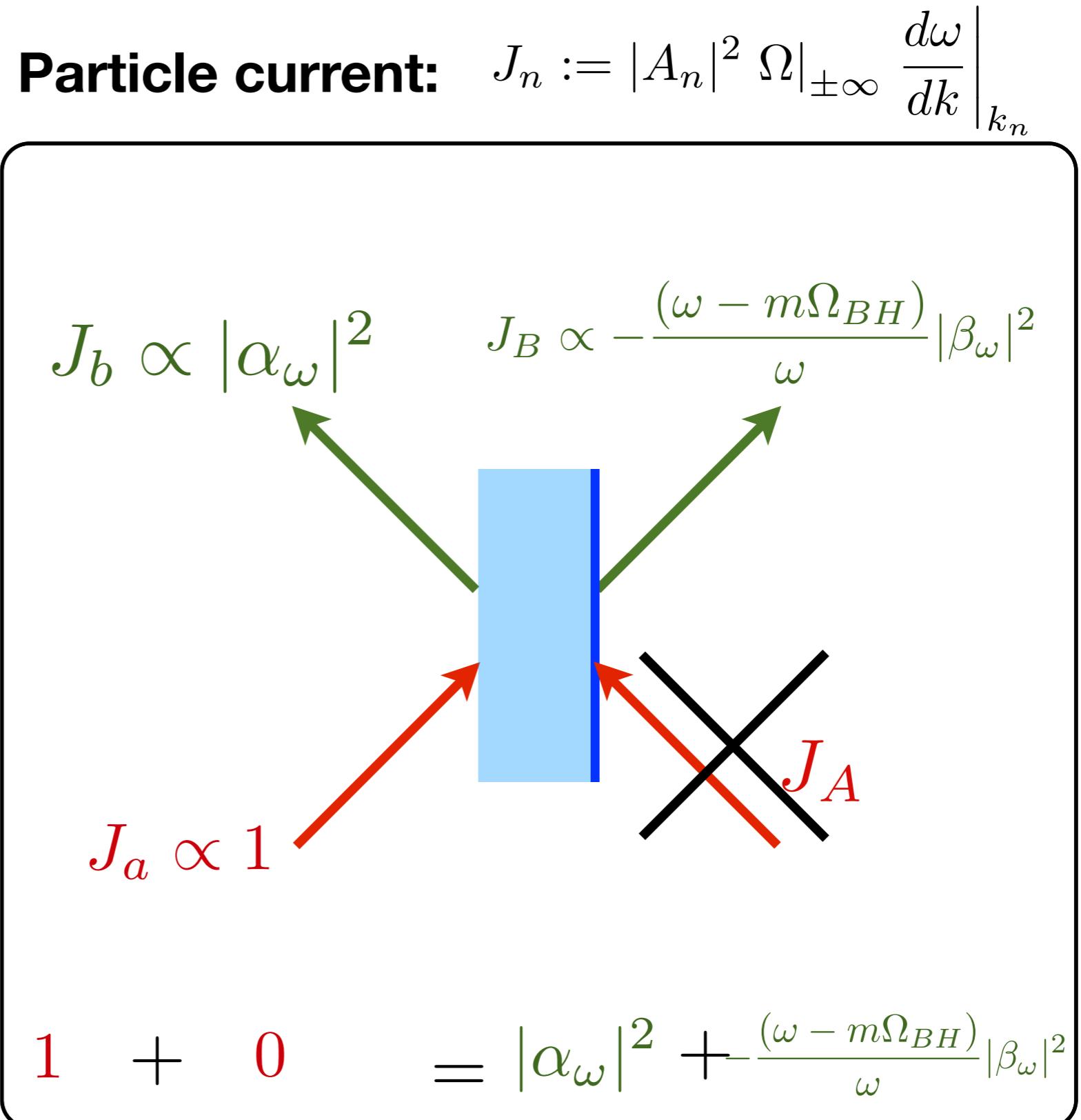
- * **Prof. J. Niemela** (ICTP), Matt Penrice and Ted Tedford
- * Prof. S. Liberati (SISSA), Dr. M. Richartz (Brasil), Dr. J. Penner (France), Dr. M. Danailov, A. Prain.

New experiment ➤ Superradiant wave scattering

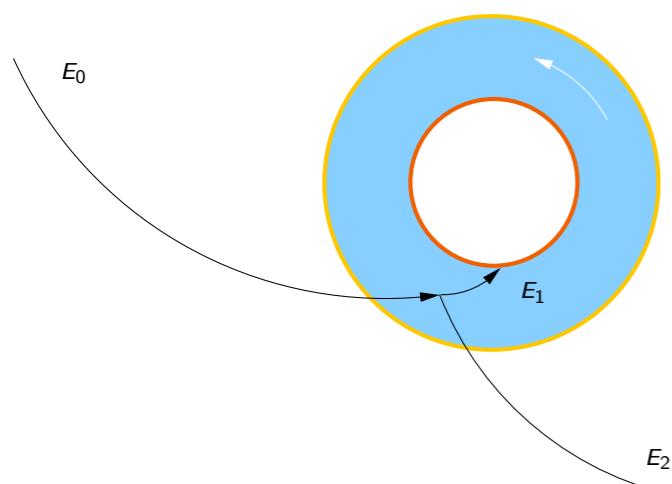


$$|R|^2 = 1 - \frac{(\omega - m\Omega_{BH})}{\omega} |T|^2$$

Dispersive superradiant scattering (A. Prain, M. Richartz, S.W., S. Liberati)



New experiment ➤ Superradiant wave scattering



$$|R|^2 = 1 - \frac{(\omega - m\Omega_{BH})}{\omega} |T|^2$$

Dispersive superradiant scattering (A. Prain, M. Richartz, S.W., S. Liberati)

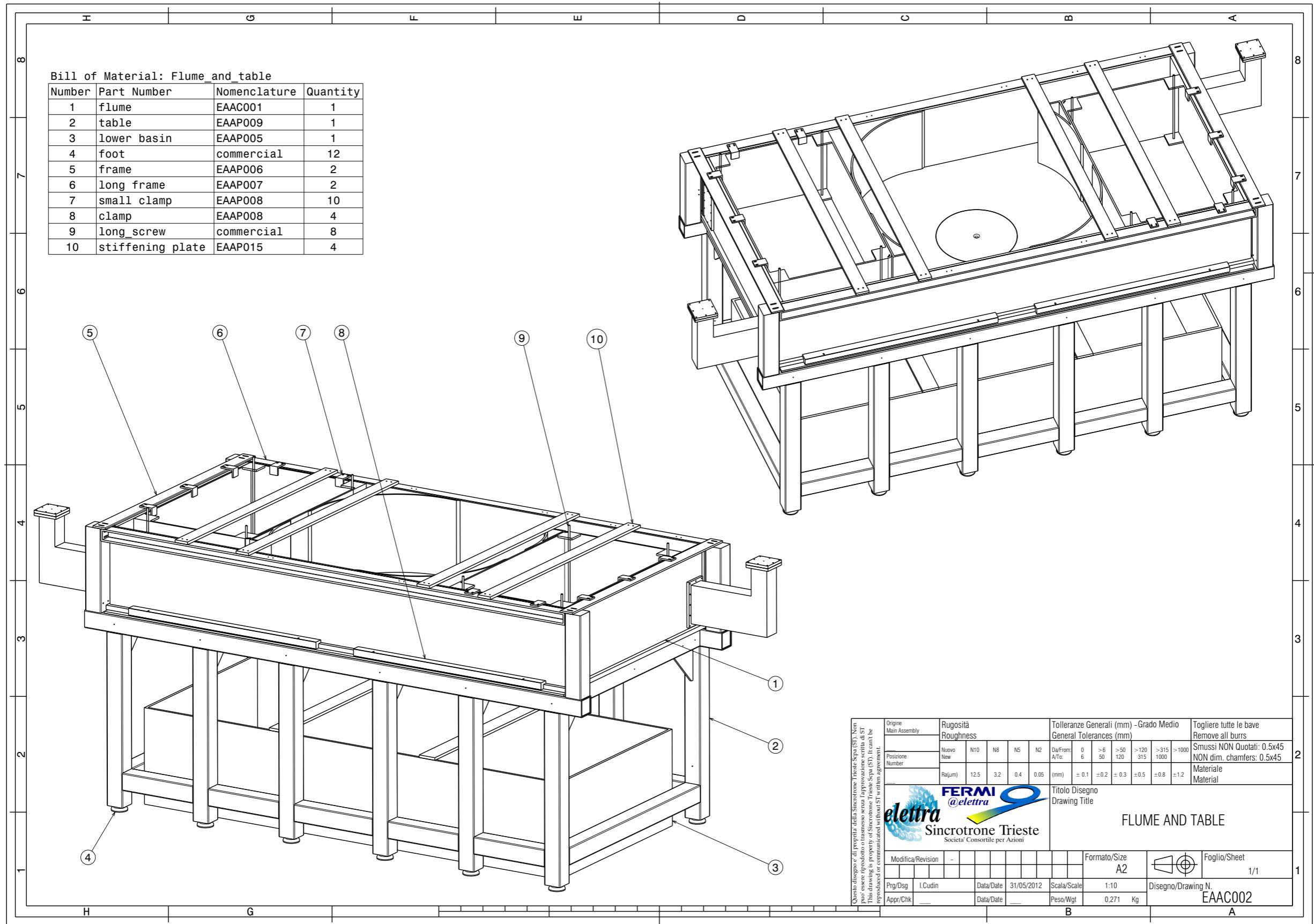
Particle current: $J_n := |A_n|^2 \Omega|_{\pm\infty} \left. \frac{d\omega}{dk} \right|_{k_n}$

$$J_b \propto |\alpha_\omega|^2 \quad J_B \propto -\frac{(\omega - m\Omega_{BH})}{\omega} |\beta_\omega|^2$$

A diagram showing three vectors originating from a central vertical blue bar. A green vector labeled $J_b \propto |\alpha_\omega|^2$ points upwards and to the left. A green vector labeled $J_B \propto -\frac{(\omega - m\Omega_{BH})}{\omega} |\beta_\omega|^2$ points upwards and to the right. A red vector labeled $J_a \propto 1$ points downwards and to the left.

$$1 + 0 = |\alpha_\omega|^2 + \frac{(\omega - m\Omega_{BH})}{\omega} |\beta_\omega|^2$$

New experiment - ongoing experiments at SISSA/ICTP/Elettra



New experiment - ongoing experiments at SISSA/ICTP/Elettra

